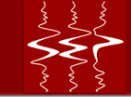


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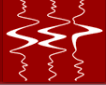
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Preconditioned elastic full waveform inversion using approximated Hessian matrix

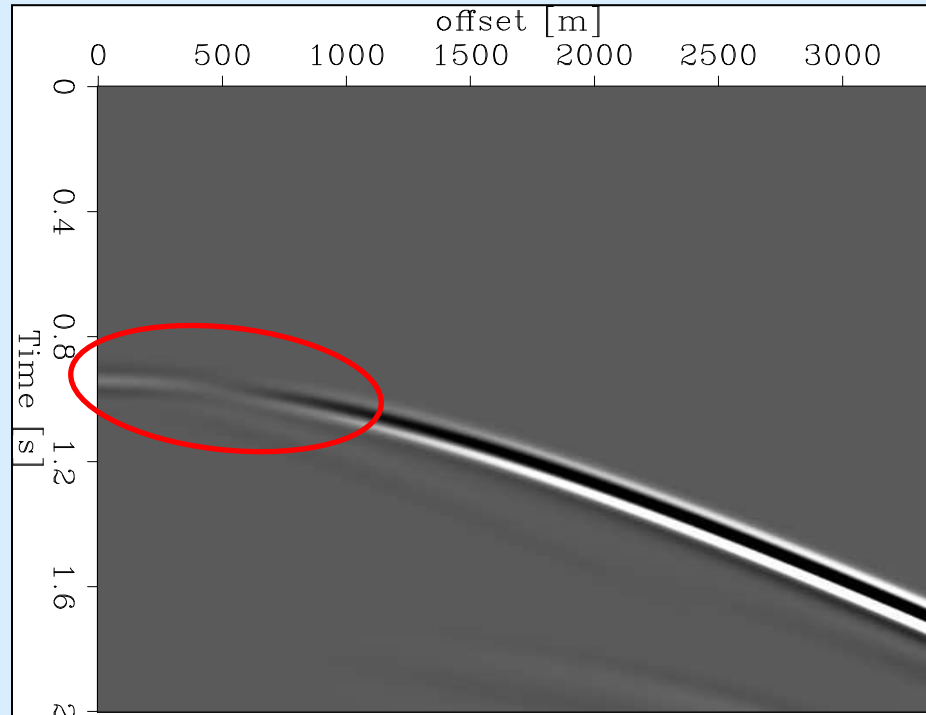


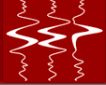
- **Why we need elastic FWI**
- **The parameter cross-talk**
- **Preconditioned elastic FWI**
- **Conclusions**



How do we invert for elastic parameters?

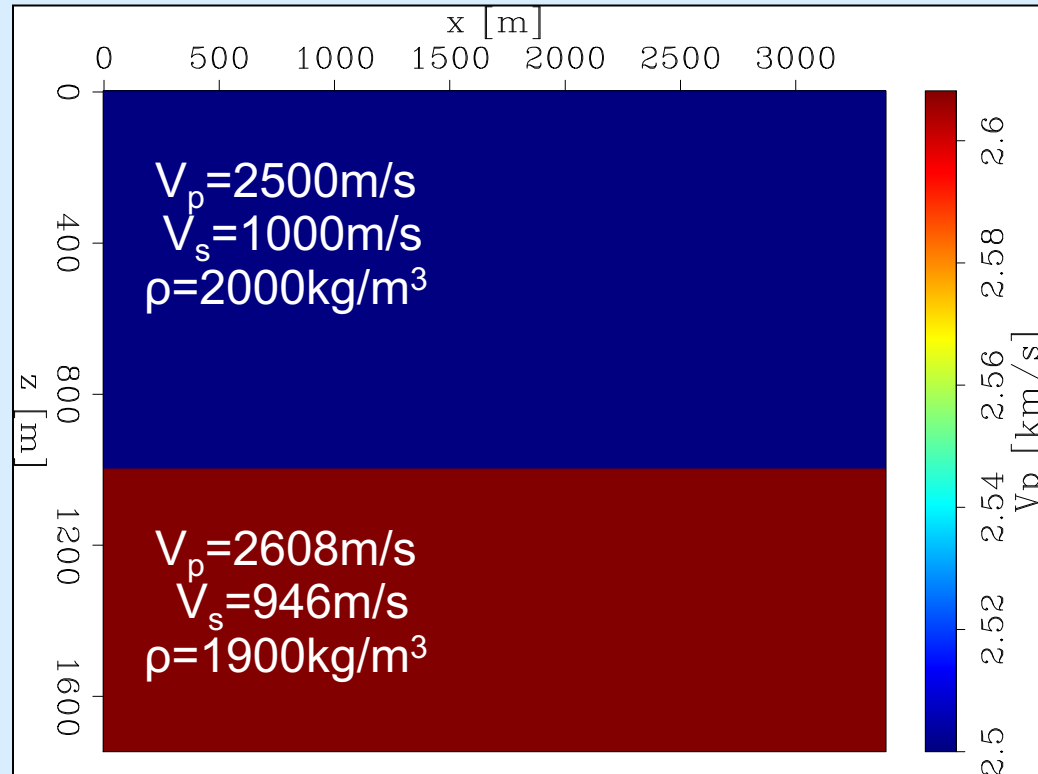
Usually using Amplitude Variations with Offsets

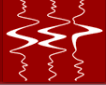




AVO response

$$\Delta V_p > 0; \Delta V_s < 0 \quad \Delta \rho < 0$$

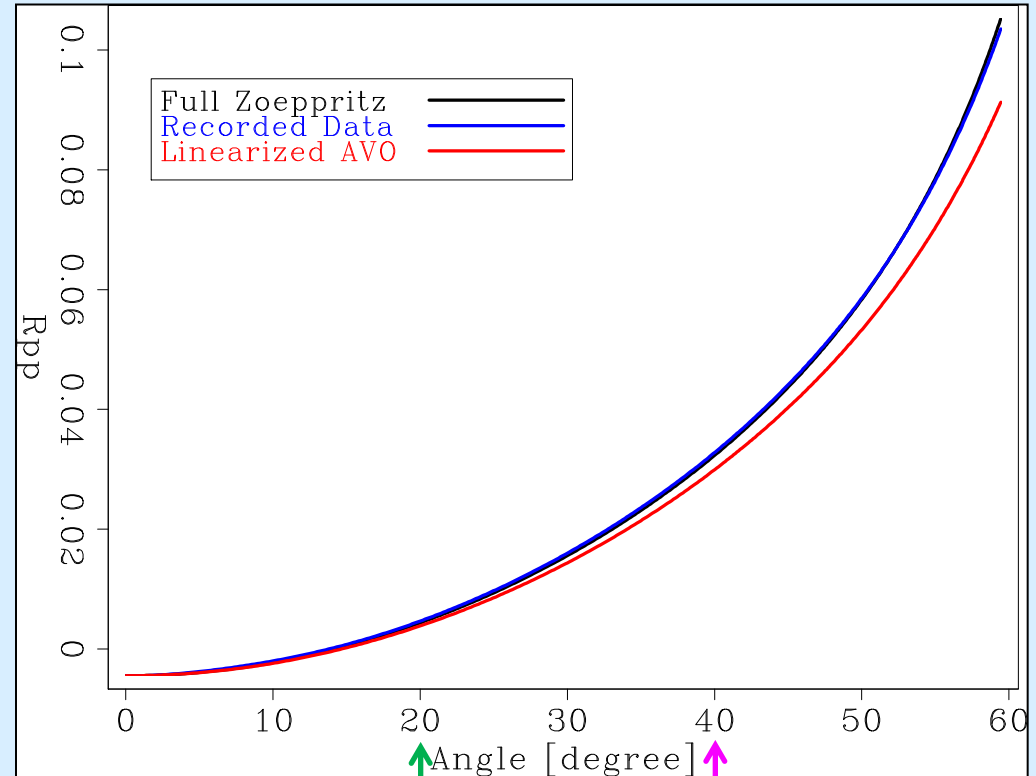
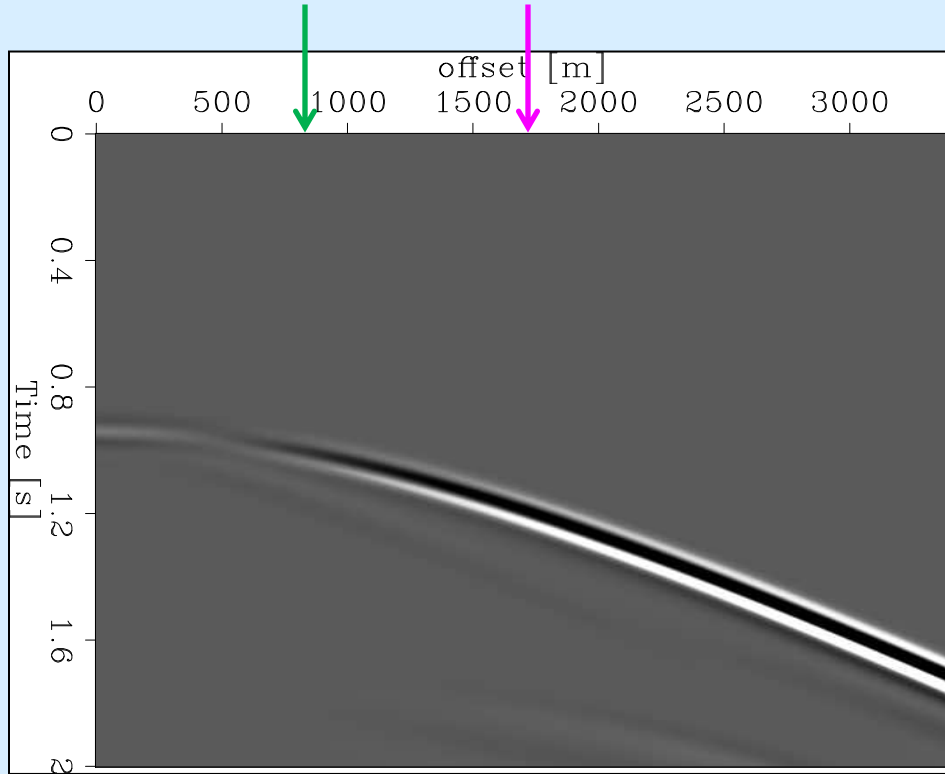


