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# Early-arrival waveform inversion for

Xukai Shen

SEP147 p73, p103

**2012 SEP Sponsor Meeting**

May 22<sup>nd</sup> 2012

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# Outline

1. Motivation
2. Theory
3. Synthetic Examples
4. Conclusions



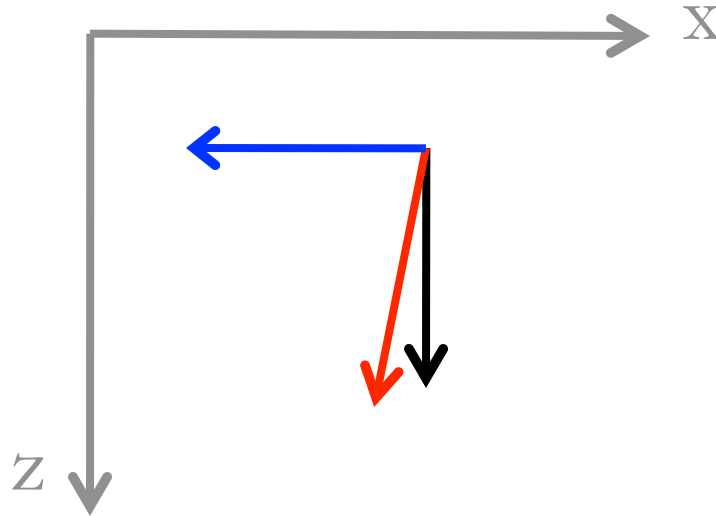
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# Introducing anisotropic parameters

Velocity vector diagram



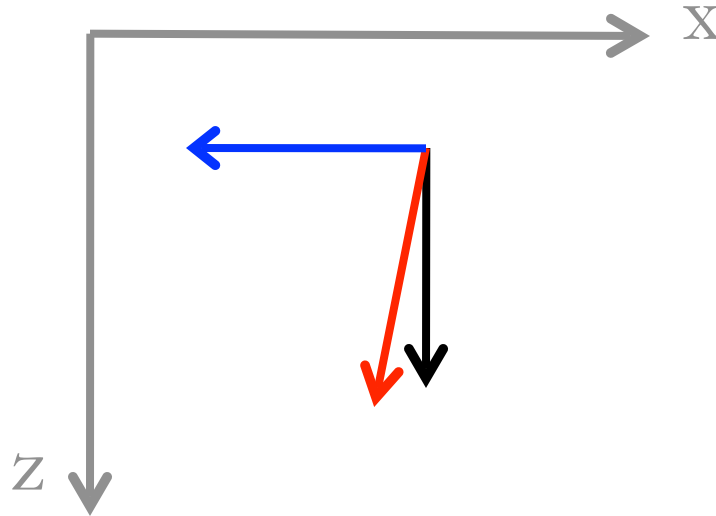
$v$  Vertical velocity

$\epsilon$  Anisotropic parameter

$\delta$  Anisotropic parameter

# Introducing anisotropic parameters

Velocity vector diagram



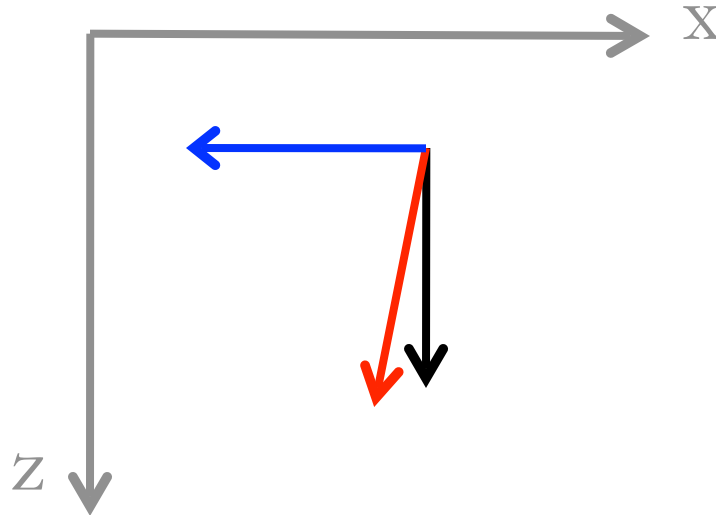
**v** Vertical velocity

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# Introducing anisotropic parameters

Velocity vector diagram



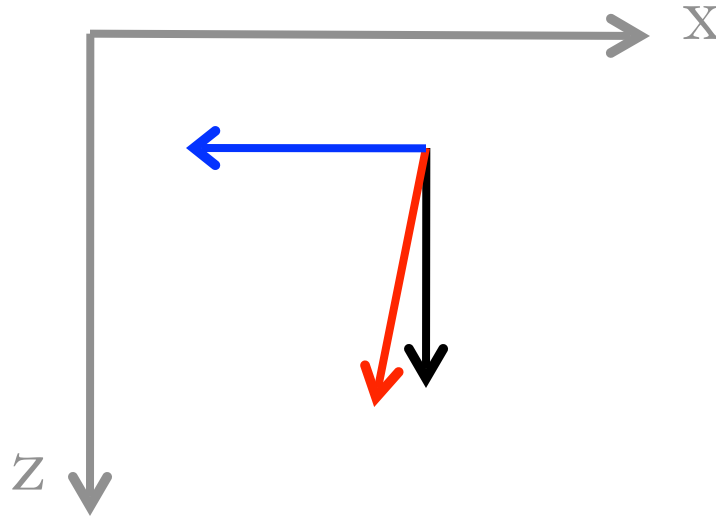
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# Introducing anisotropic parameters

Velocity vector diagram



**v** Vertical velocity

$\epsilon$  Anisotropic parameter

**$\delta$**  Anisotropic parameter

# Early Arrival Full Waveform Inversion (EAFWI)

$\min f(\mathbf{v})$

where

$$f(\mathbf{v}) = \sum_{s,r,t} \left\| \mathbf{d}_{\text{ea,obs}} - \mathbf{d}_{\text{ea,mod}}(\mathbf{v}) \right\|^2$$

$\mathbf{v}$       Near surface velocity

$\mathbf{d}_{\text{ea,obs}}$       Observed early arrivals

$\mathbf{d}_{\text{ea,mod}}$       Forward modeled early arrivals

# EAFWI

$\min f(\mathbf{v})$

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$$f(\mathbf{v}) = \sum_{s,r,t} \left\| \mathbf{d}_{\text{ea,obs}} - \mathbf{d}_{\text{ea,mod}}(\mathbf{v}) \right\|^2$$

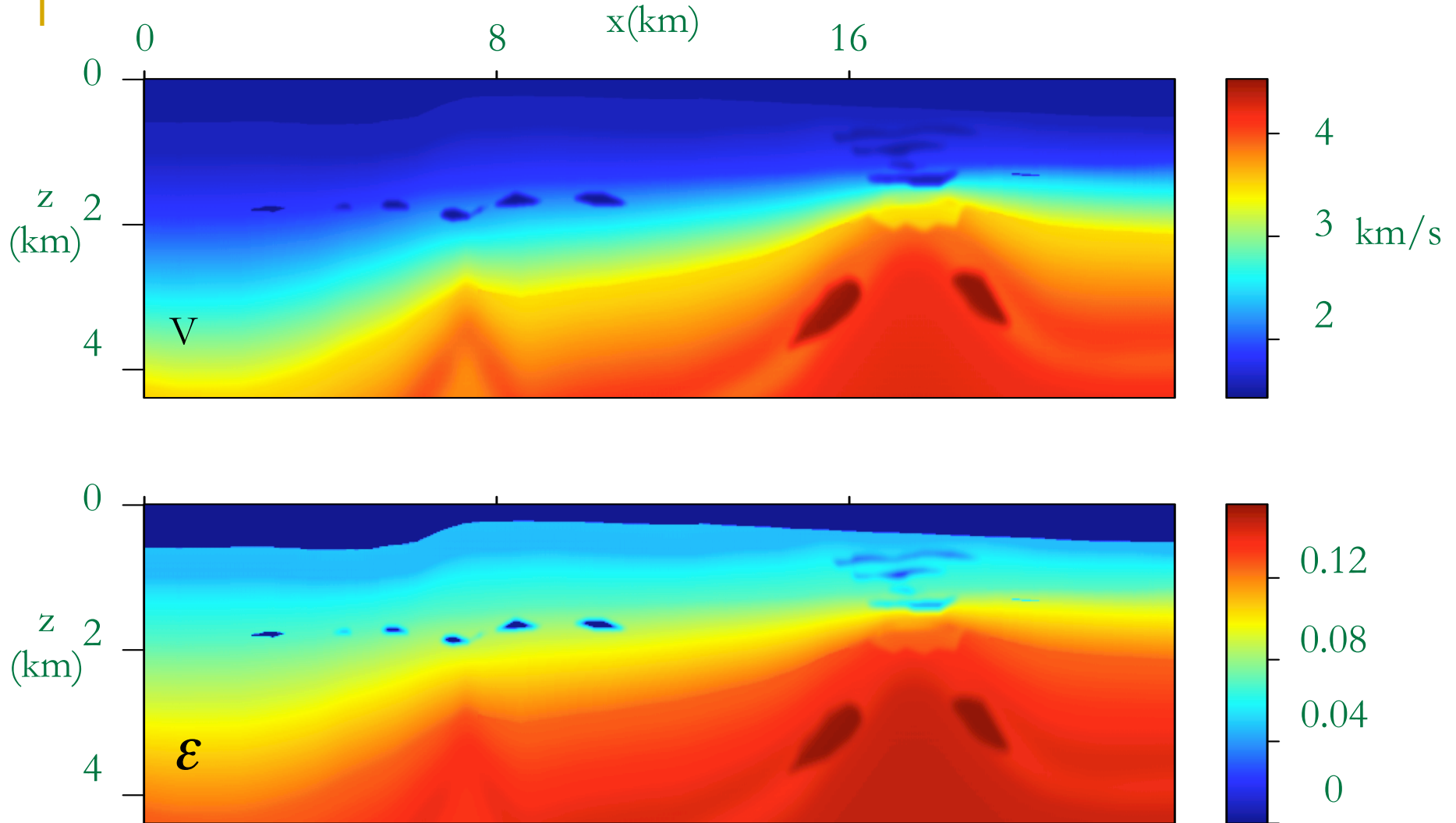
$\mathbf{v}$       Near surface velocity

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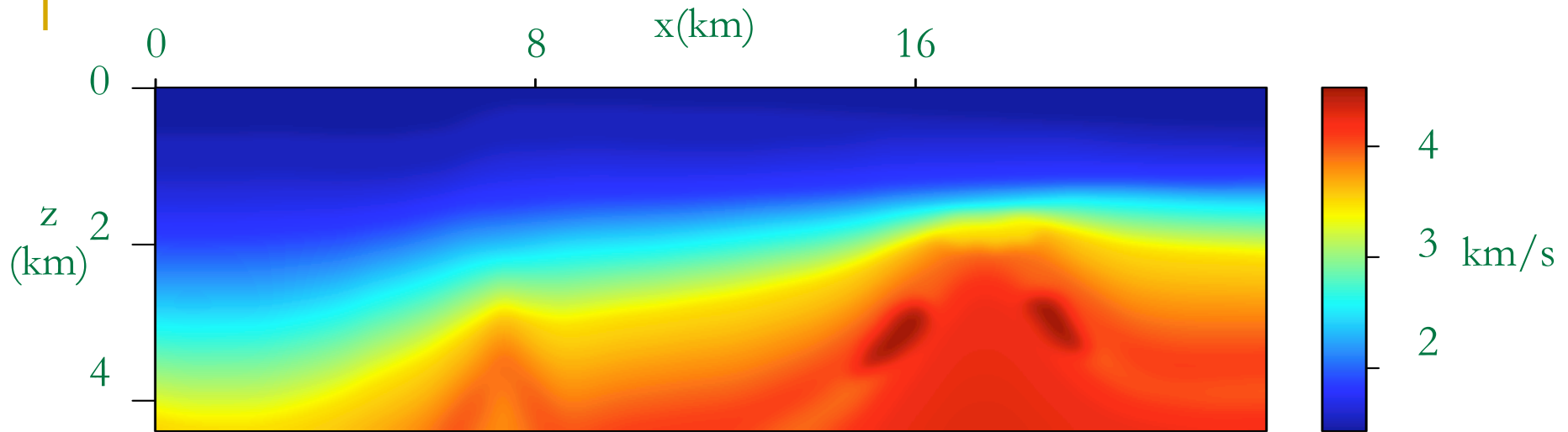
How does isotropic inversion of anisotropic data look like?

# True anisotropic model

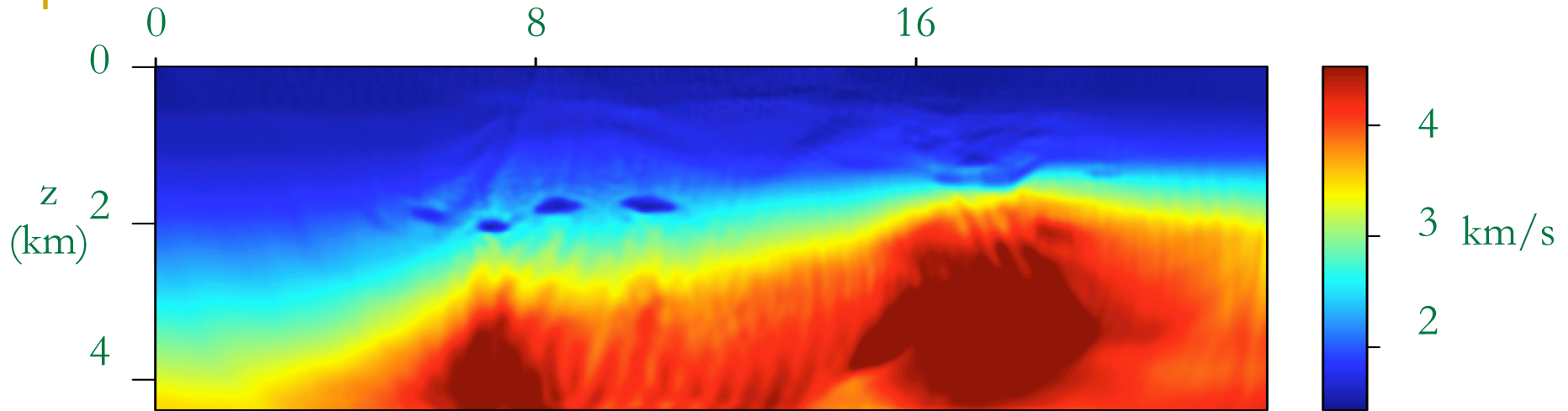




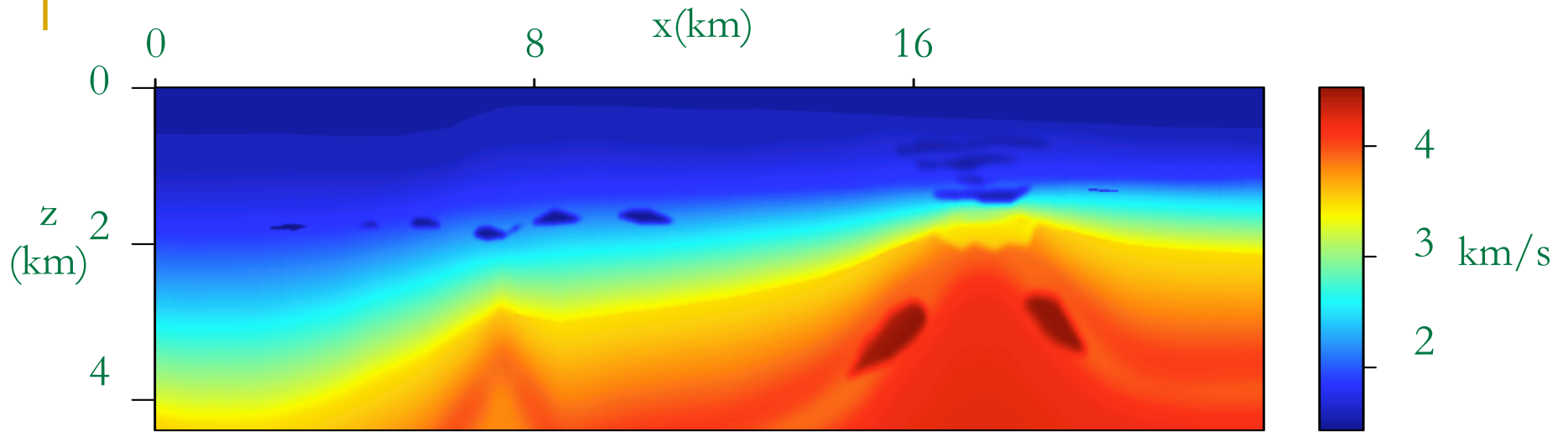
# Starting velocity for isotropic inversion



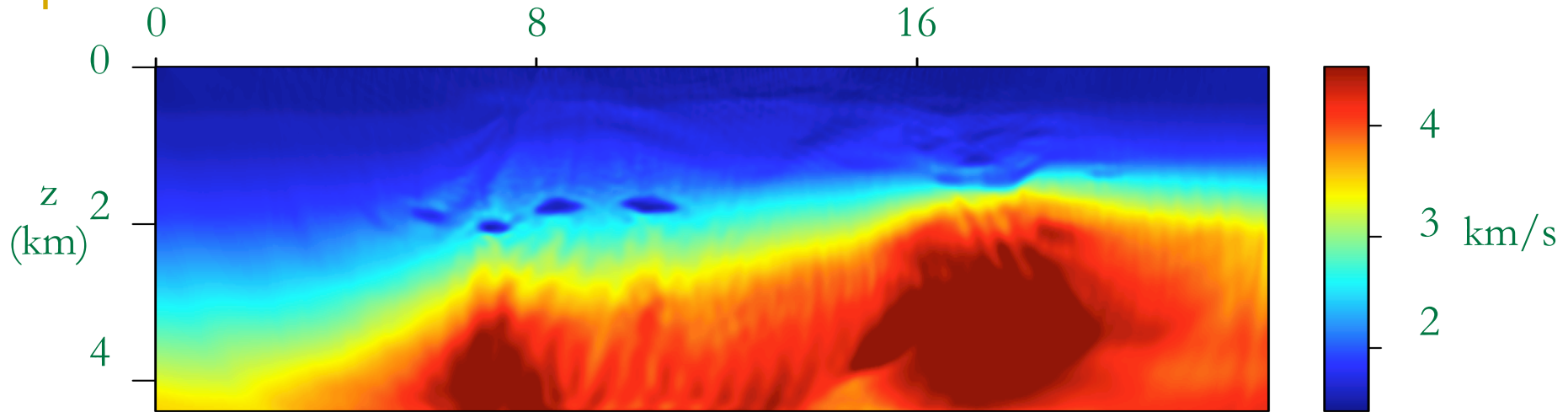
# Final velocity from isotropic inversion



# True isotropic velocity



# Final velocity from isotropic inversion



How does isotropic inversion of anisotropic data look like?