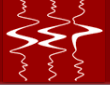


AVO response

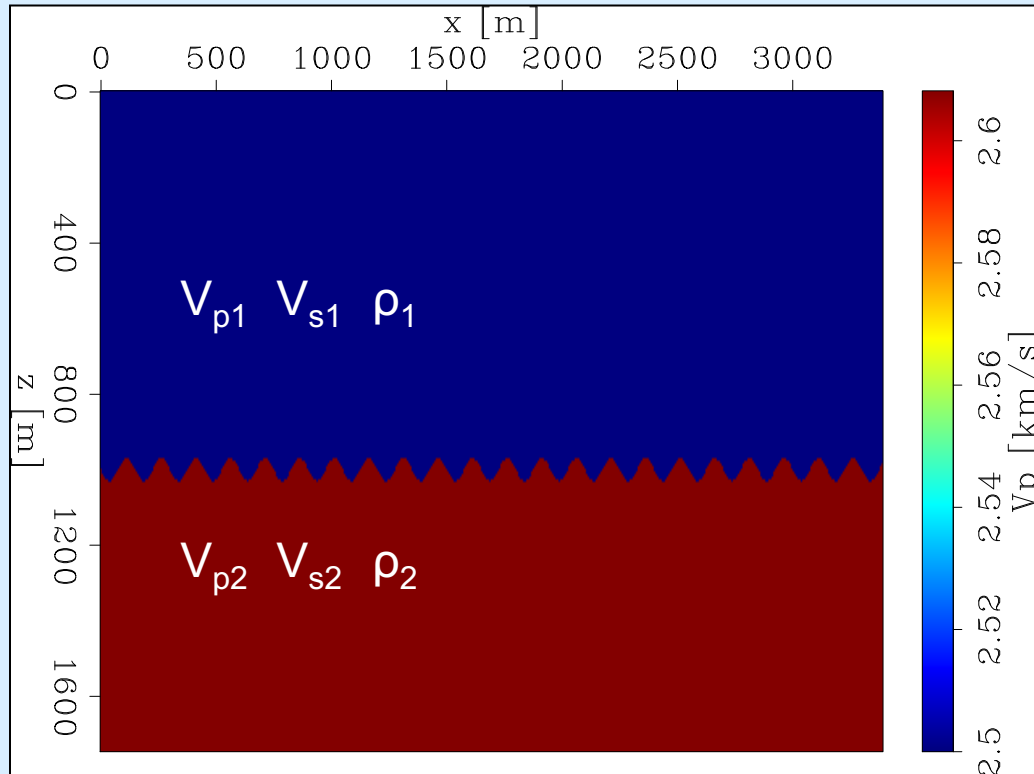
Flat reflector case

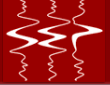
725m 1675m



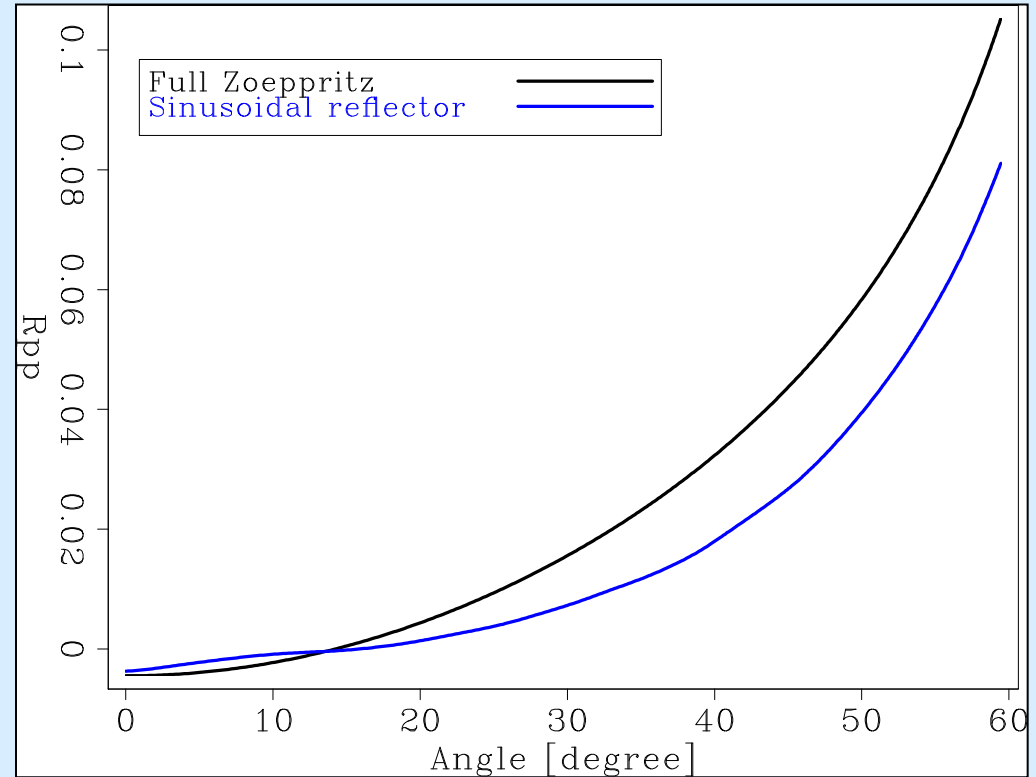
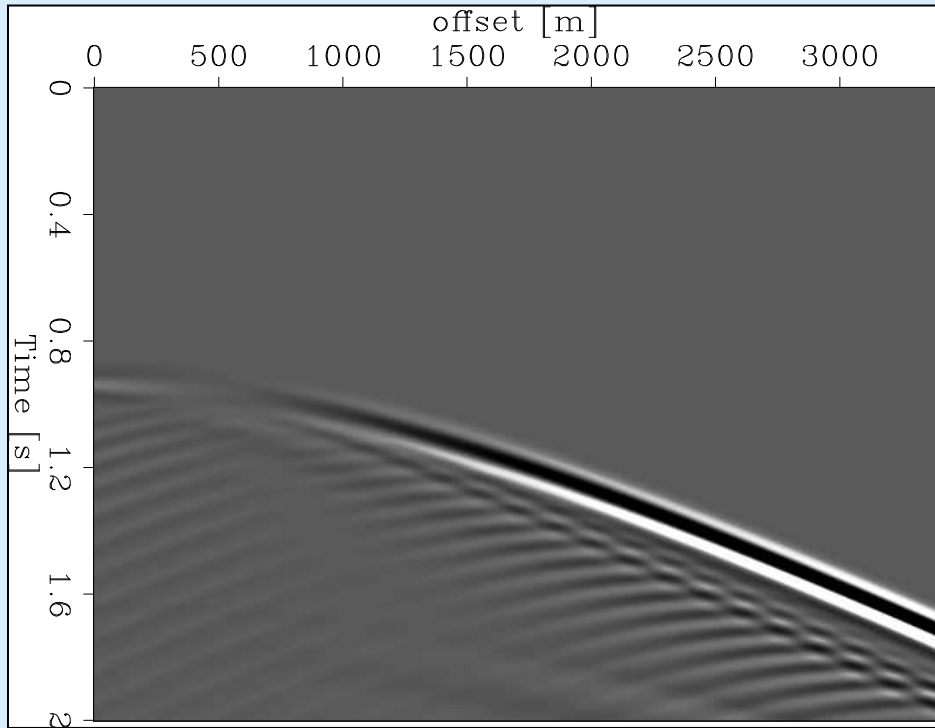


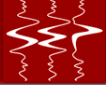
Sinusoidal reflector: planar reflector assumption



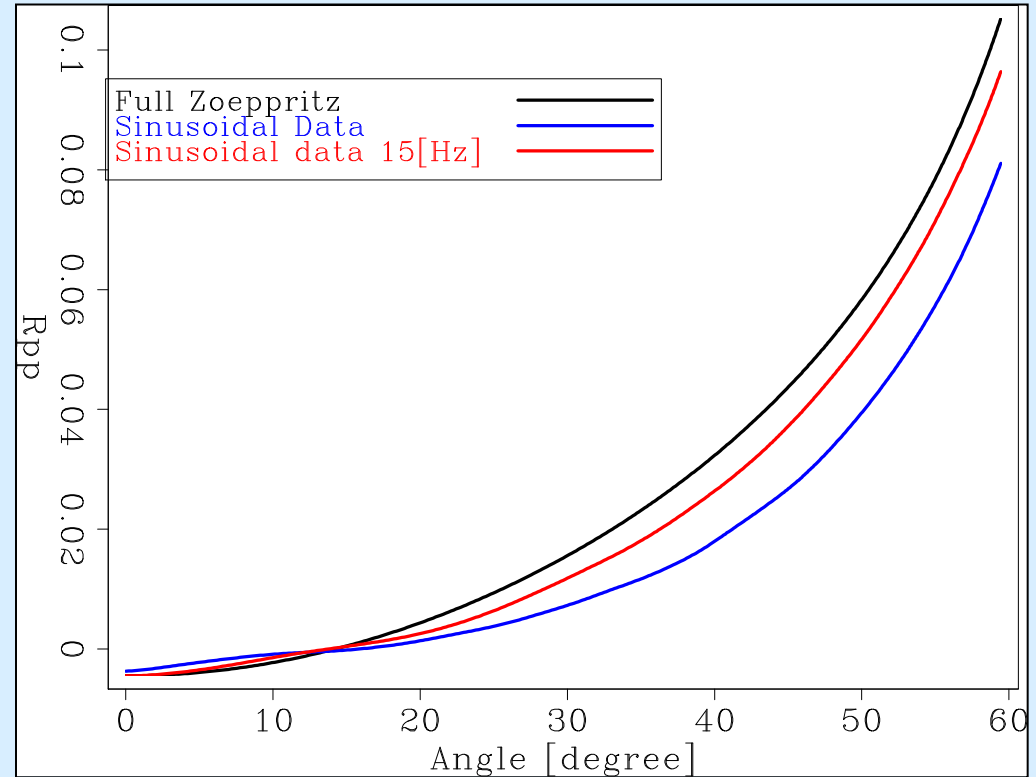
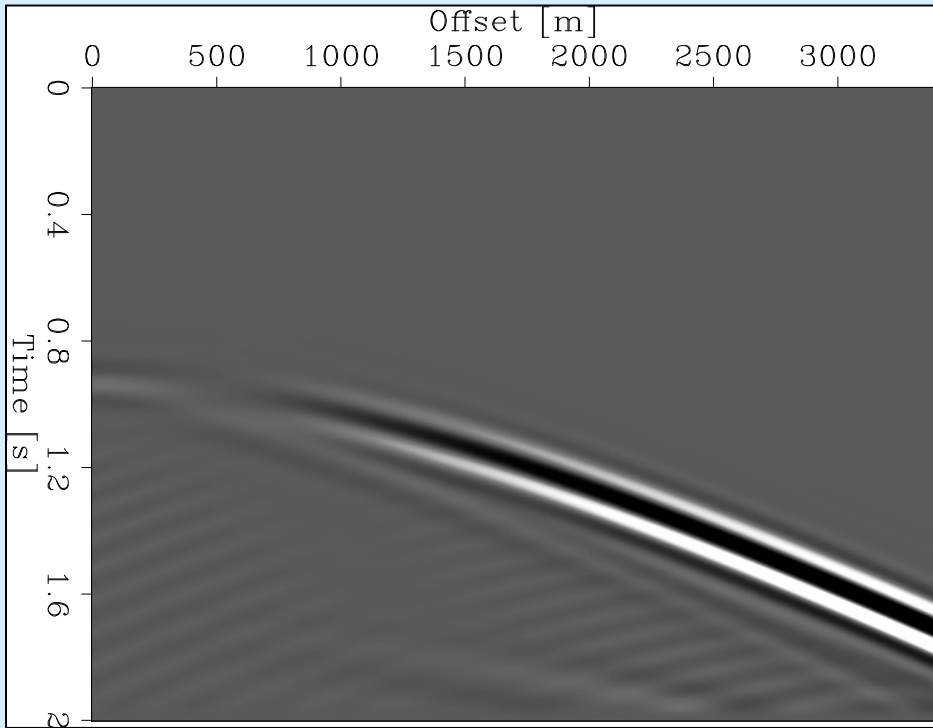


Sinusoidal reflector: planar reflector assumption





Sinusoidal reflector: planar reflector assumption The bandwidth matters!



Full waveform inversion uses all the frequencies in the data!

$$\phi(V_p, V_s, \rho) = \frac{1}{2} \|f(V_p, V_s, \rho) - d\|_2^2$$

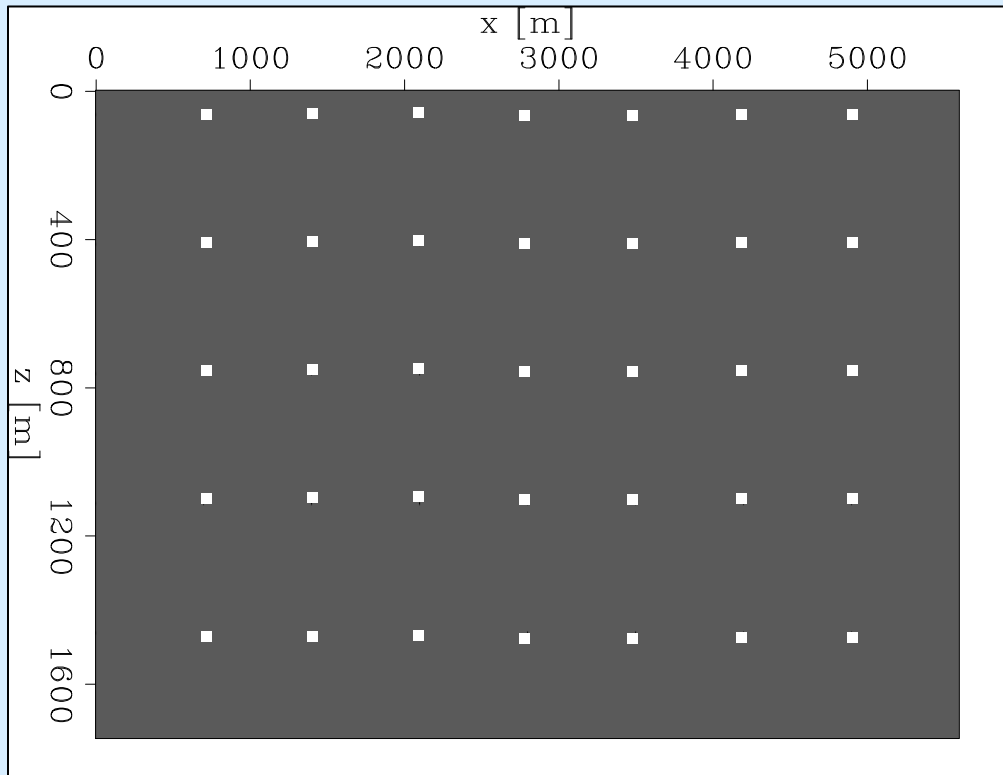
Full waveform inversion uses all the frequencies in the data!