**Vertical stretch of true velocity model !**

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# Multi-parameter Waveform Inversion strategy:

Serial inversion (Gholami et al., 2011)

Joint inversion (Plessix and Rynja, 2010; Plessix and Cao, 2011)

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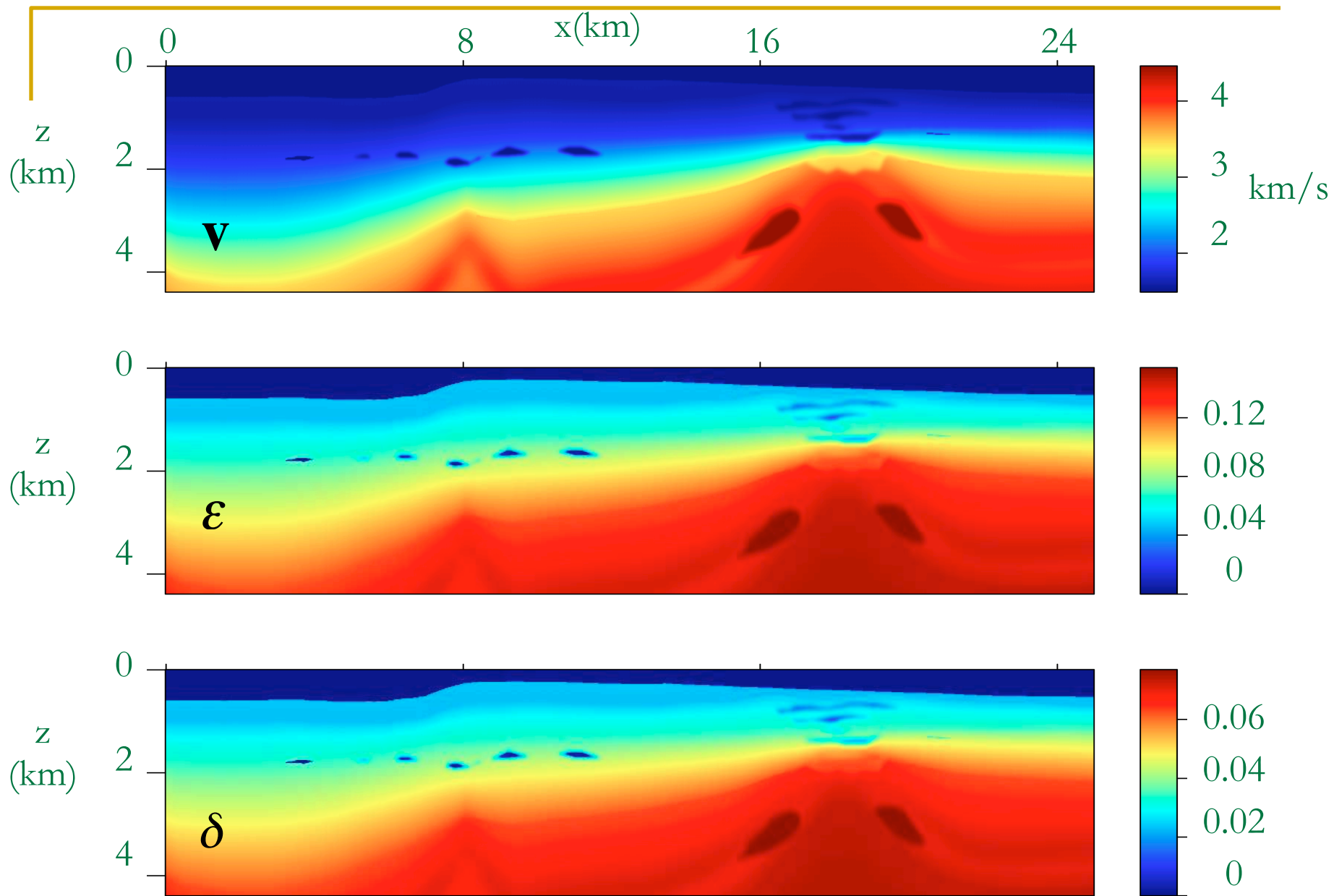
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# Data sensitivity to model perturbation

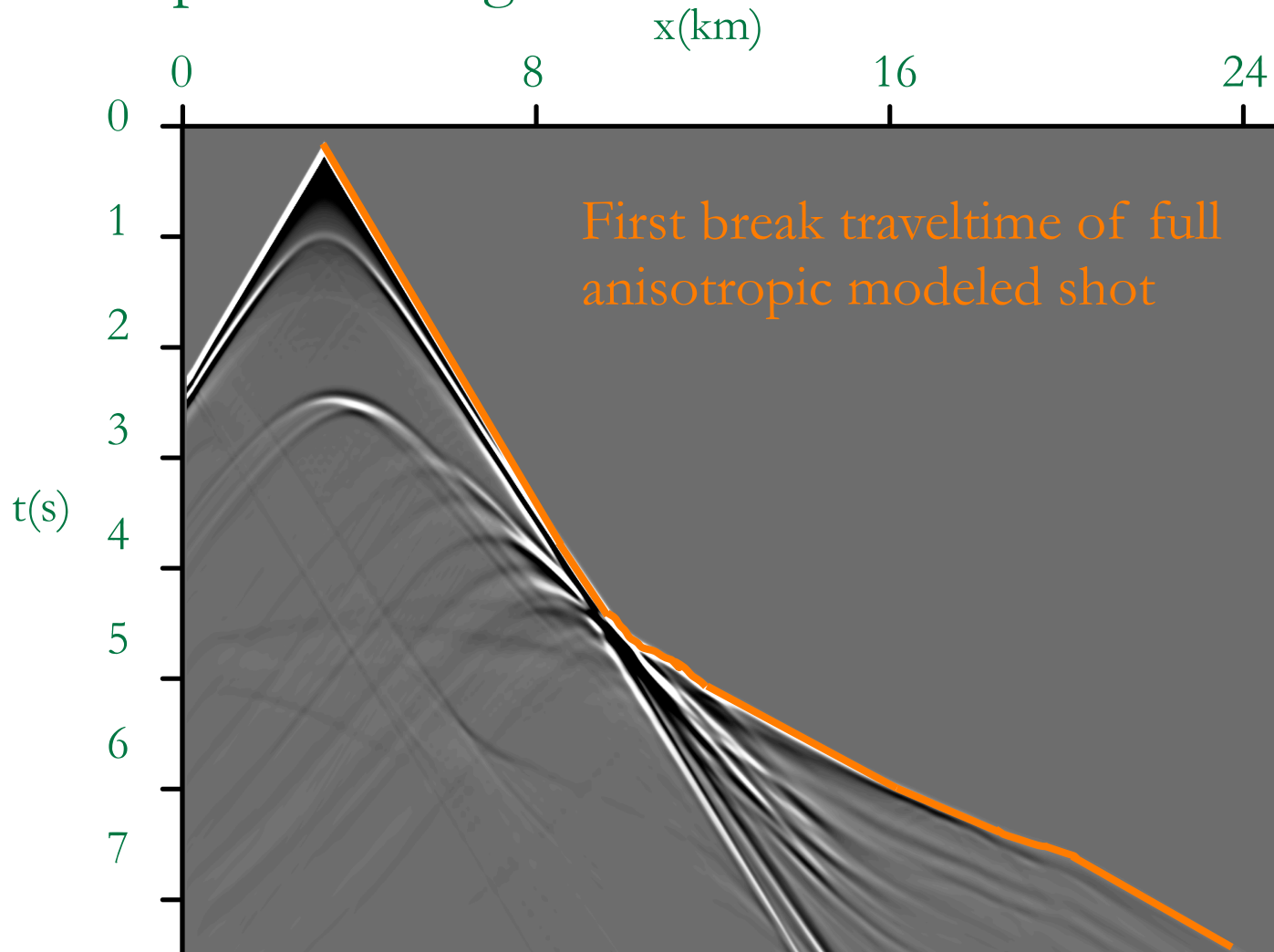
$$\mathbf{d}_{\text{ea,mod}}(\mathbf{v}, \varepsilon, \delta)$$

$\mathbf{v}$	Vertical near surface velocity
$\varepsilon$	Anisotropic parameter
$\delta$	Anisotropic parameter
$\mathbf{d}_{\text{ea,mod}}$	Modeled early arrivals