$$\phi(V_p, V_s, \rho) = \frac{1}{2} \|f(V_p, V_s, \rho) - d\|_2^2$$

However:

- Computationally intensive
(wave-equation-based)**
- Affected by parameter cross-talk
("leakage" of one parameter into the other)**

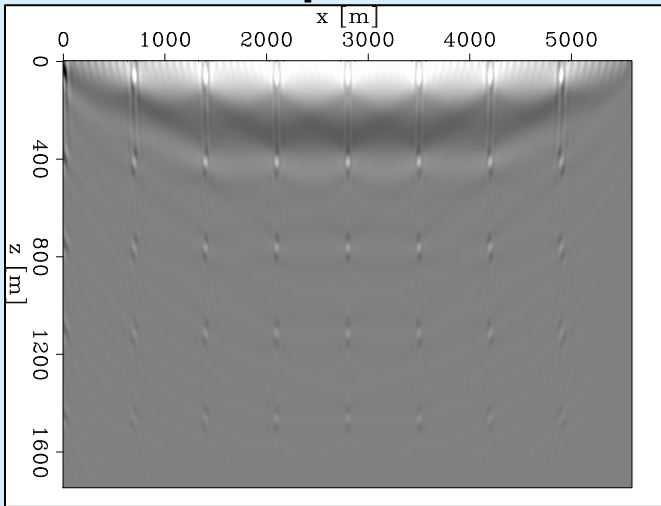
True perturbation is in Vp only:



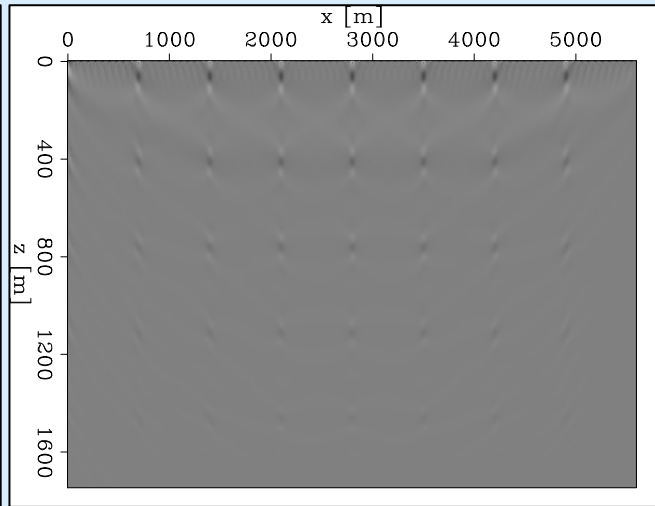
True perturbation is in Vp only:
compute the gradient

$$g(m) = B^* r$$

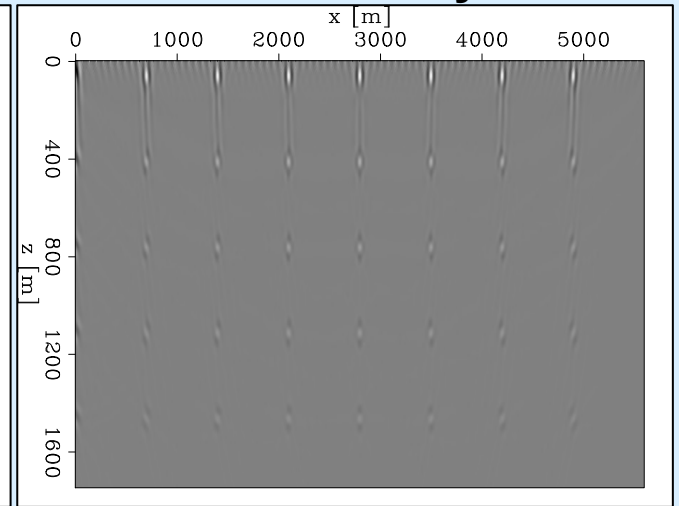
Vp

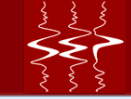


Vs



Density





**Hessian-based optimization techniques
(e.g., truncated Newton)
diminish parameter cross-talk!**

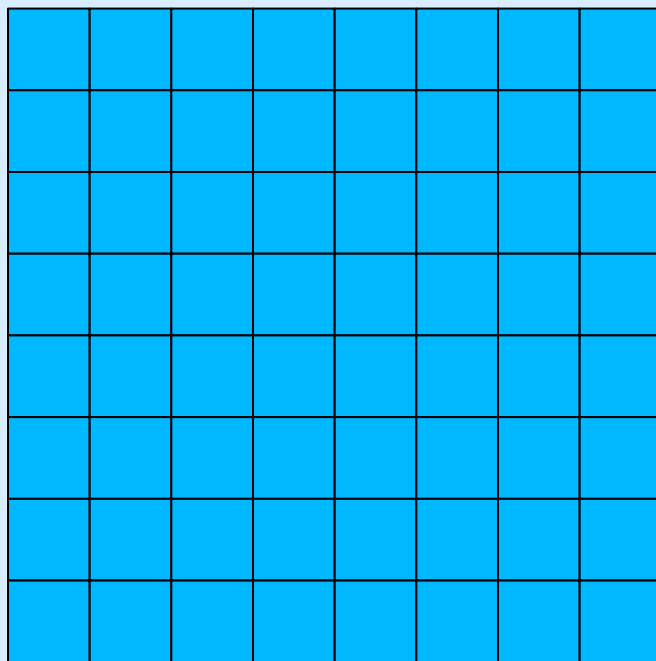
**Hessian-based optimization techniques
(e.g., truncated Newton)
diminish parameter cross-talk!**

**How do we estimate a computationally efficient
Hessian-based preconditioner?**

$$\frac{\partial^2 \phi(\mathbf{m})}{\partial \mathbf{m}^2} = \mathbf{H}(\mathbf{m})$$

model parameters

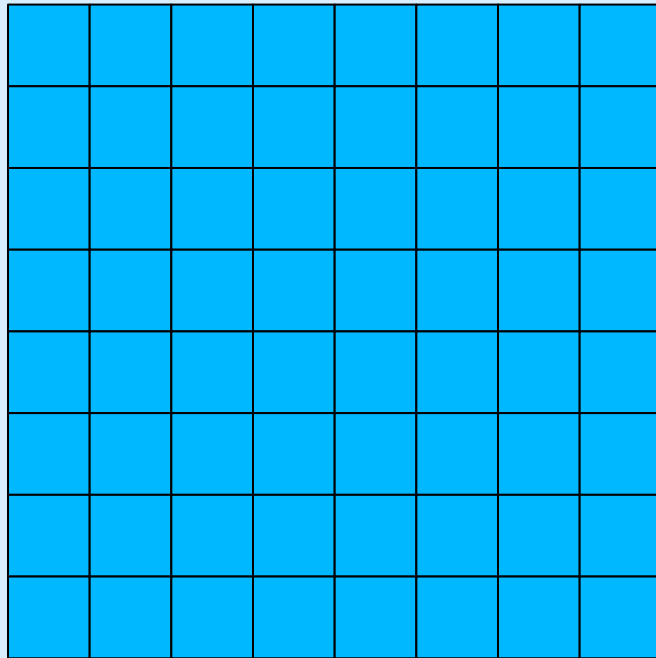
model parameters



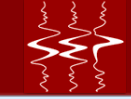
$$\frac{\partial^2 \phi(\mathbf{m})}{\partial \mathbf{m}^2} = \mathbf{H}(\mathbf{m})$$

model parameters

model parameters

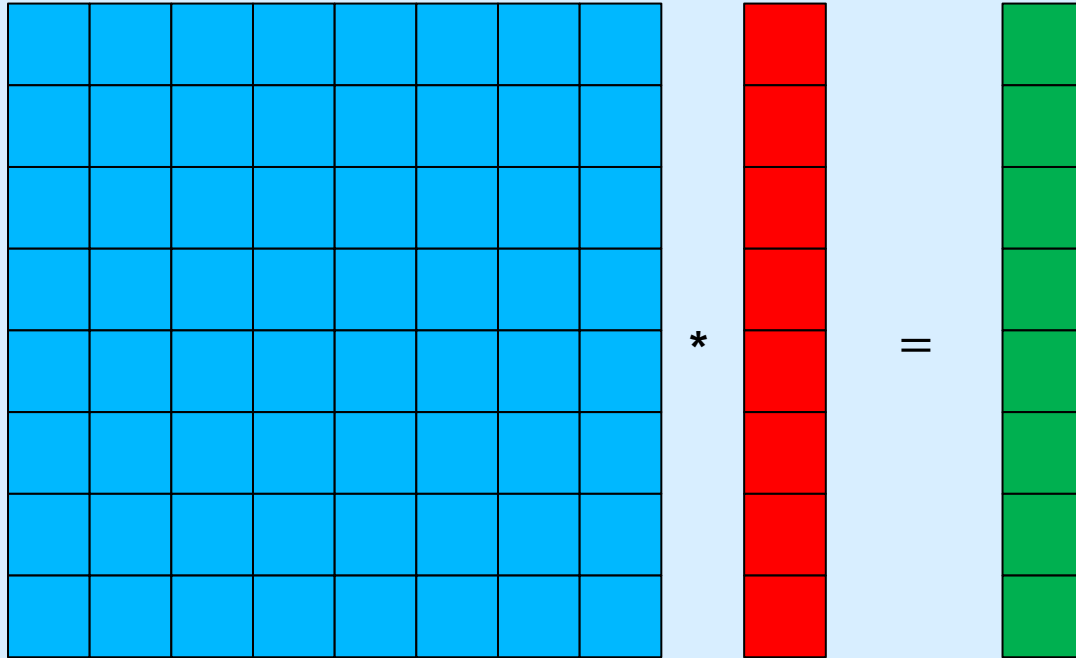


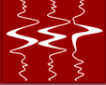
**EVEN FOR SIMPLE
2D PROBLEM IT HAS:
 $\approx 10^{9-12}$ elements**