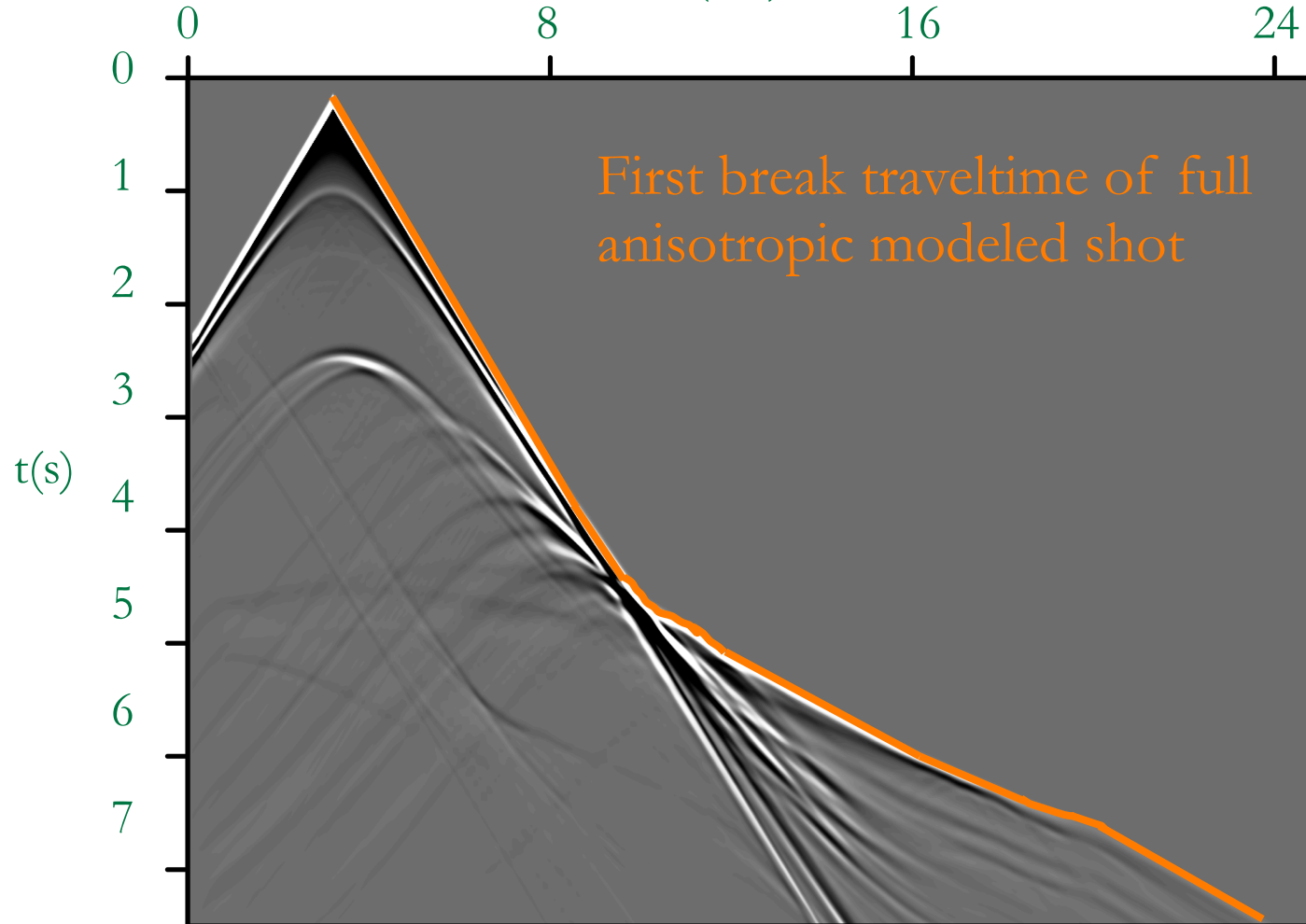




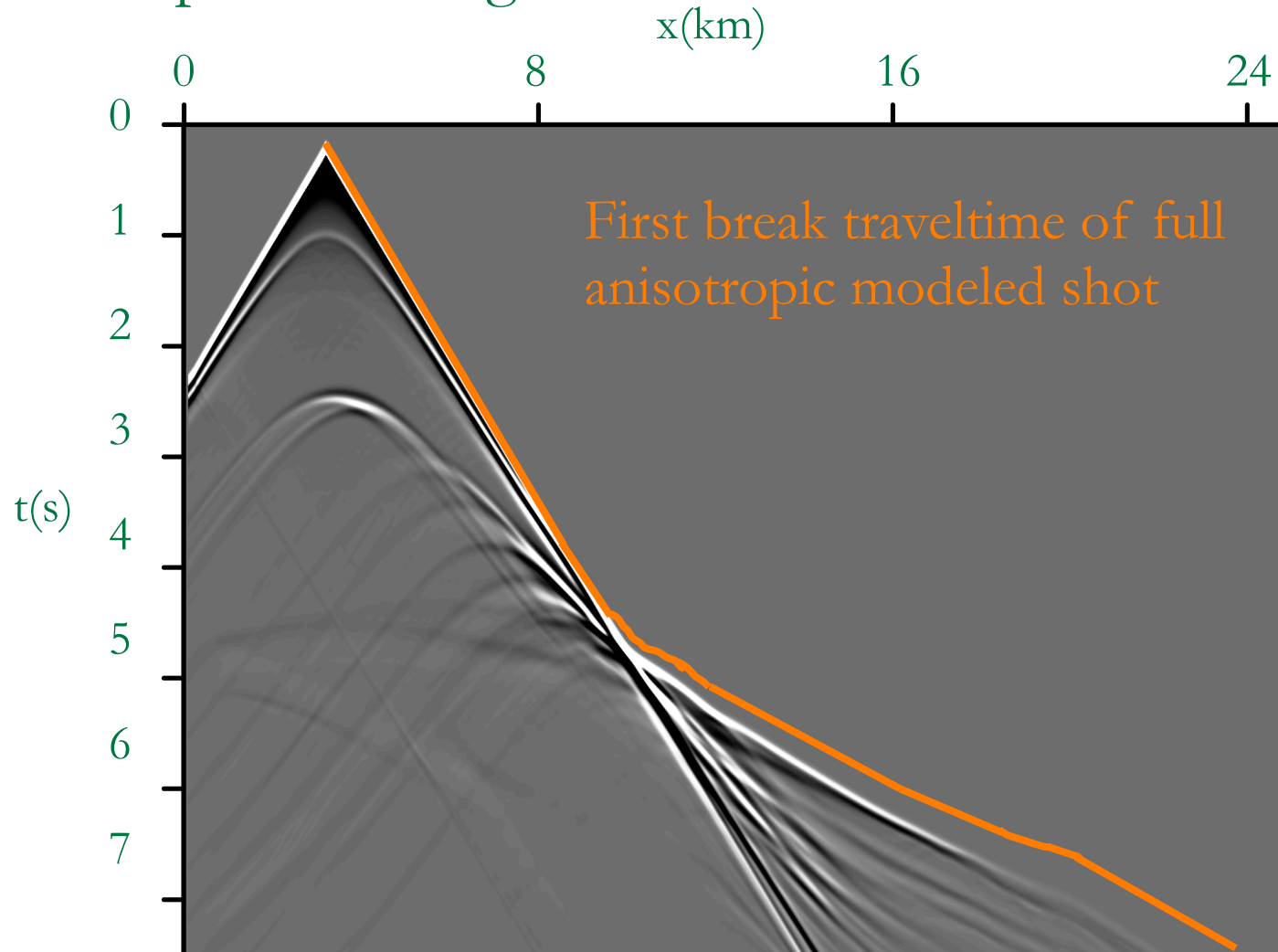
# Anisotropic modeling with

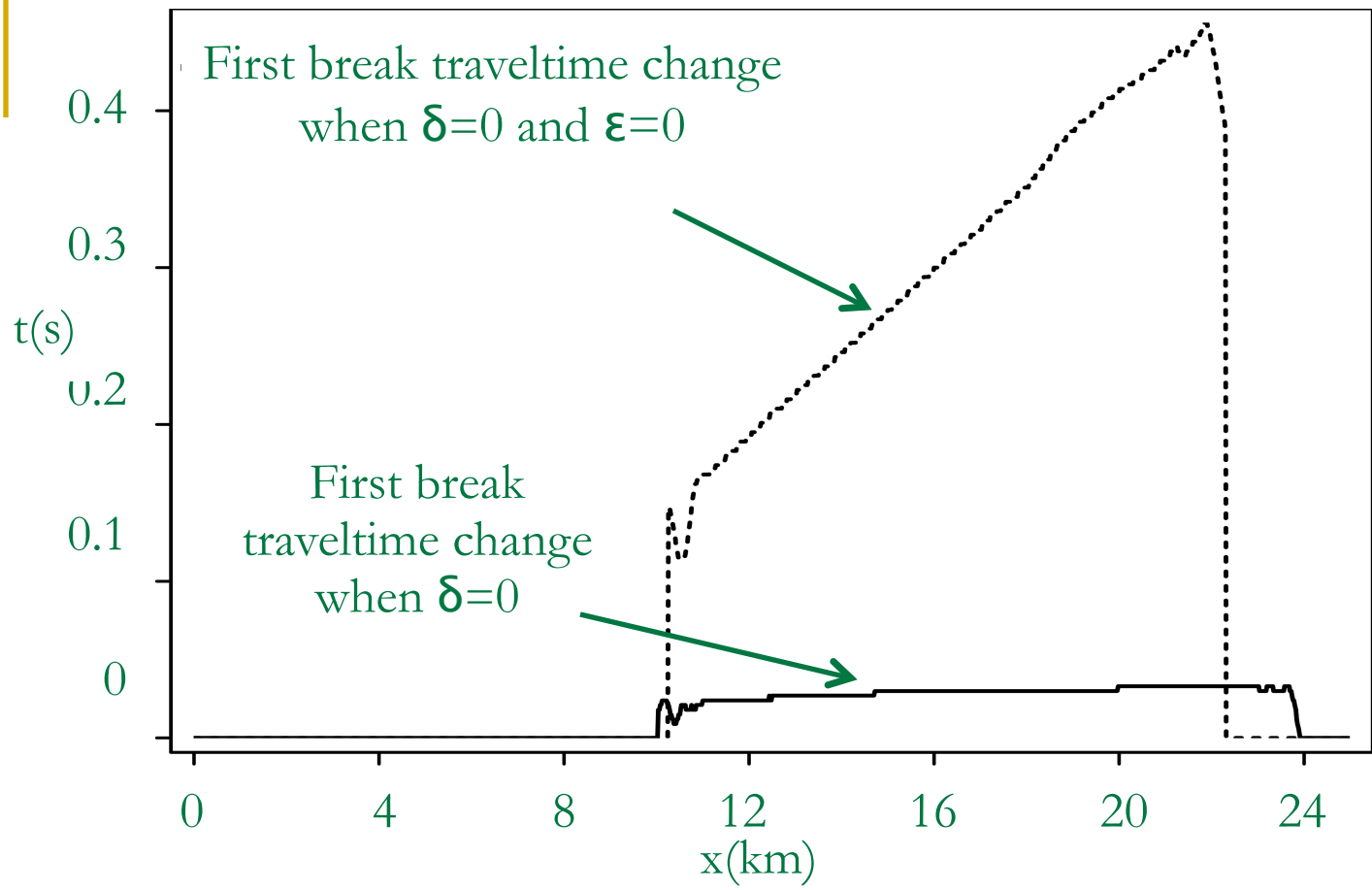


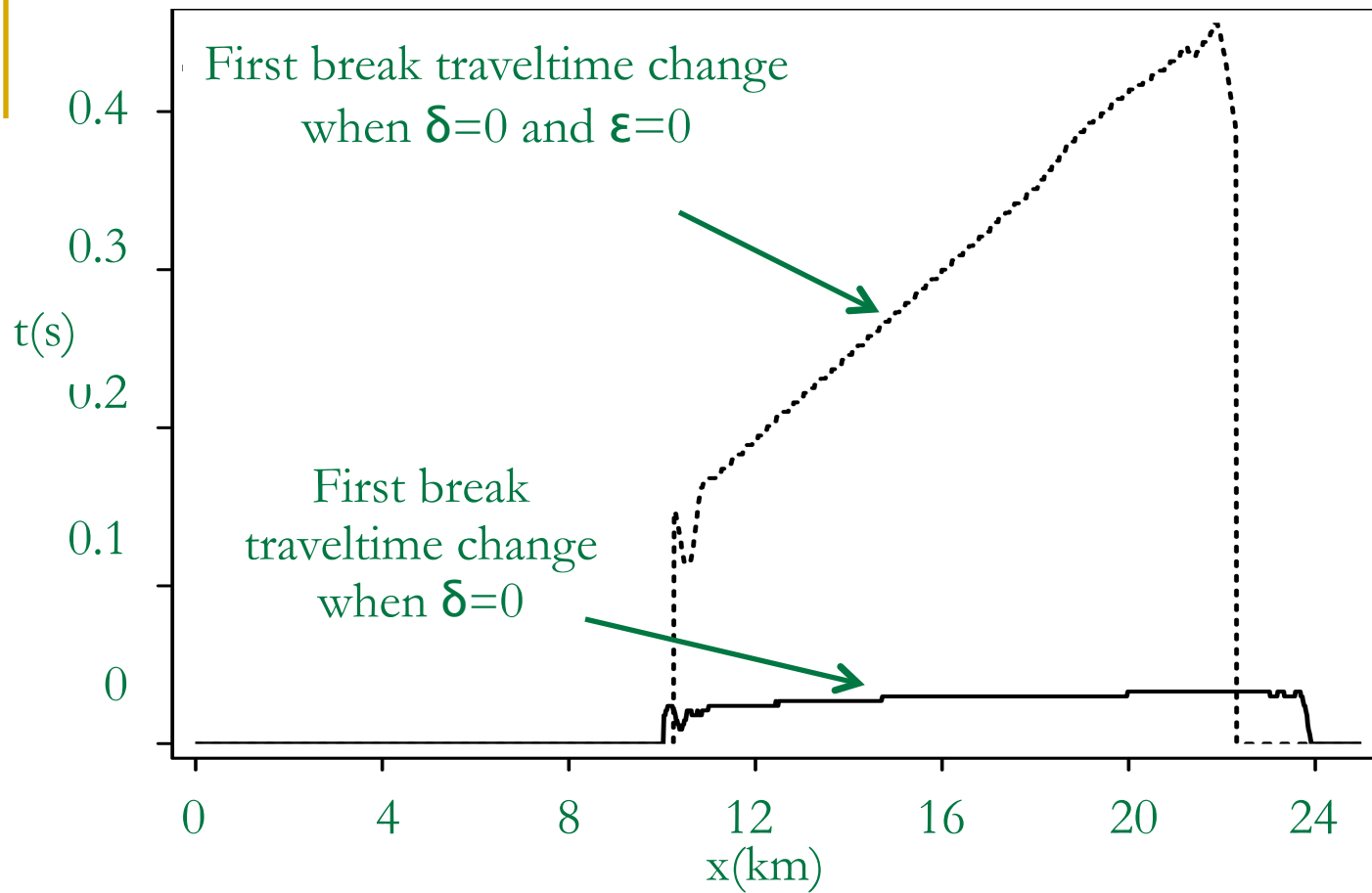
# Anisotropic modeling with $\delta=0$



# Anisotropic modeling with $\delta=0$ and $\epsilon=0$







Early-arrivals are more sensitive to  $\nu$  and  $\epsilon$

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# Inversion strategy

Joint inversion of  $\mathbf{v}$  and  $\boldsymbol{\varepsilon}$ , fixing  $\delta$

# Inversion strategy

Joint inversion of  $\mathbf{v}$  and  $\boldsymbol{\varepsilon}$ , fixing  $\delta$

Acoustic anisotropic wave equation

$$\frac{\partial^2 p}{\partial t^2} = v^2(1 + 2\varepsilon) \frac{\partial^2 p}{\partial x^2} + v^2(1 + 2\delta) \frac{\partial^2 r}{\partial z^2}$$

$$\frac{\partial^2 r}{\partial t^2} = v^2(1 + 2\delta) \frac{\partial^2 p}{\partial x^2} + v^2 \frac{\partial^2 r}{\partial z^2}$$

- $\mathbf{v}$  Vertical near surface velocity
- $\varepsilon$  Anisotropic parameter
- $\delta$  Anisotropic parameter
- $p$  Horizontal pressure wavefield
- $r$  Vertical pressure wavefield