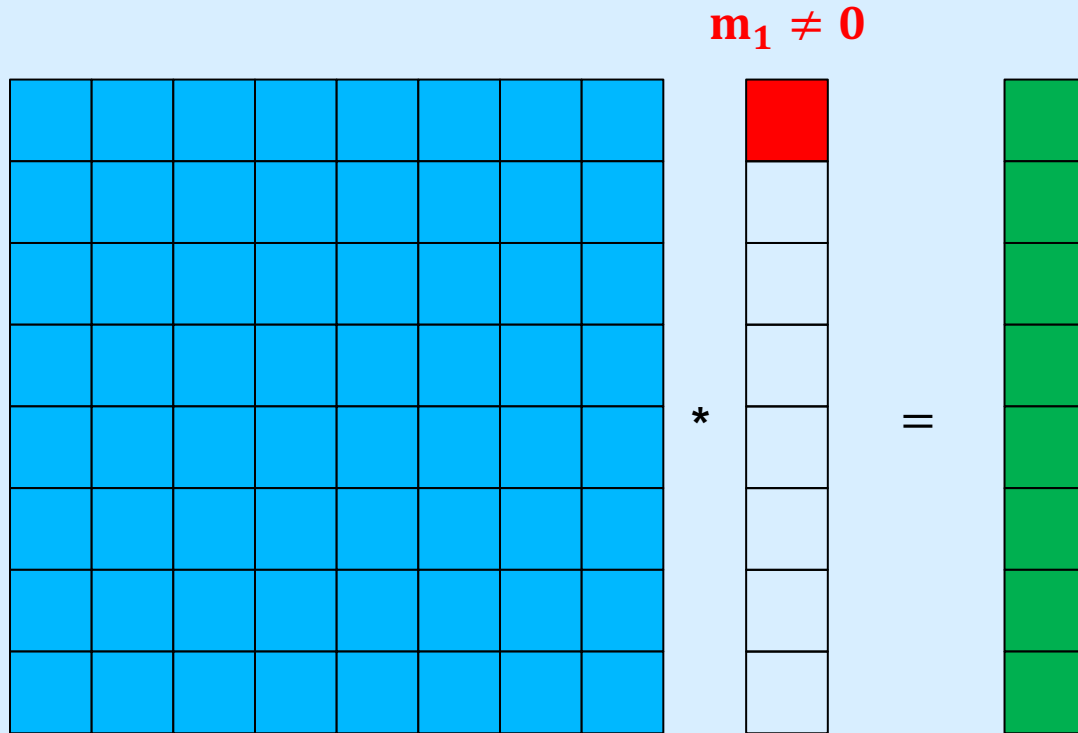
Elastic FWI: Hessian estimation

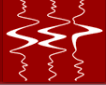
$$H(m)\mathbf{m} = \tilde{\mathbf{m}}$$





$$H(m)\mathbf{m} = \tilde{\mathbf{m}}$$

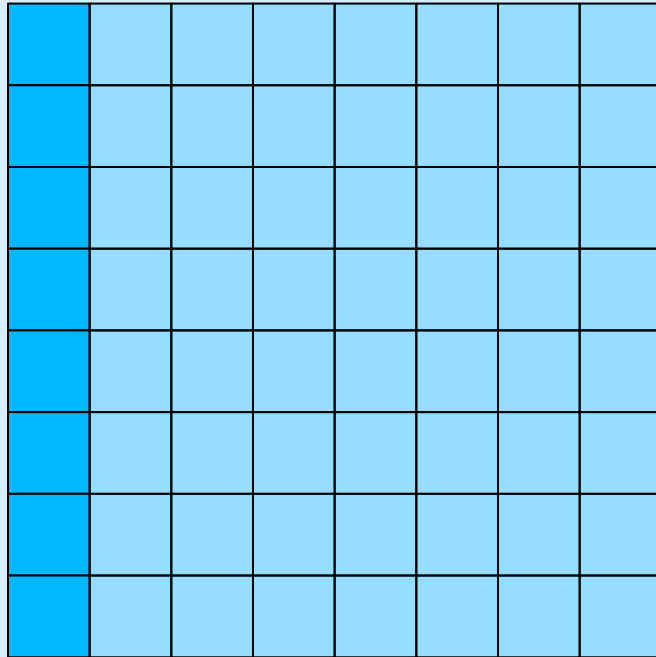




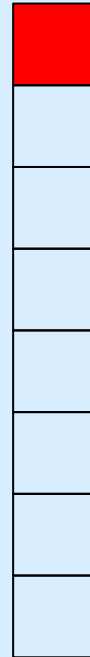
Elastic FWI: Hessian estimation

$$H(m)\mathbf{m} = [H(m)]_{i1}$$

$[H(m)]_{i1}$



$\mathbf{m}_1 \neq 0$



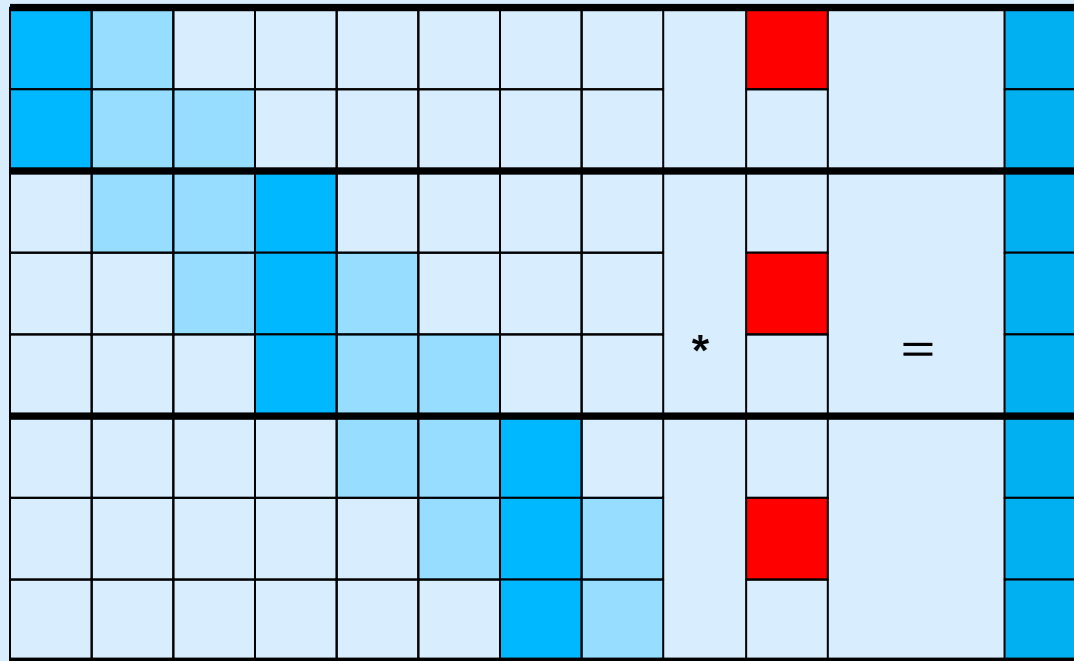
*

=

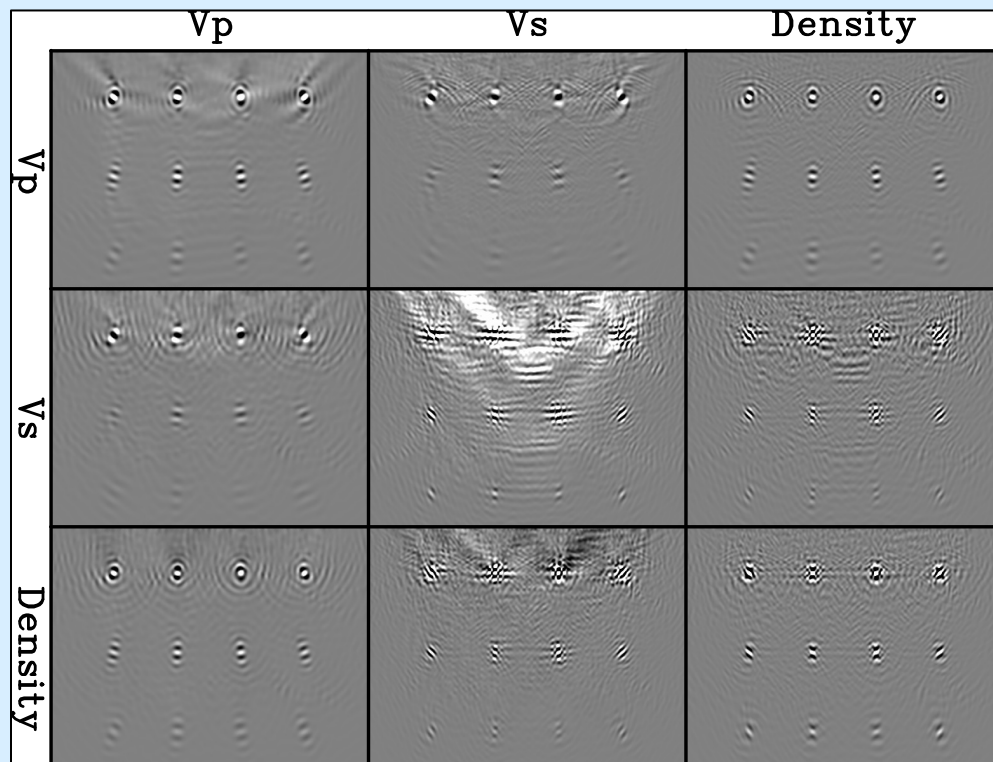
$[H(m)]_{i1}$



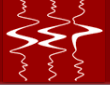
$$H(m)\mathbf{m} = \tilde{\mathbf{m}}$$



Application of the Hessian for element estimation

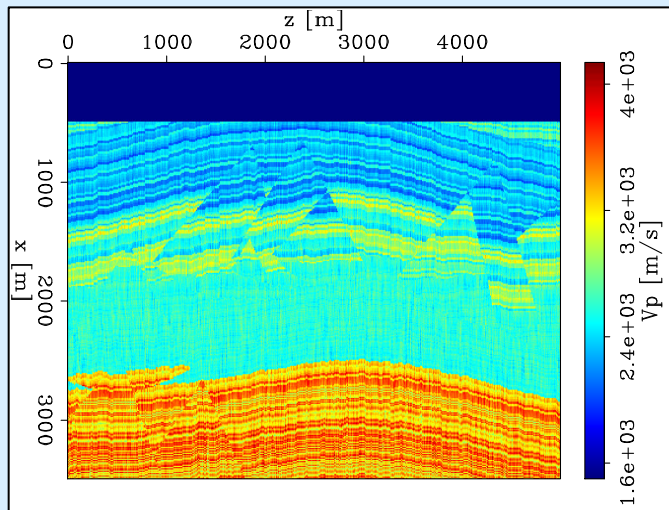


(Tang, 2015)

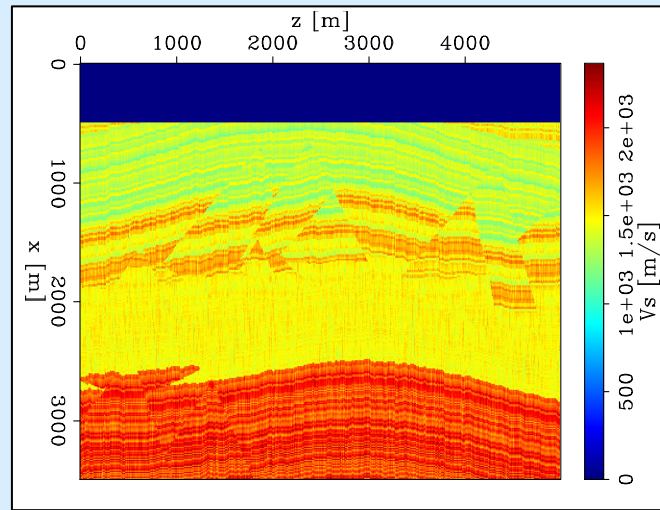


Elastic Full Waveform Inversion with multi-component data

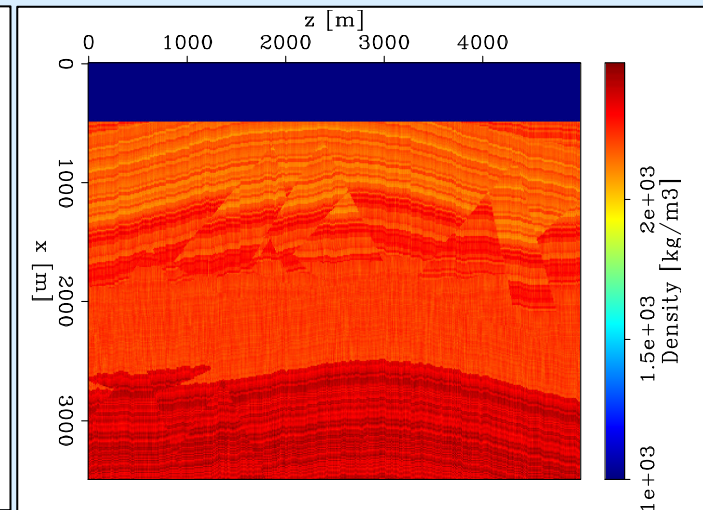
- 50 shots with 500 multi-component receivers



Vp



Vs



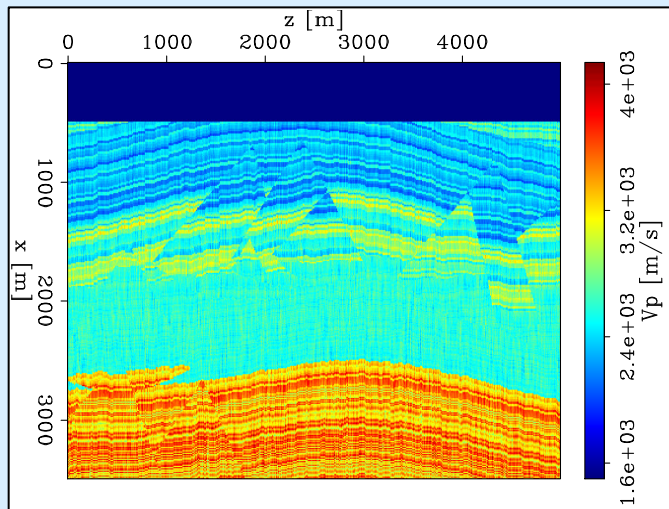
Density

(Clapp, 2014)

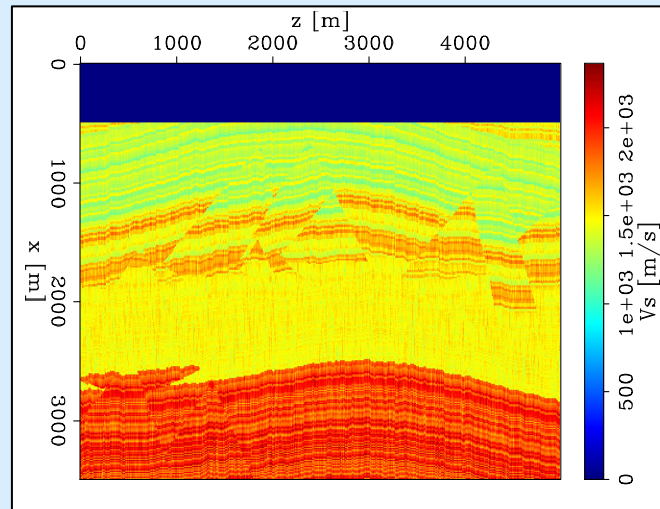


Elastic Full Waveform Inversion with multi-component data

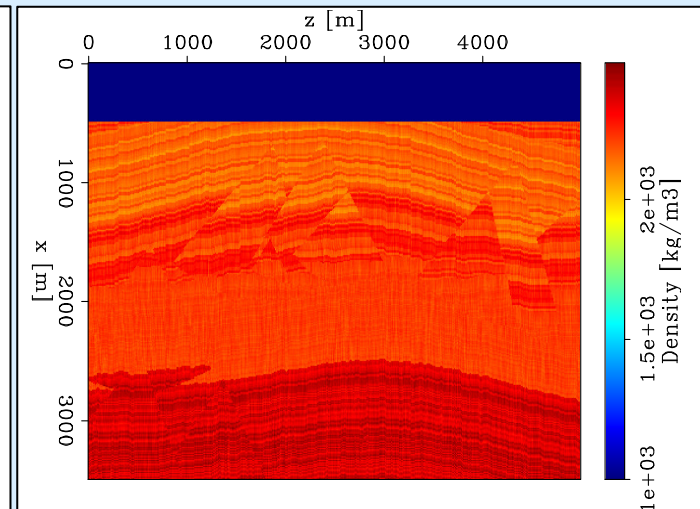
- 50 shots with 500 multi-component receivers
- Multi-scale approach (4 bands: up to 5/10/15/20 Hz)



Vp



Vs



Density

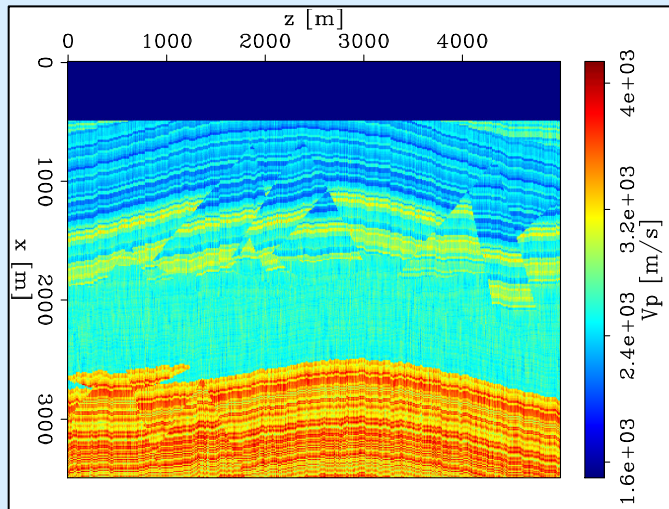
(Clapp, 2014)



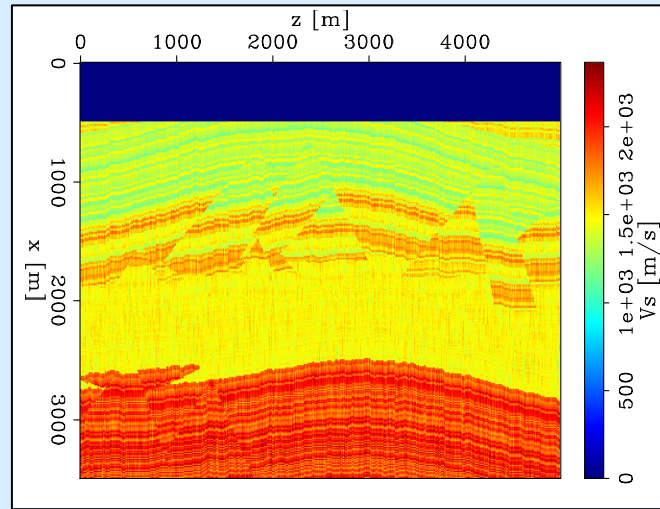
Elastic FWI: synthetic test

Elastic Full Waveform Inversion with multi-component data

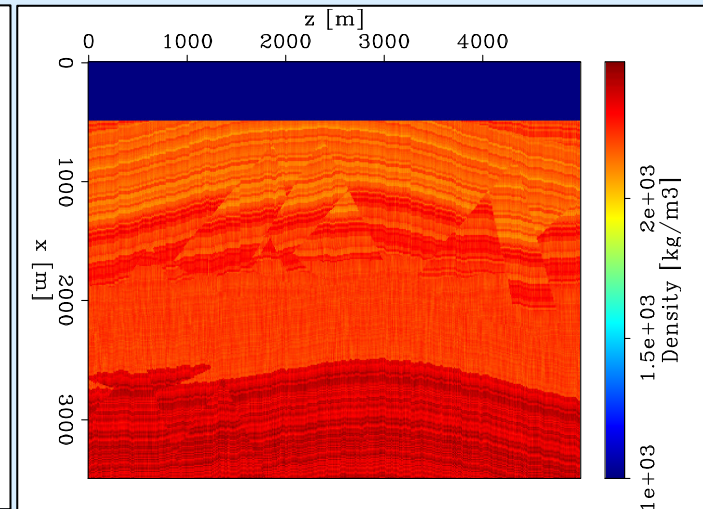
- 50 shots with 500 multi-component receivers
- Multi-scale approach (4 bands: up to 5/10/15/20 Hz)
 - 40 iterations for each band



Vp

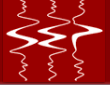


Vs

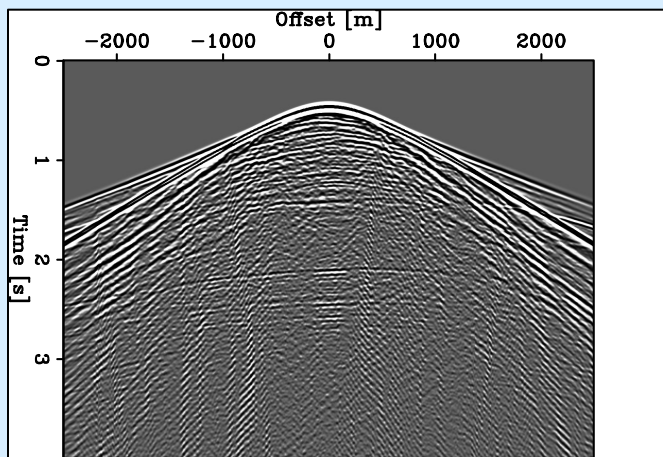


Density

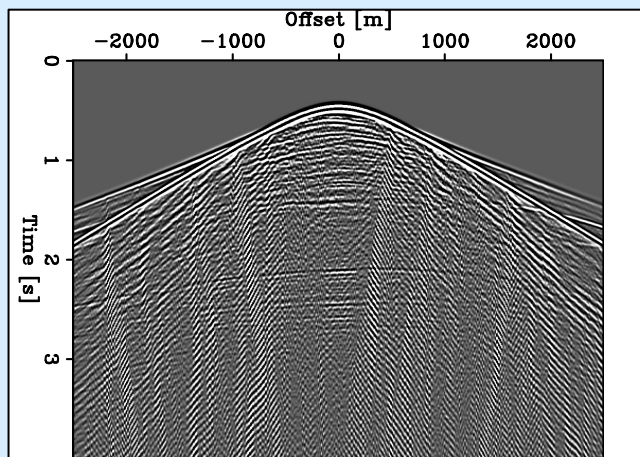
(Clapp, 2014)