# Parameterization choices

**Straightforward**

$$m_1 = v^{-2}$$

$$m_2 = 1 + 2\varepsilon$$

**Velocity**

$$m_1 = v^2$$

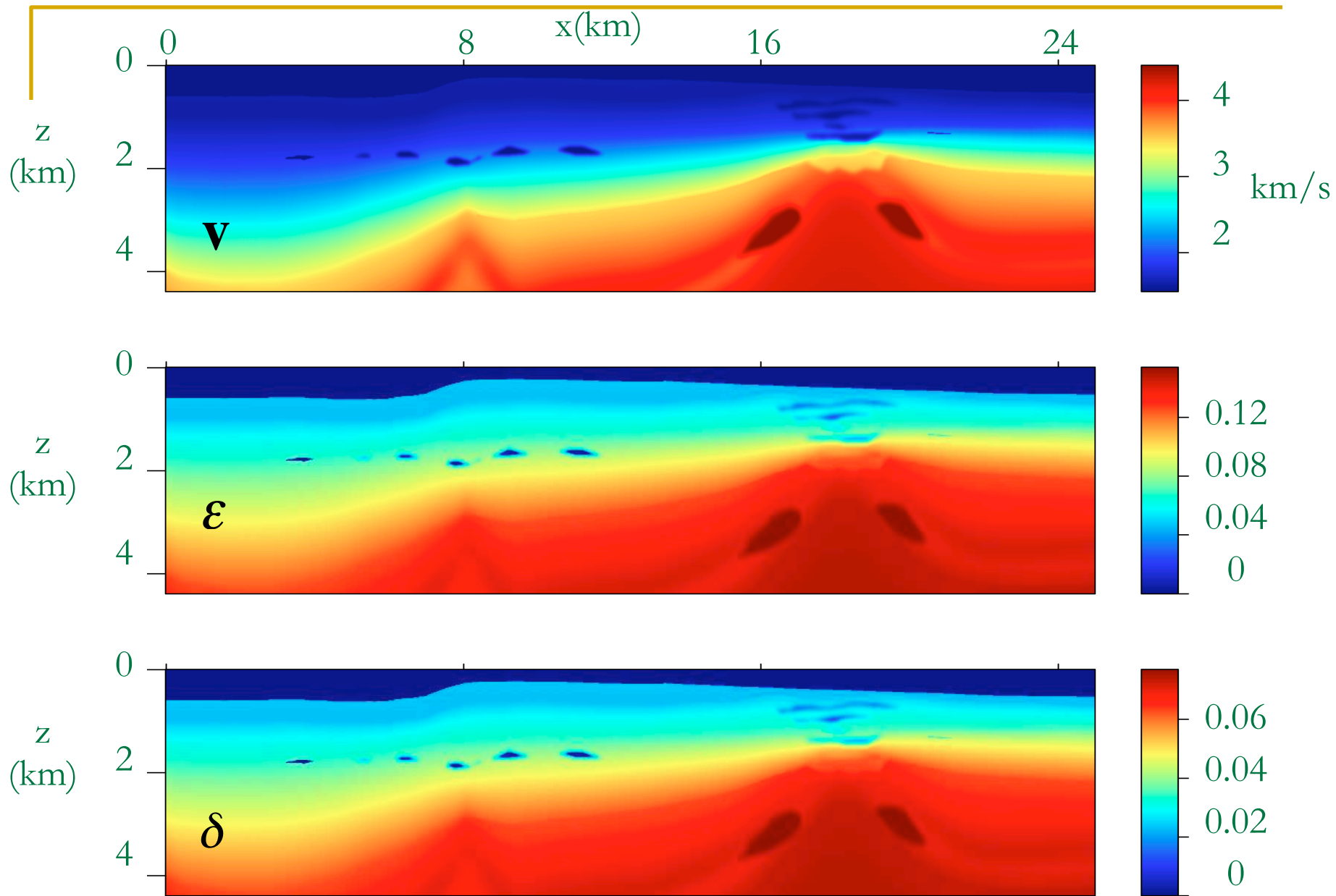
$$m_2 = v_h^2 = v^2(1 + 2\varepsilon)$$

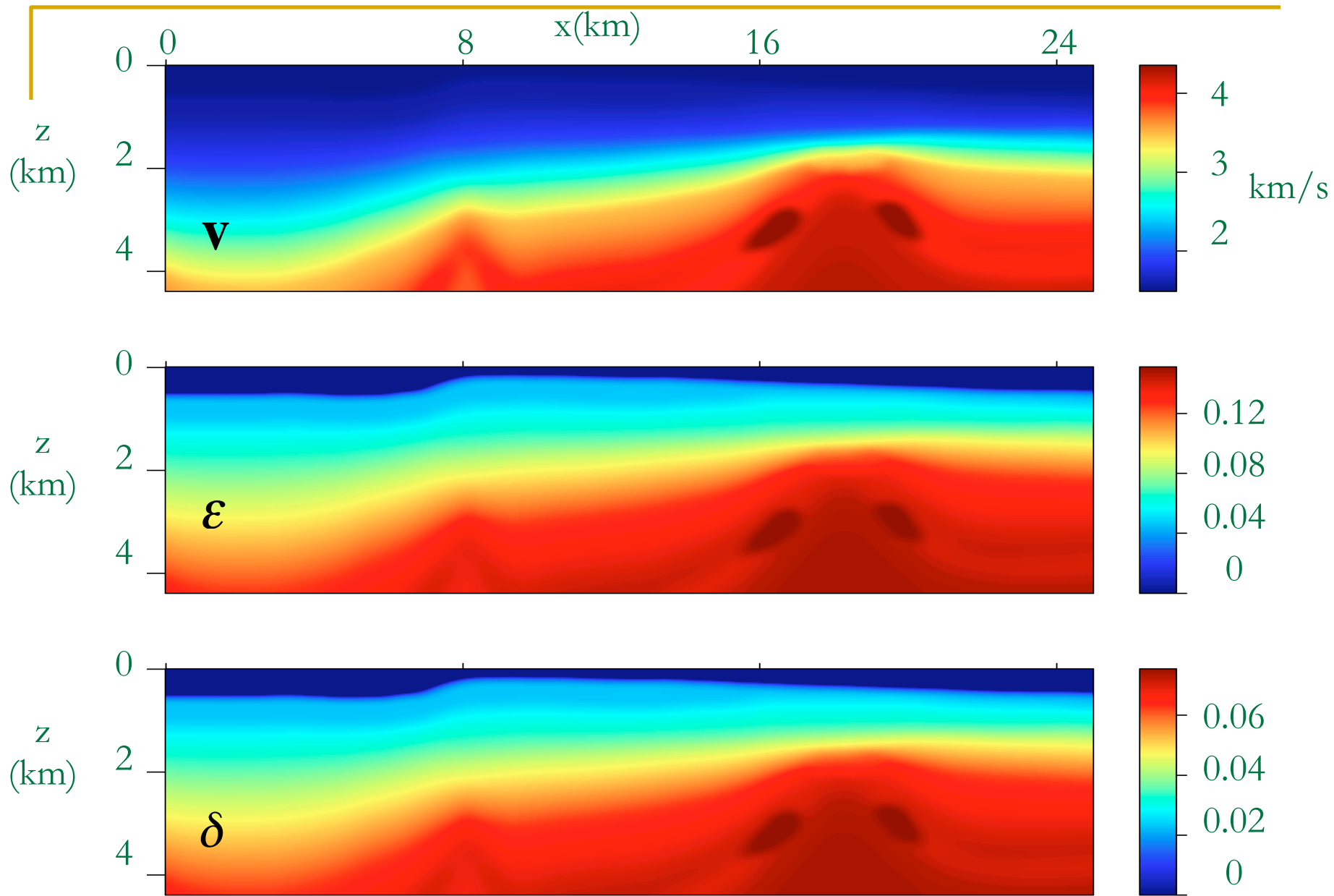
**Logarithm slowness**

$$m_1 = \log(v^{-2})$$

$$m_2 = 1 + 2\varepsilon$$







# Relative sensitivity kernel evaluation

$$k_{m_i} = \Delta m_i / m_i$$

$\Delta m_i$  Gradient of model component  $i$

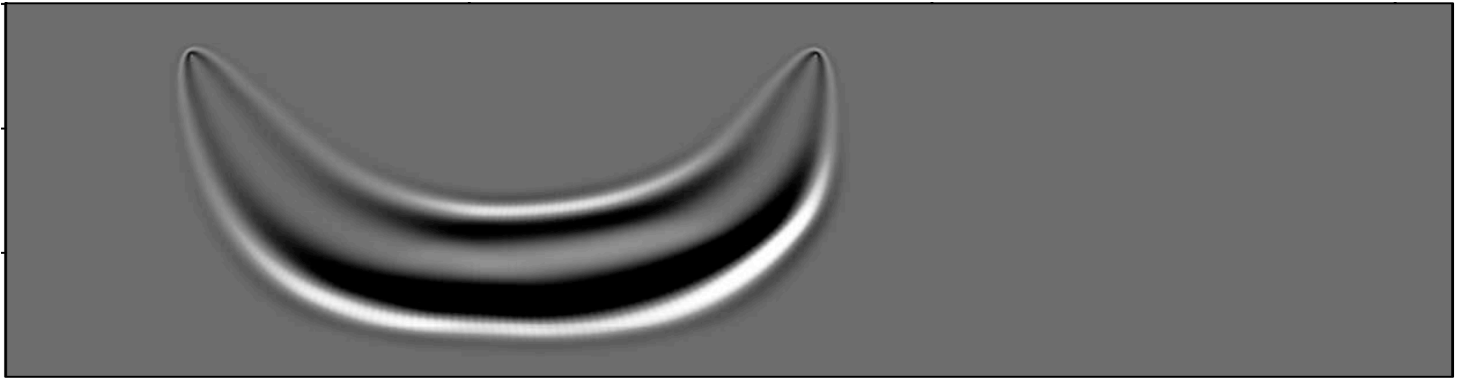
# Straightforward parameterization

$$m_1 = v^{-2}$$

$$k_{m_1} \quad x$$

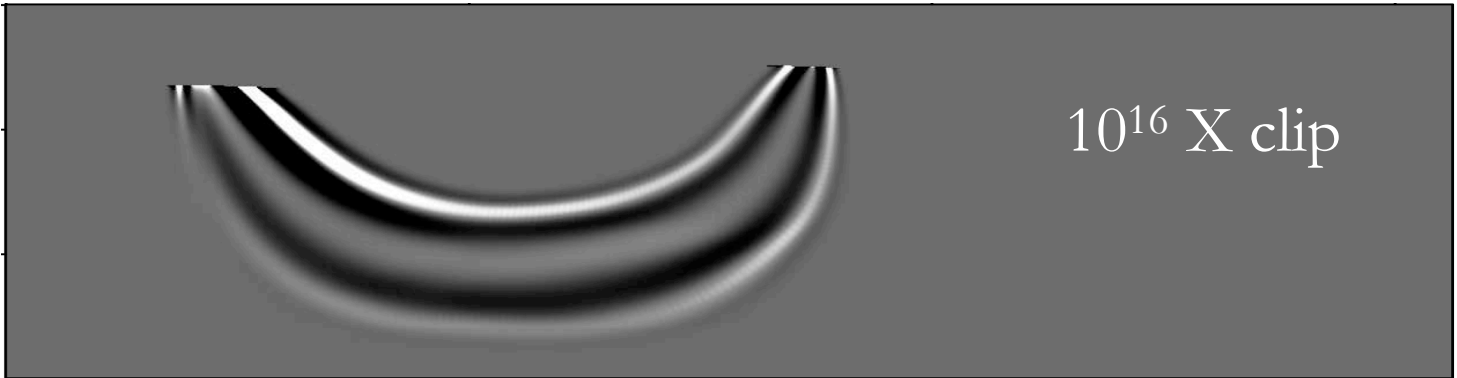
$$m_2 = 1 + 2\varepsilon$$

z



$$k_{m_2}$$

z



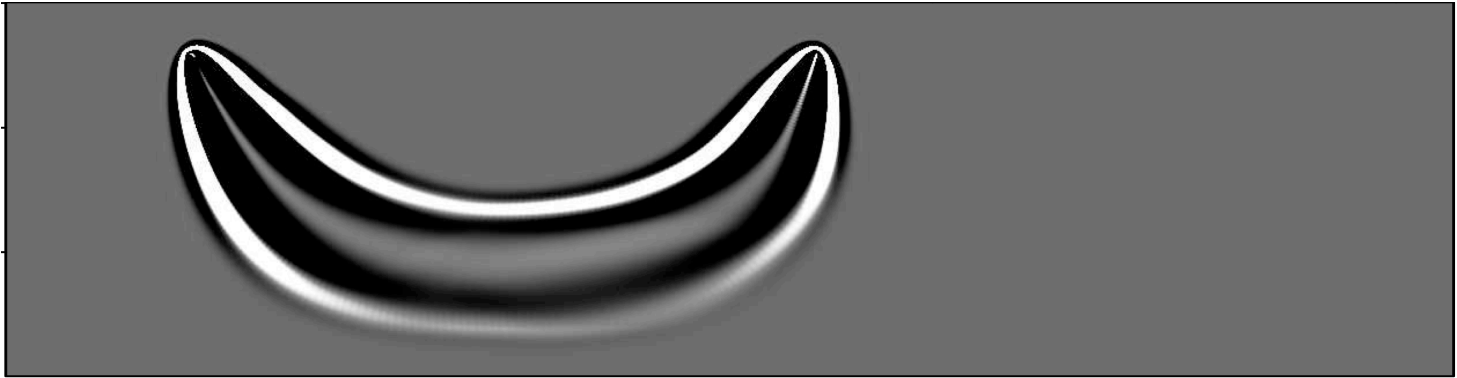
# Velocity parameterization

$$m_1 = v^2$$

$k_{m_1}$  x

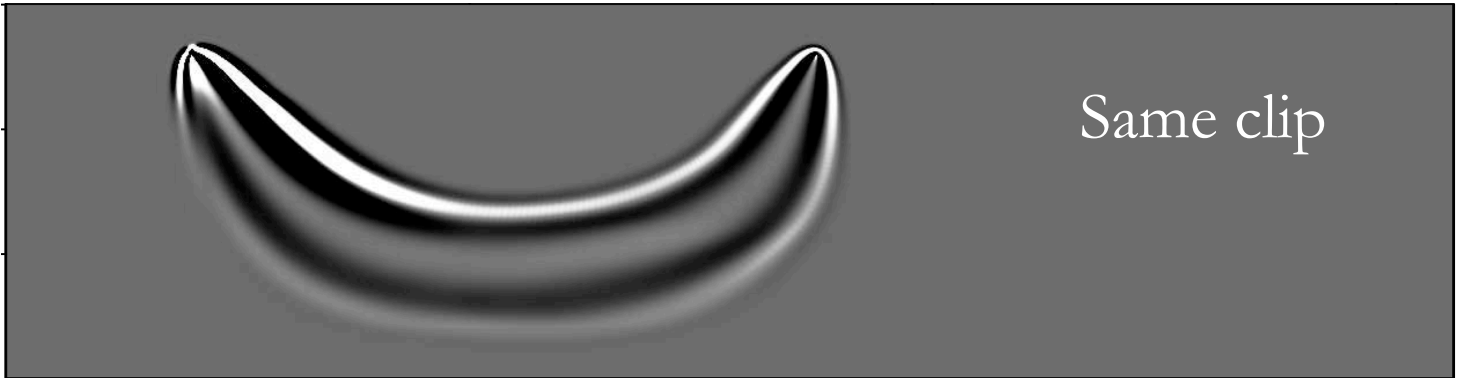
$$m_2 = v_h^2 = v^2(1 + 2\varepsilon)$$

z



$k_{m_2}$

z



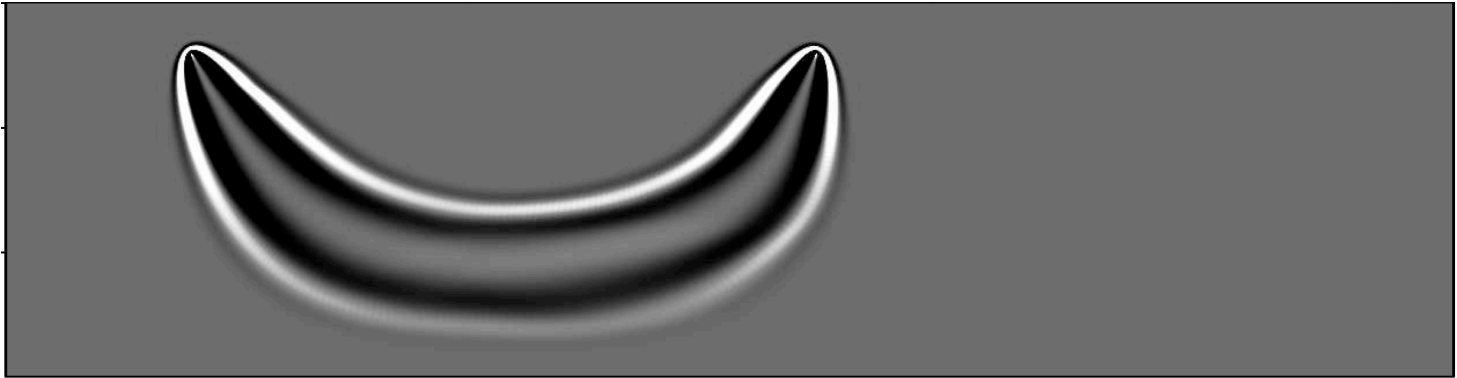
# Logarithm slowness parameterization

$$m_1 = \log(v^{-2})$$

$$m_2 = 1 + 2\varepsilon$$

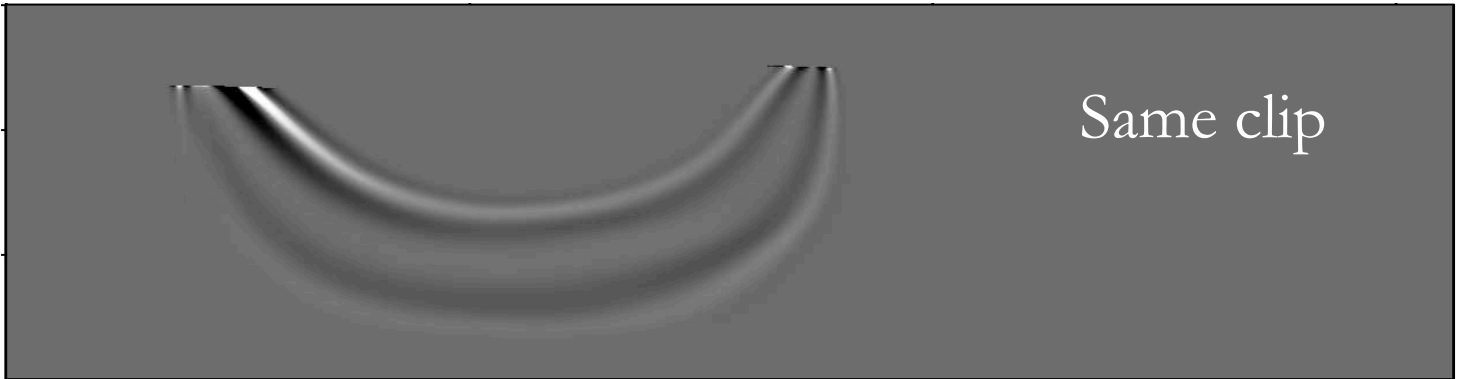
$k_{m_1}$  x

z



$k_{m_2}$

z

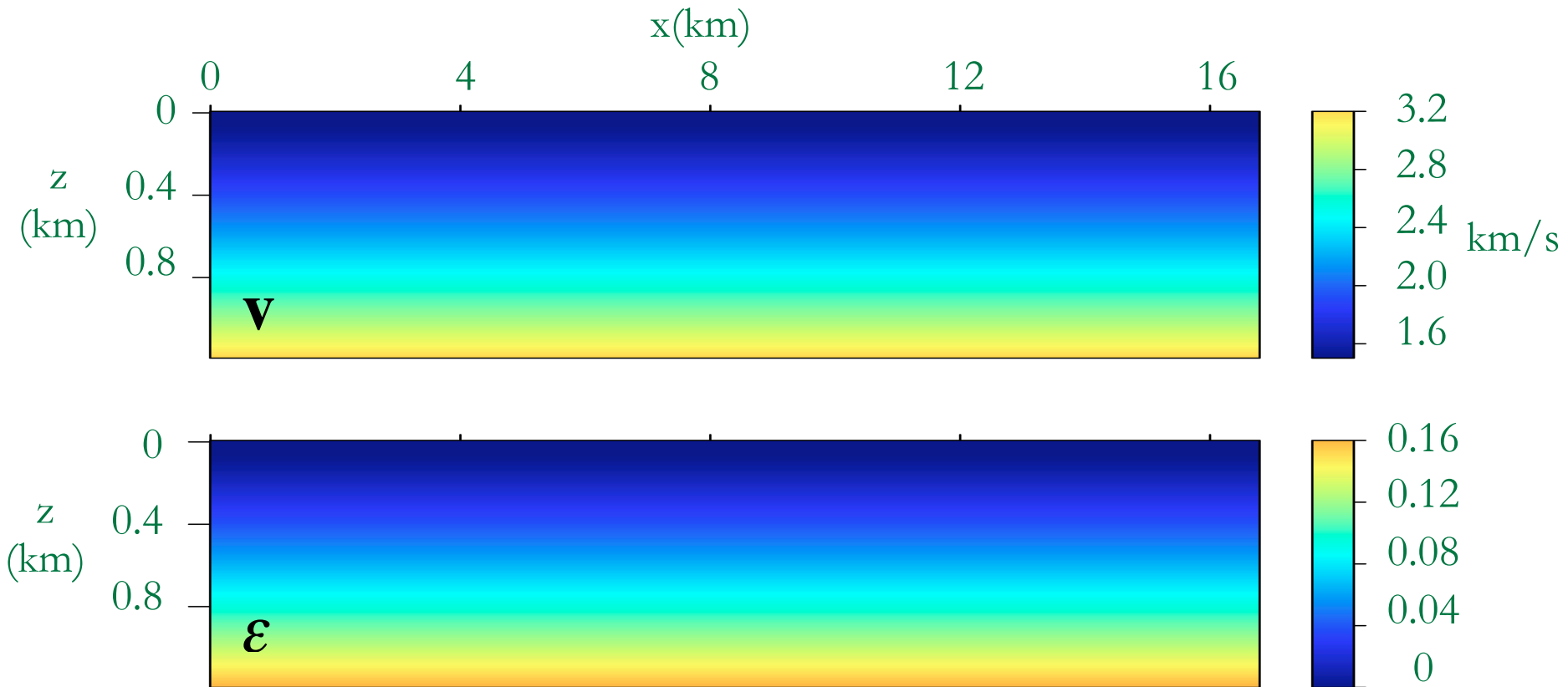


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# Background model





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# Acquisition geometry

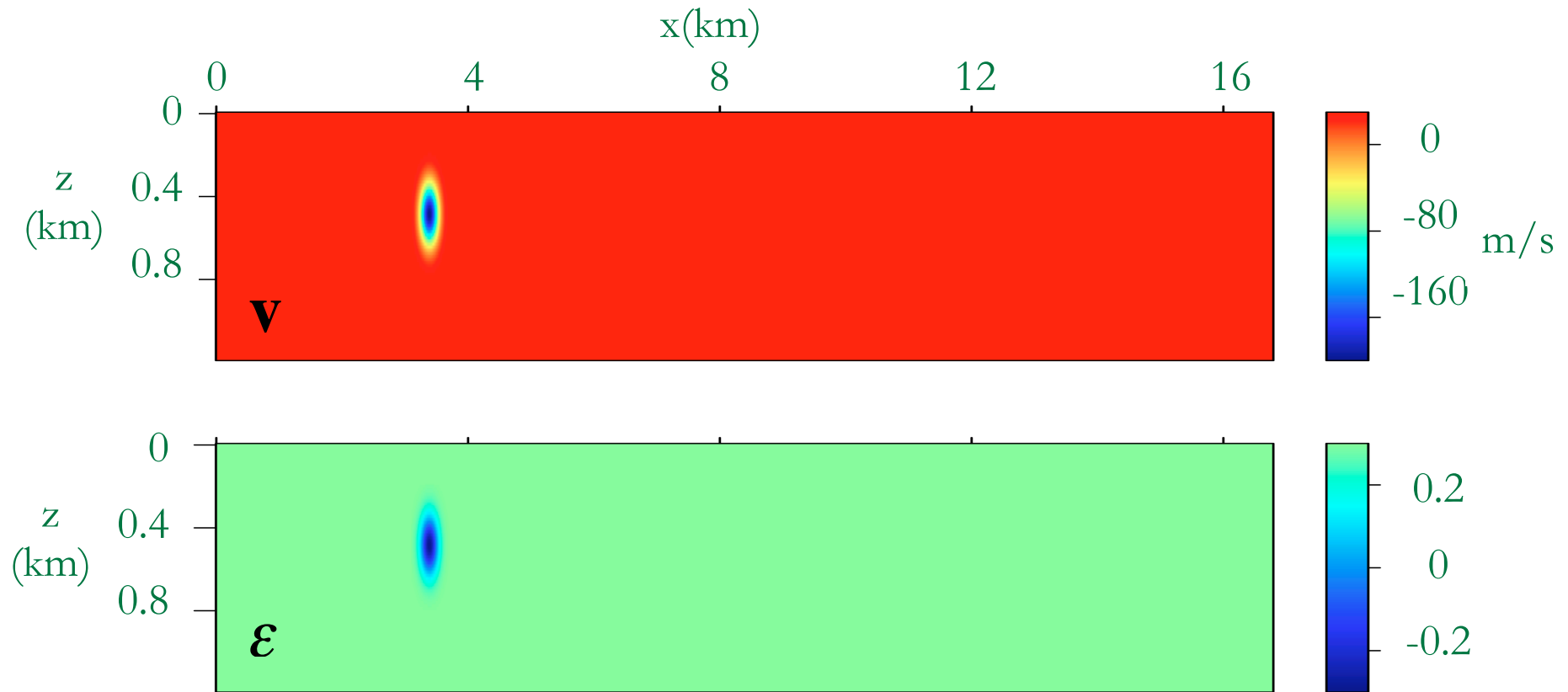
1120 \*80 grid points, 15 m spacing

64 shots, 225 meter spacing

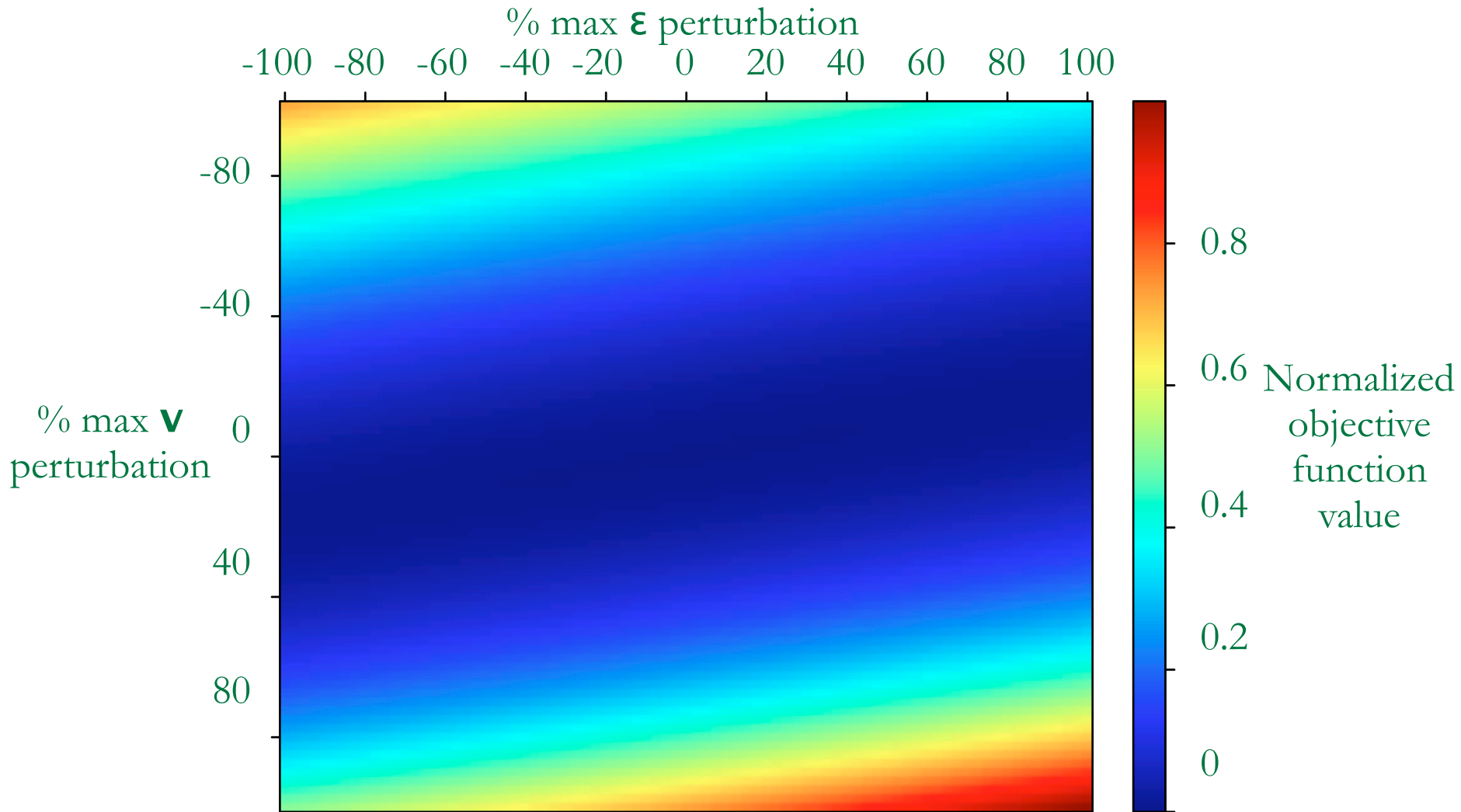
7Hz peak frequency source

Receivers everywhere on the surface

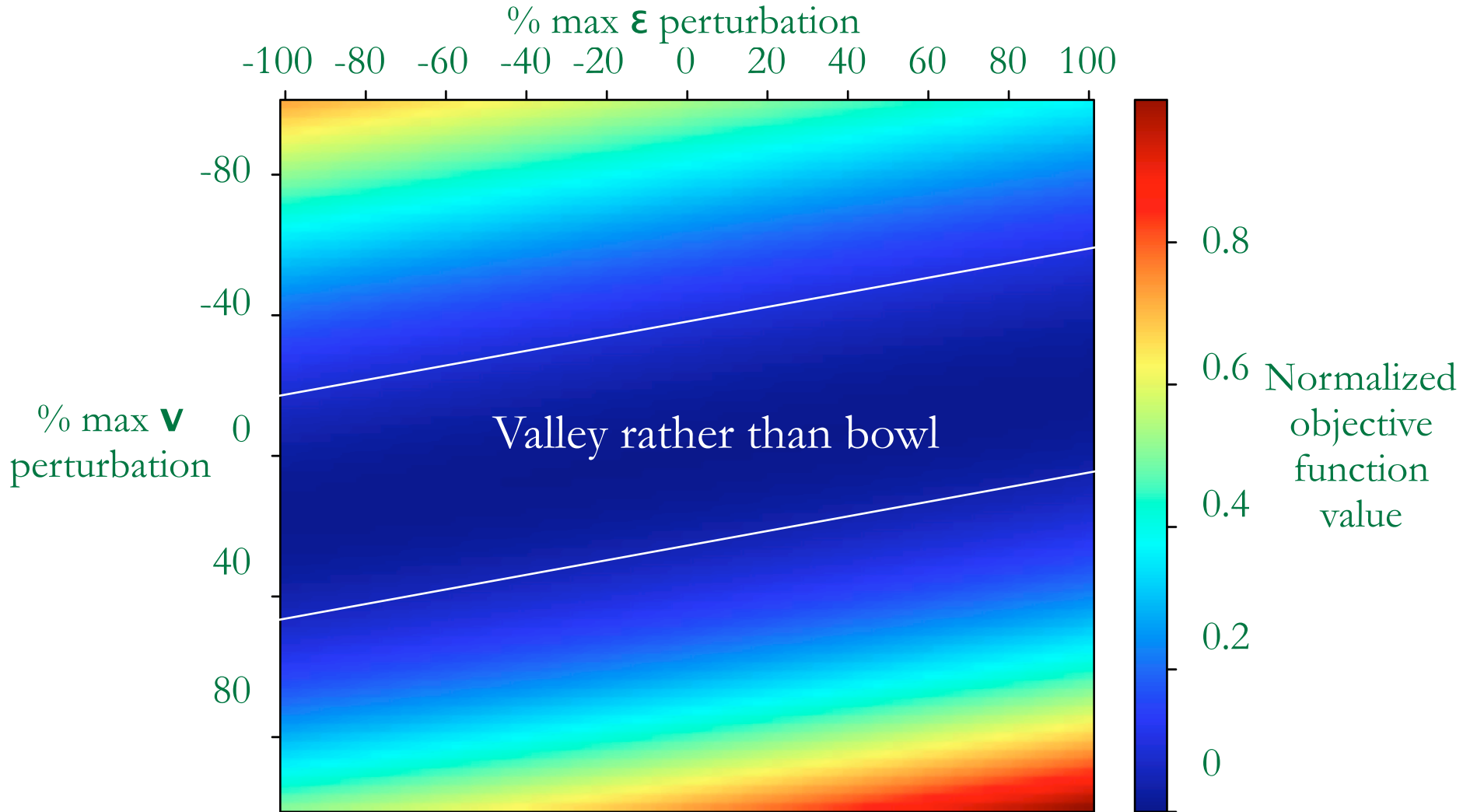
# Maximum perturbation



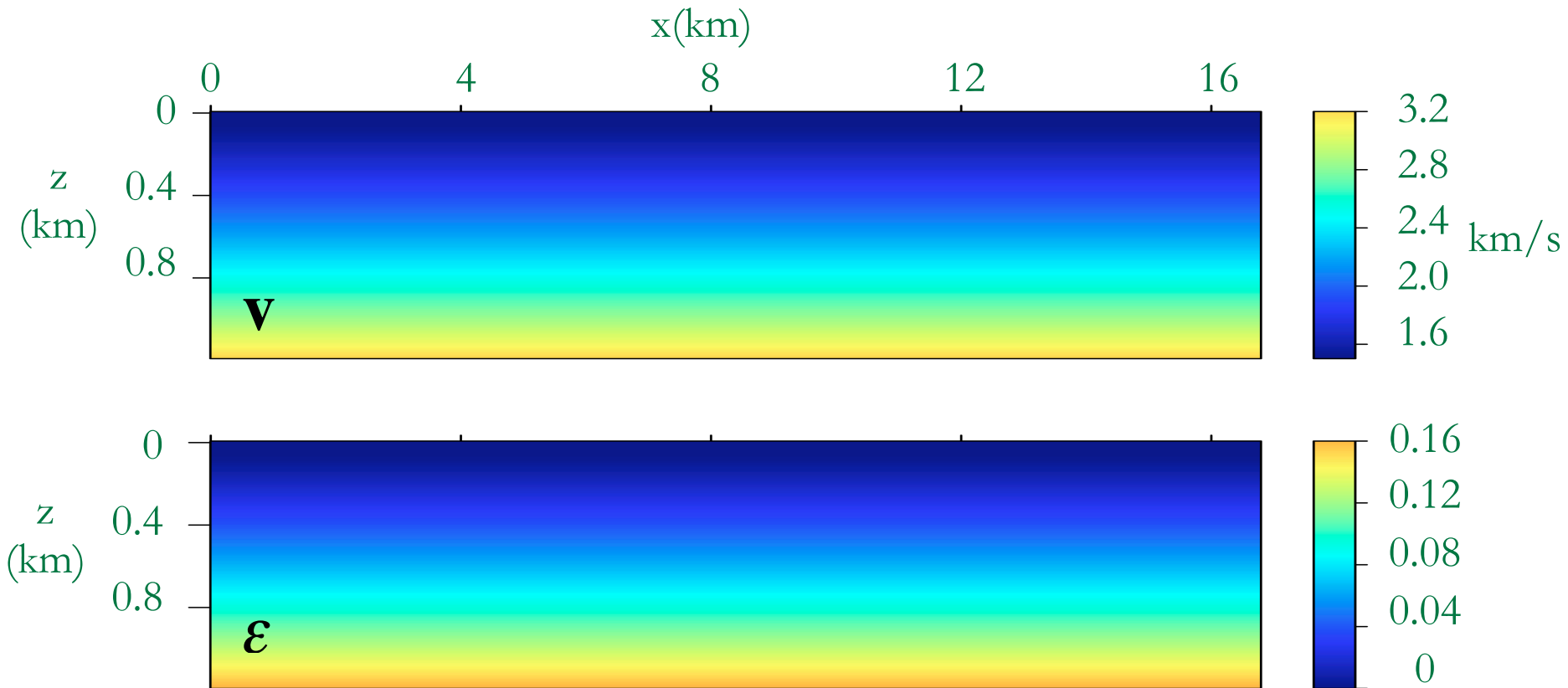
# Objective function evaluation



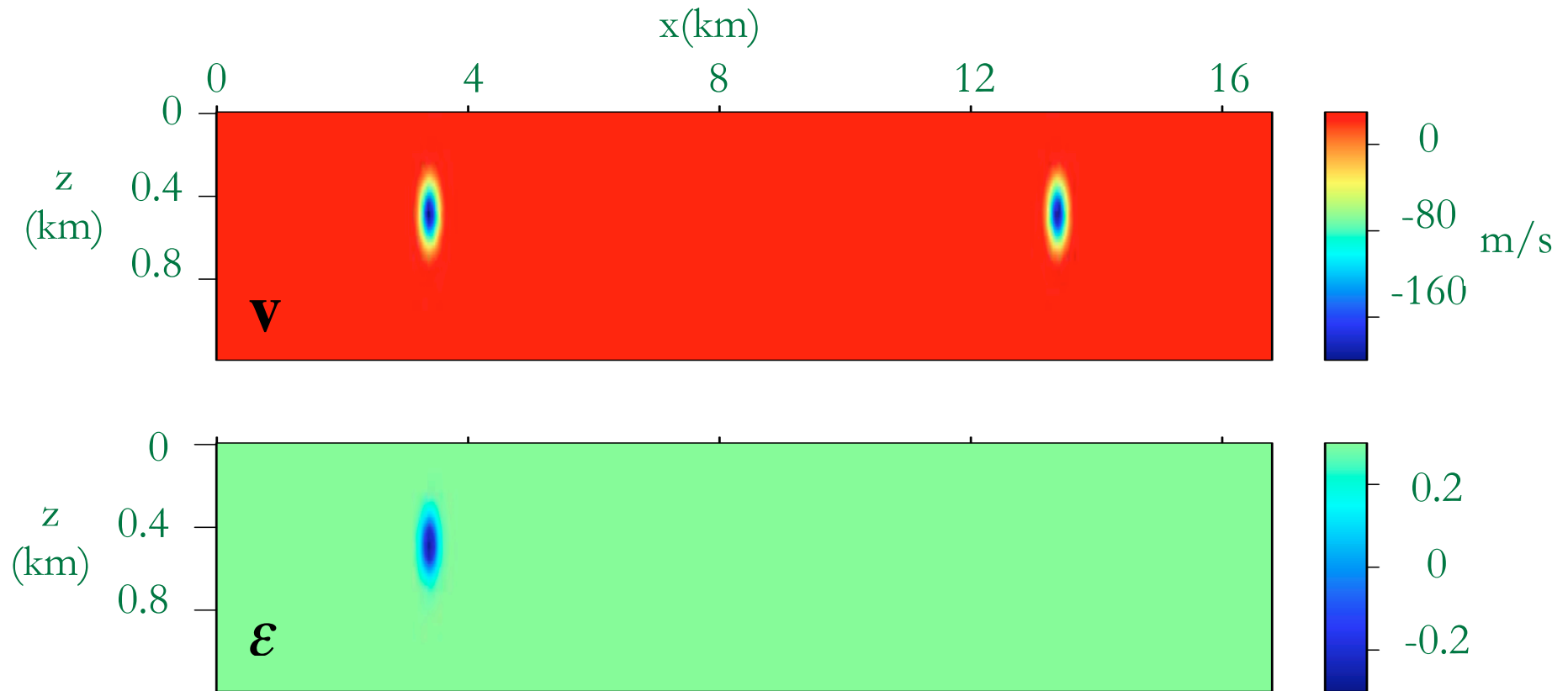
# Ambiguity between $\mathbf{v}$ and $\boldsymbol{\varepsilon}$



# Background model & Starting model for inversion



# True perturbation



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# Acquisition geometry

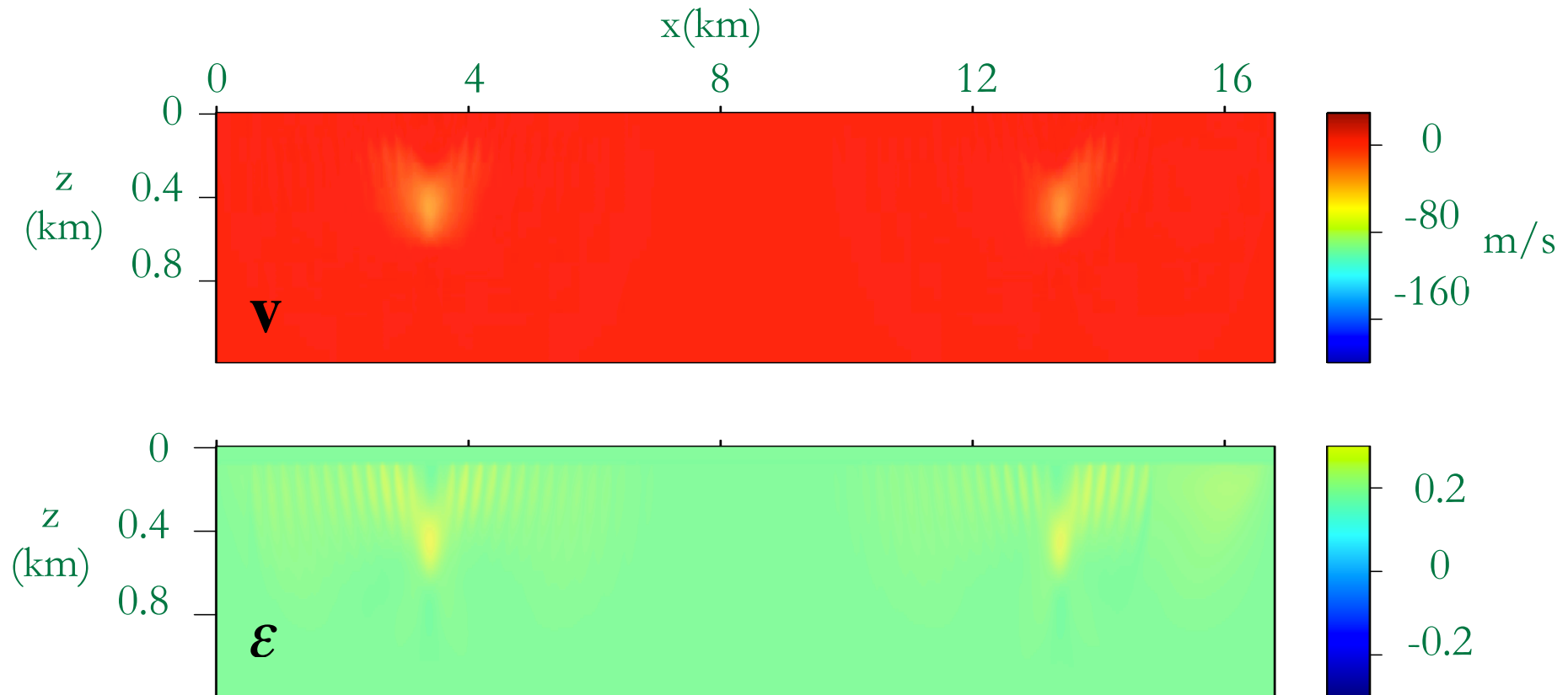
1120 \*80 grid points, 15 m spacing

64 shots, 225 meter spacing

7Hz peak frequency source

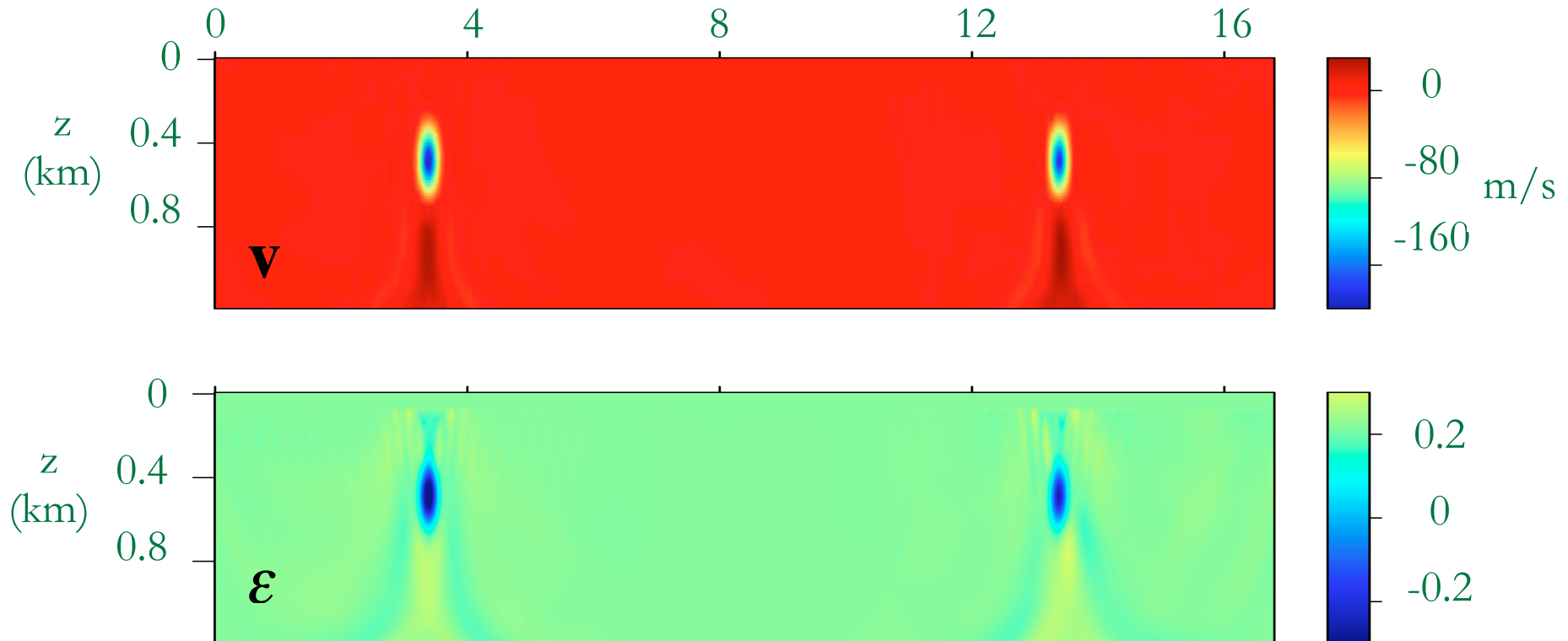
Receivers everywhere on the surface

# Estimated perturbation, velocity parametrization

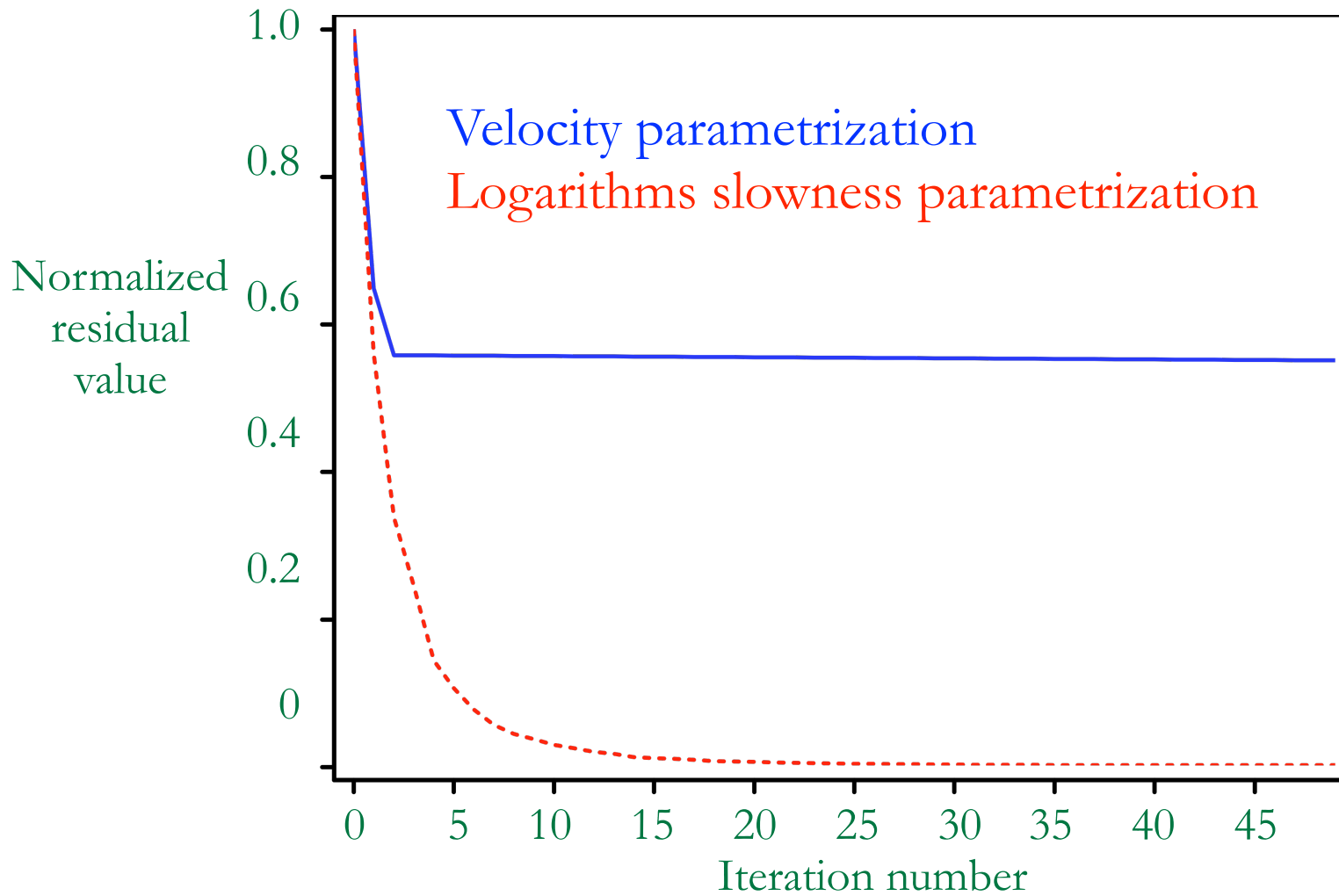




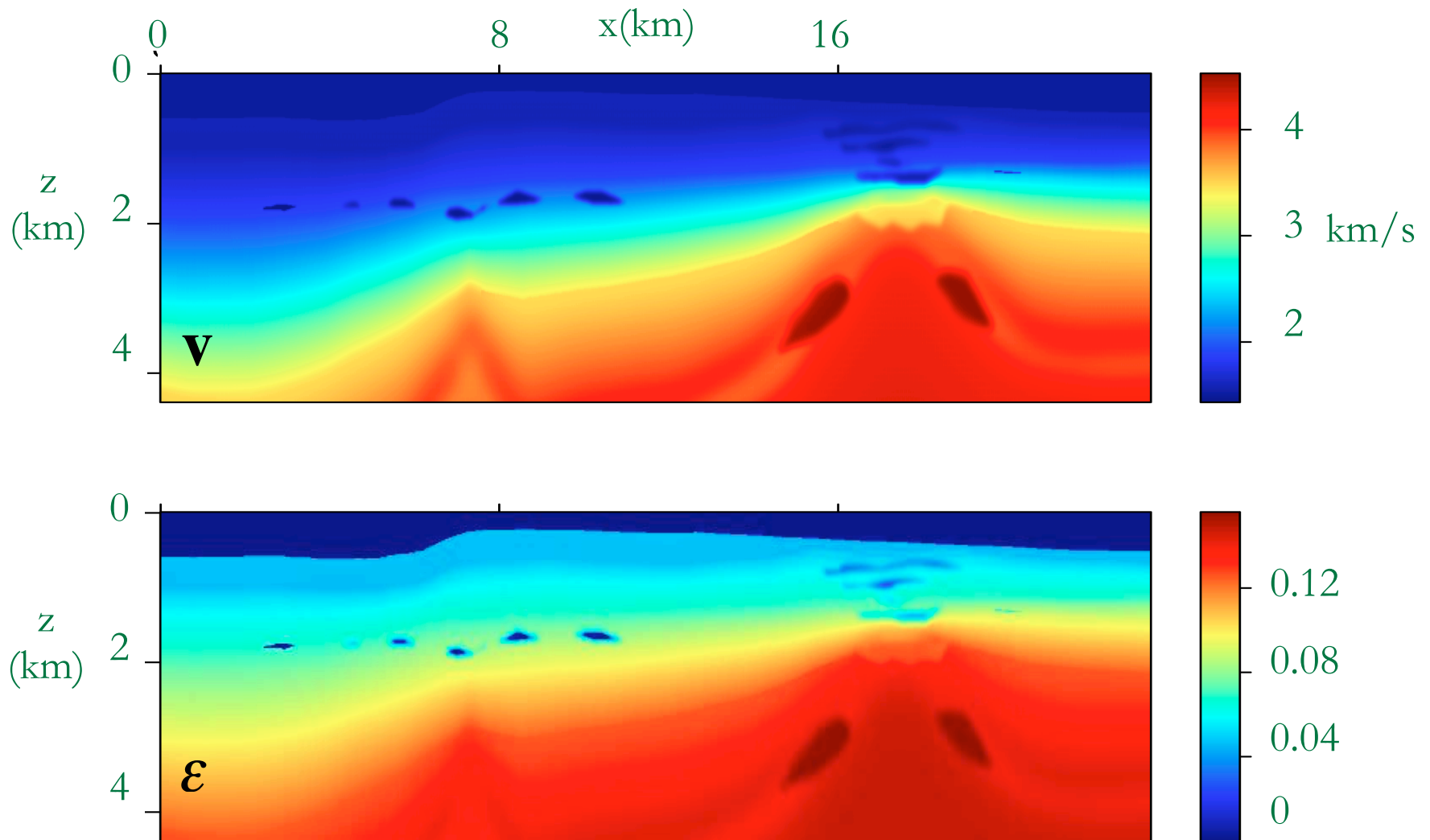
# Estimated perturbation, logarithm slowness parametrization



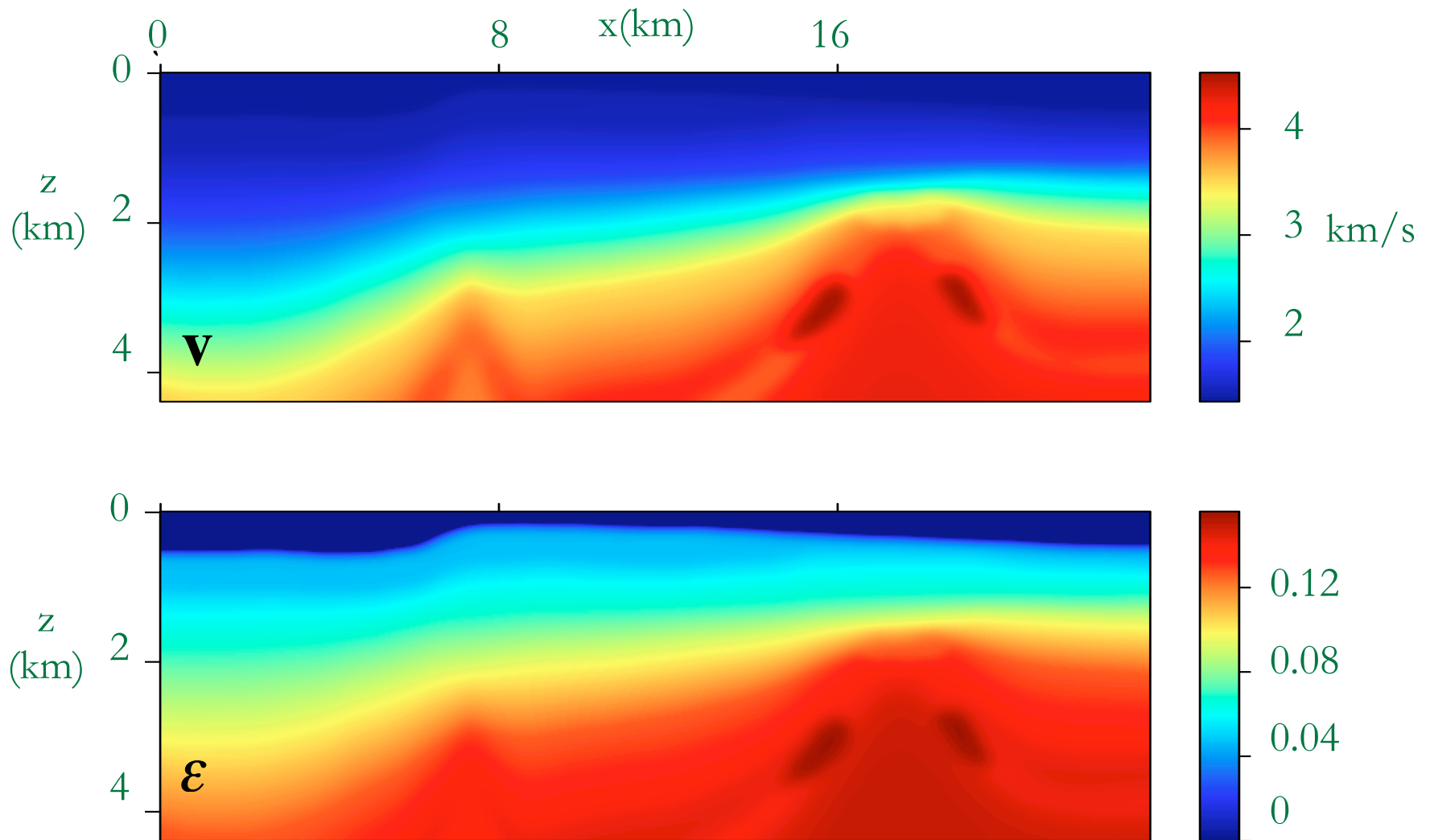
# Residual comparison



# True model



# Initial model



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# Acquisition geometry

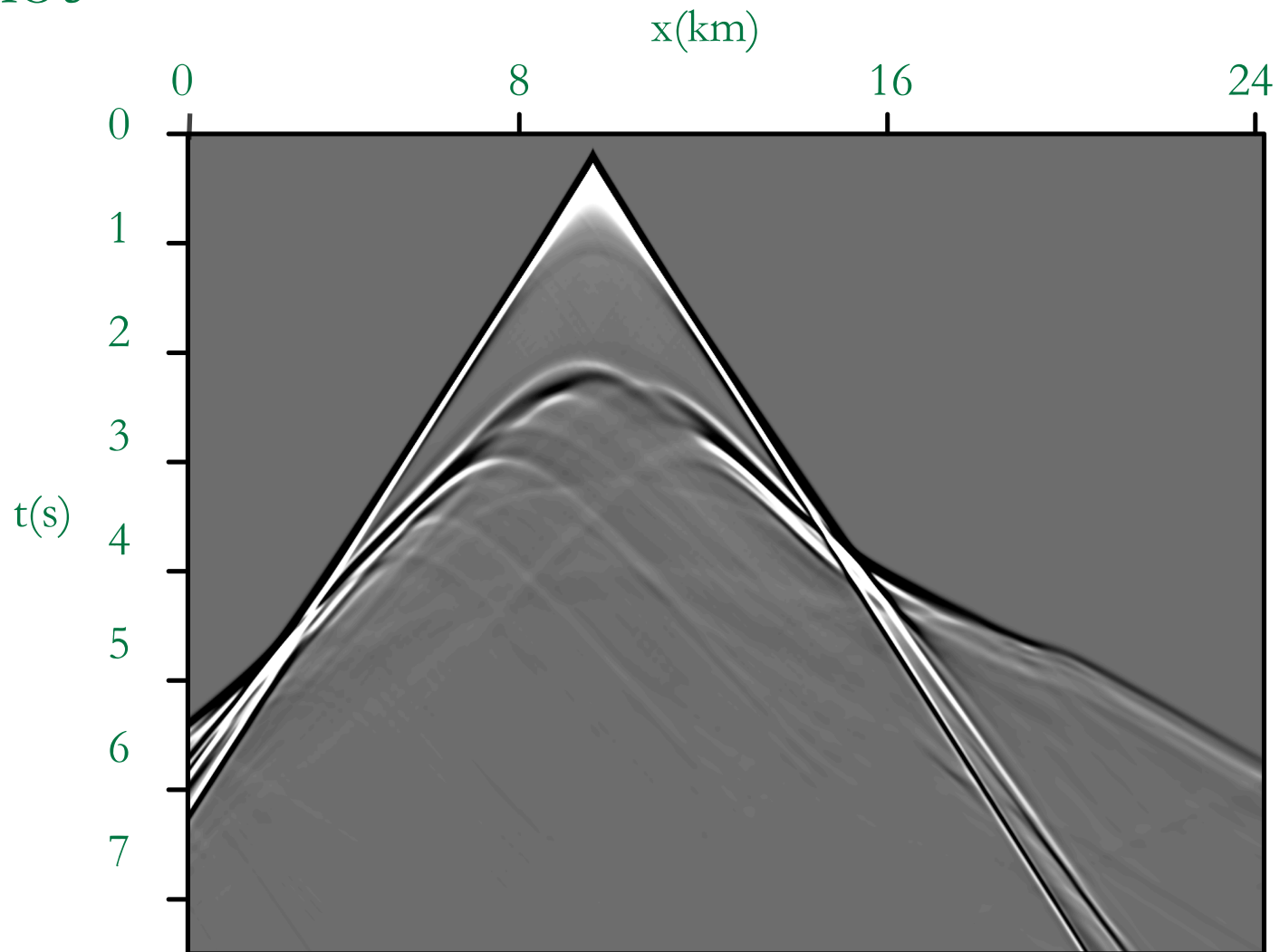
1170 \*220 grid points, 20 m spacing

64 shots, 320 meter spacing

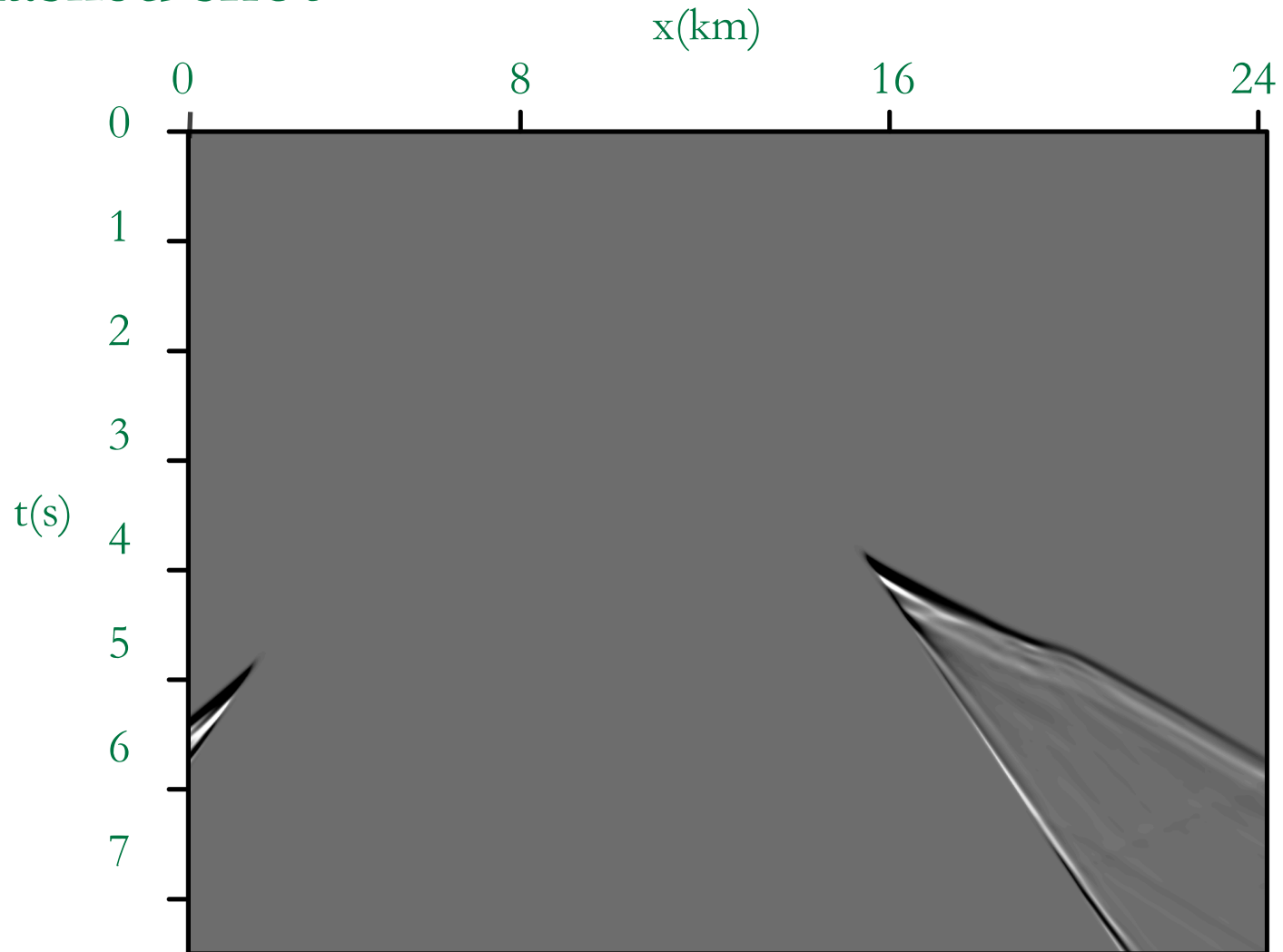
7Hz peak frequency source

Receivers everywhere on the surface

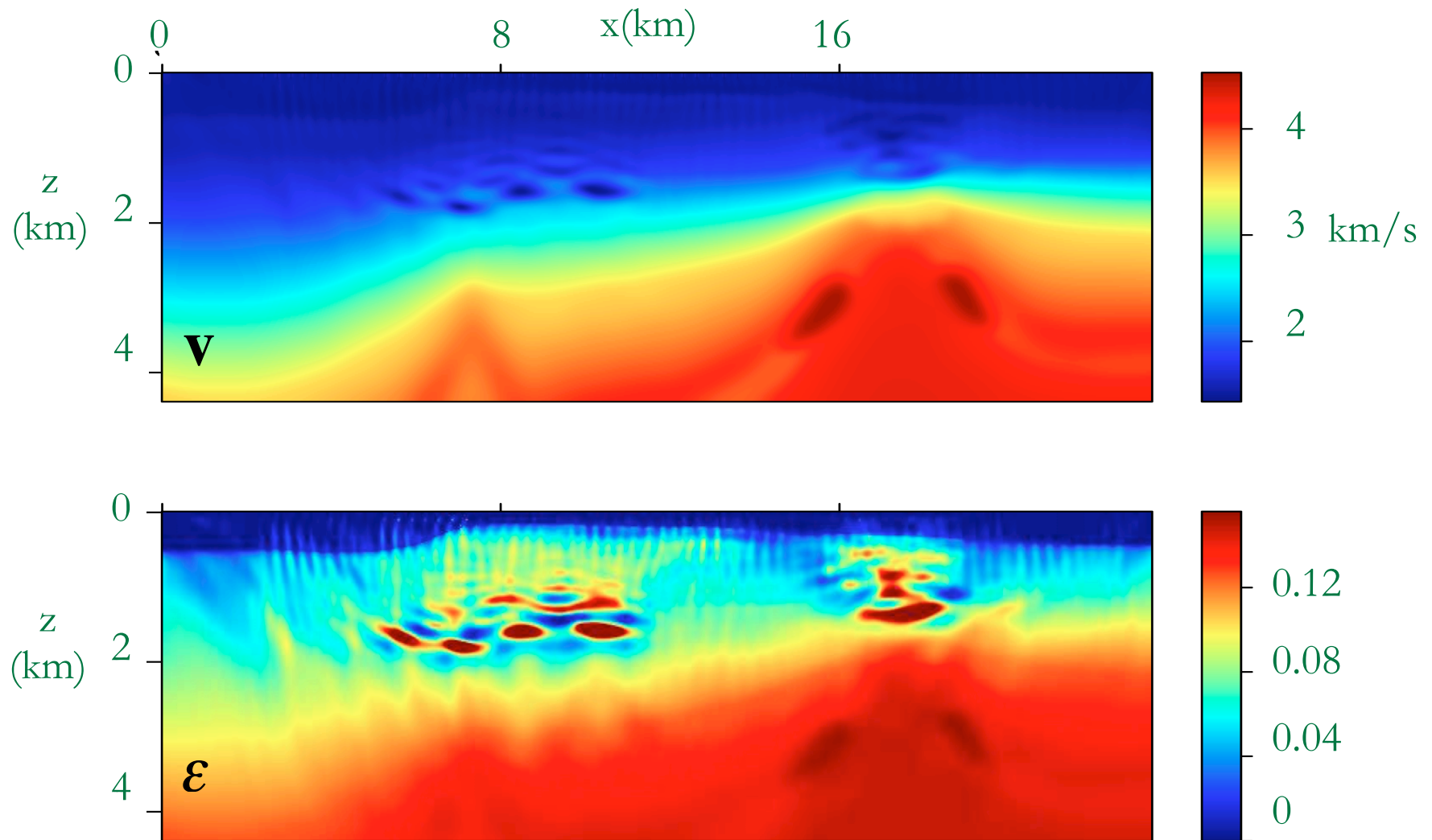
# Shot



# Masked shot

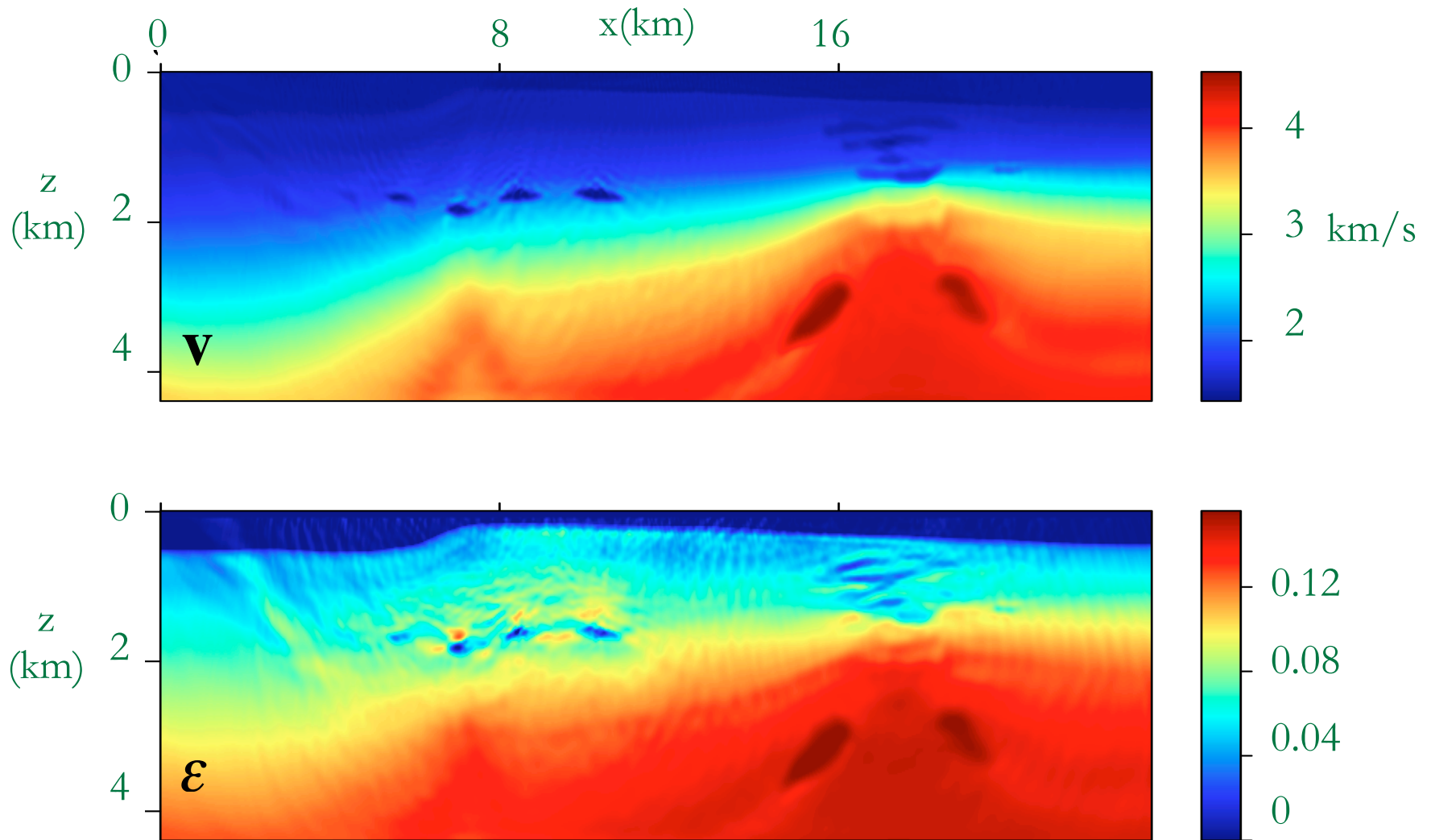


# Estimated model, velocity parametrization

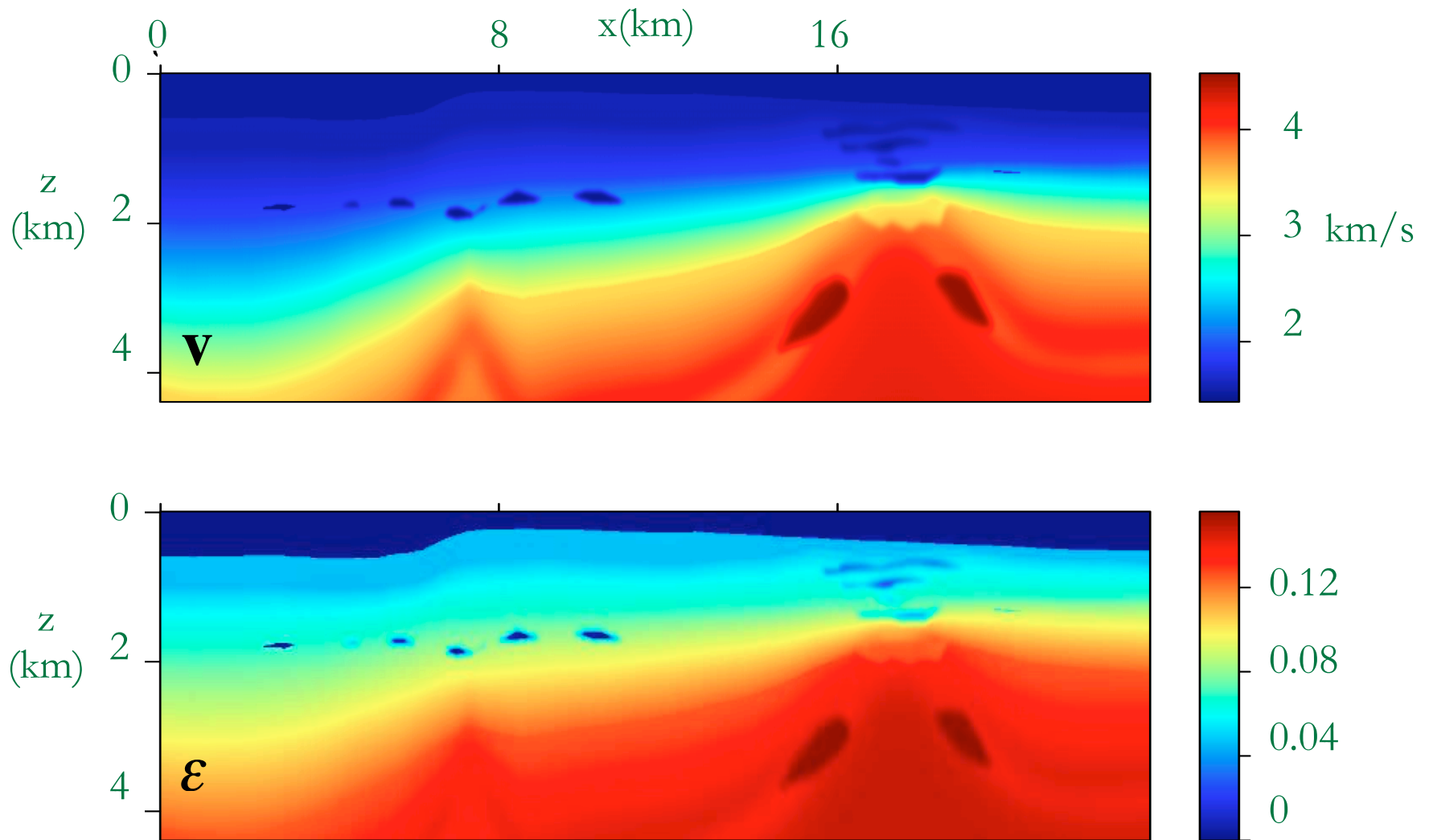




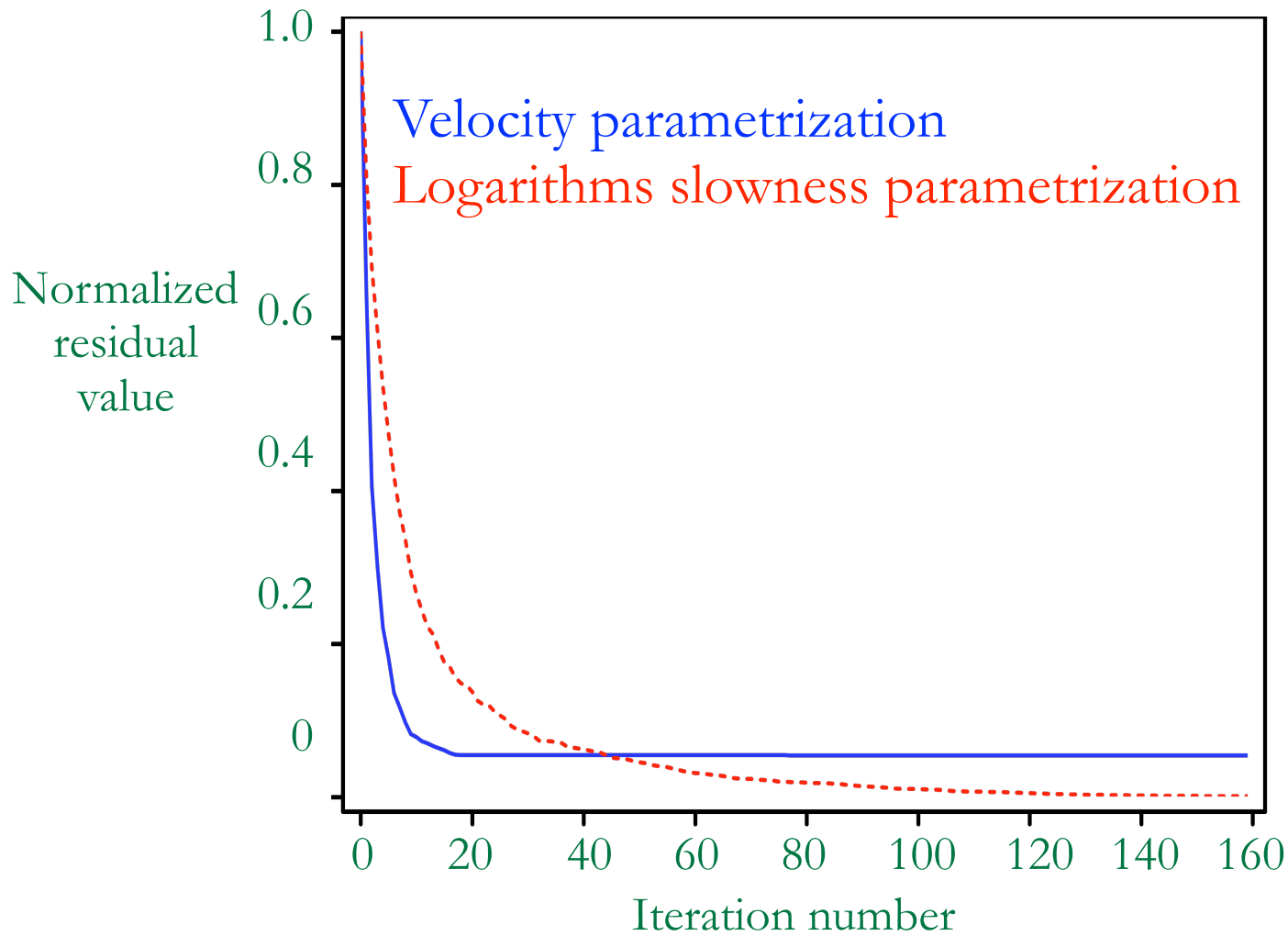
# Estimated model, logarithm slowness parametrization



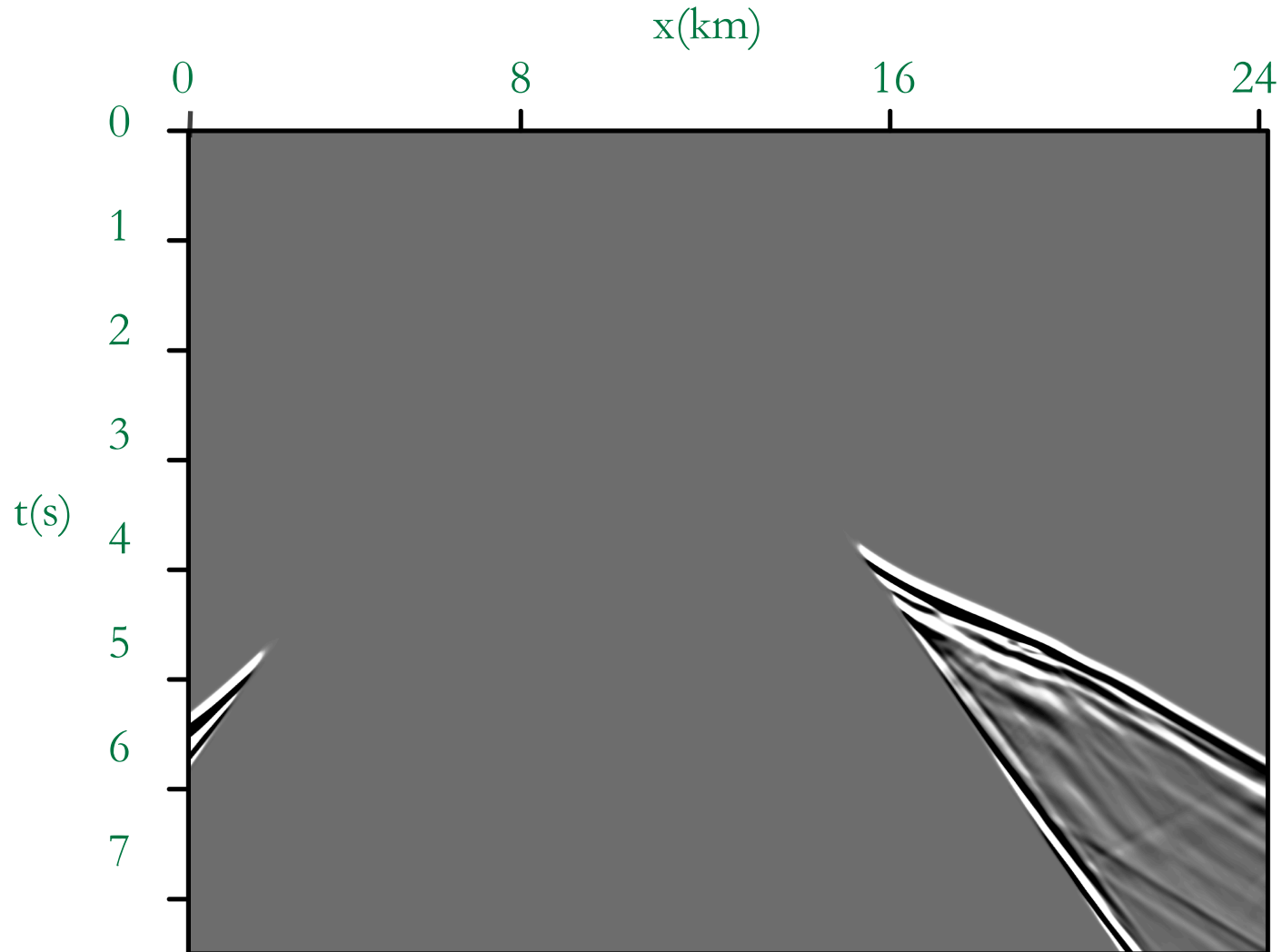
# True model



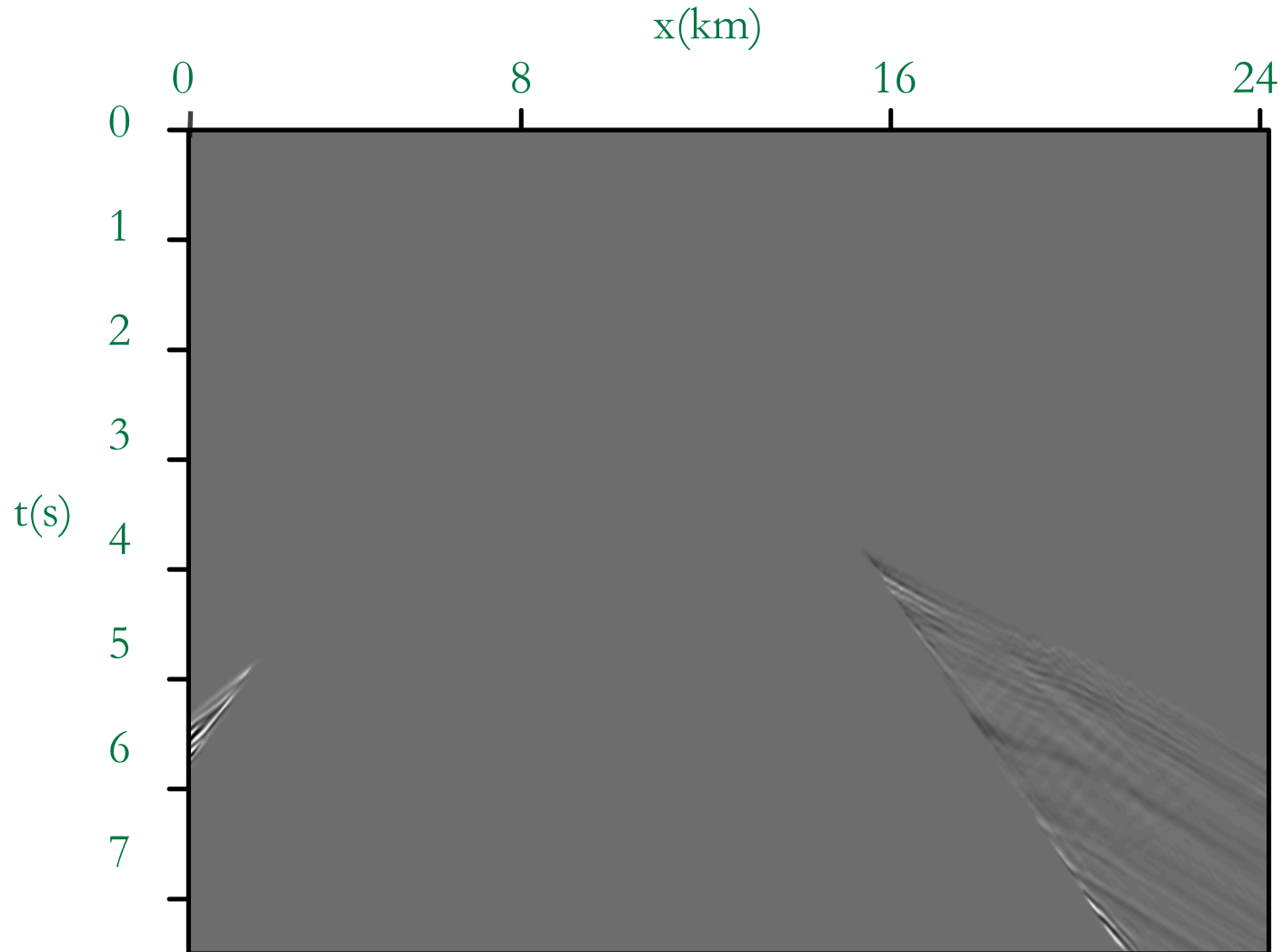
# Residual comparison



# Initial residual, logarithm slowness parametrization



# Final residual, logarithm slowness parametrization



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# Conclusions

- Including anisotropic parameter estimation as part of early-arrival waveform inversion is necessary for anisotropic data.

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- Logarithm parametrization works better than velocity parametrization.



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# Conclusions

- Including anisotropic parameter estimation as part of early-arrival waveform inversion is necessary for anisotropic data.
- Logarithm parametrization works better than velocity parametrization.
- Data ambiguity exist between velocity and anisotropy parameter. Solution needs to be investigated.

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# Acknowledgements

- SEP sponsors for the financial support of this research
- Elita for discussion about anisotropic parameter inversion
- SEP colleagues for suggestions about the synthetic examples

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Thank you