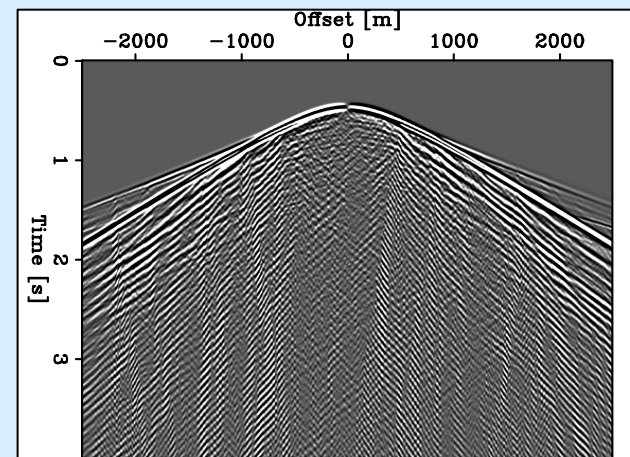
Recorded multi-component data for central shot



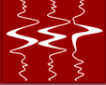
Pressure



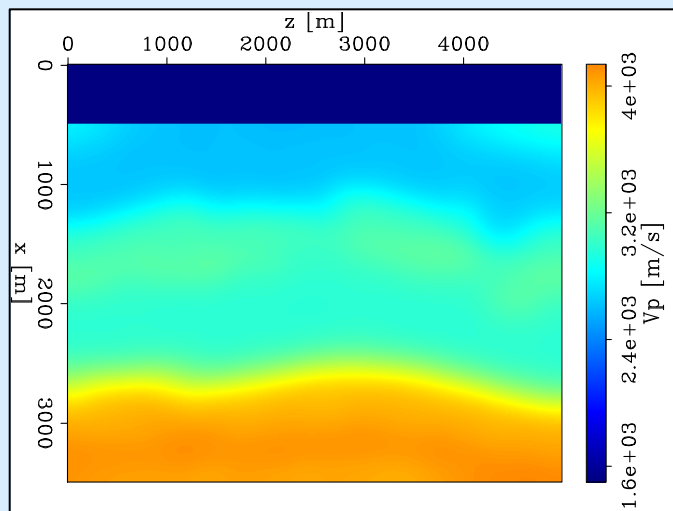
V_z



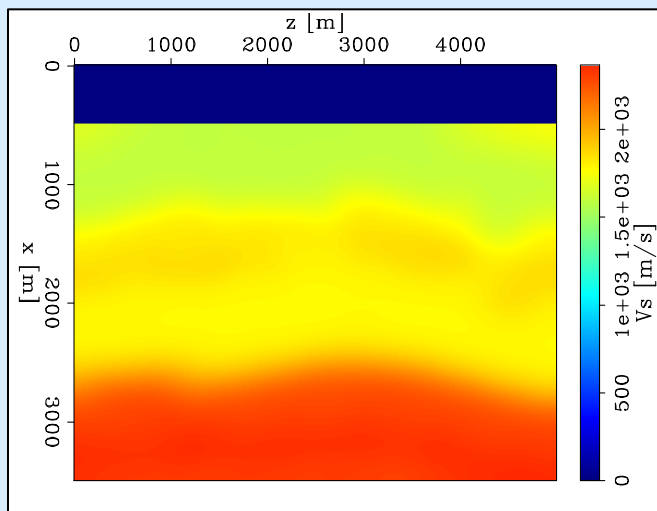
V_x



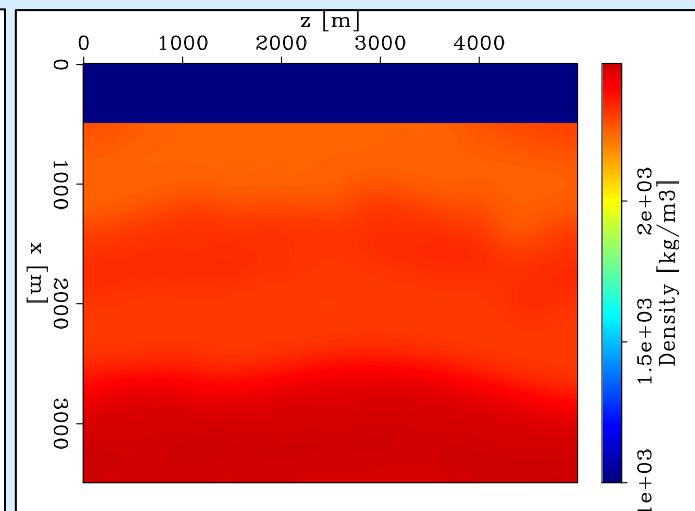
Starting subsurface model



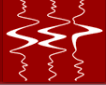
V_p



V_s



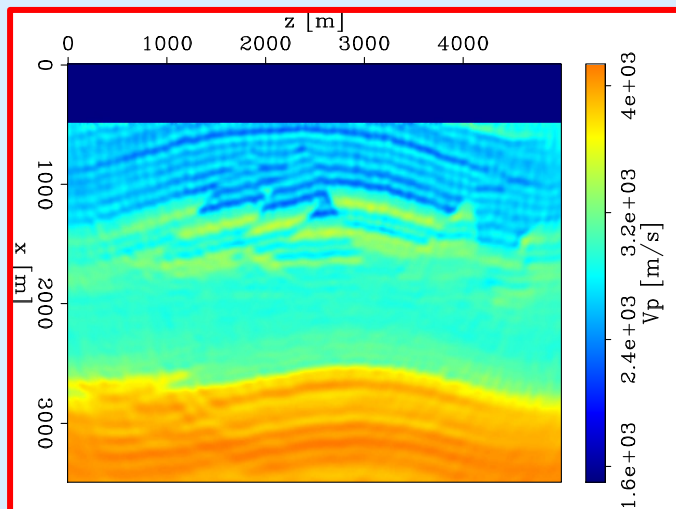
Density



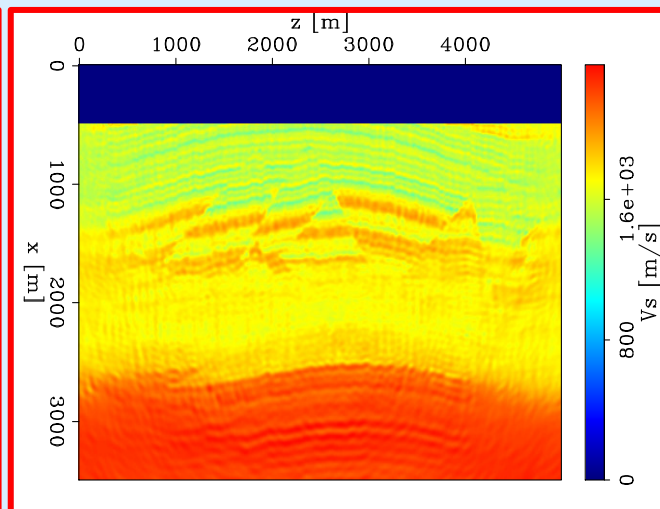
Elastic FWI: synthetic test

40 iterations for 4 bands (5/10/15/20)

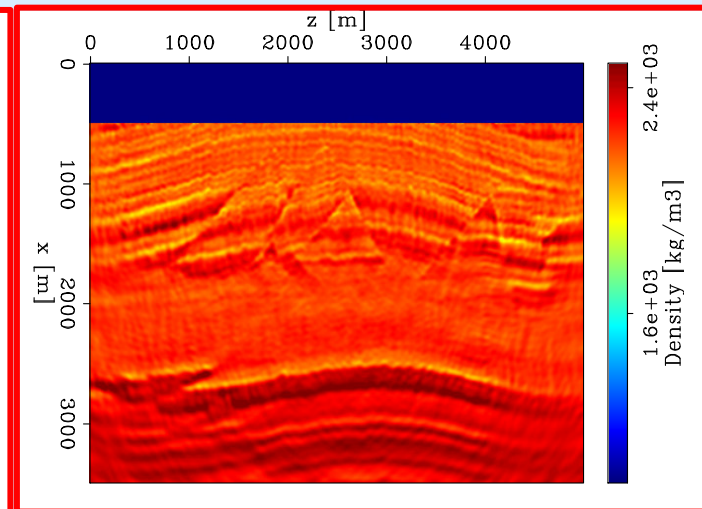
Inverted model **without preconditioning**



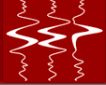
V_p



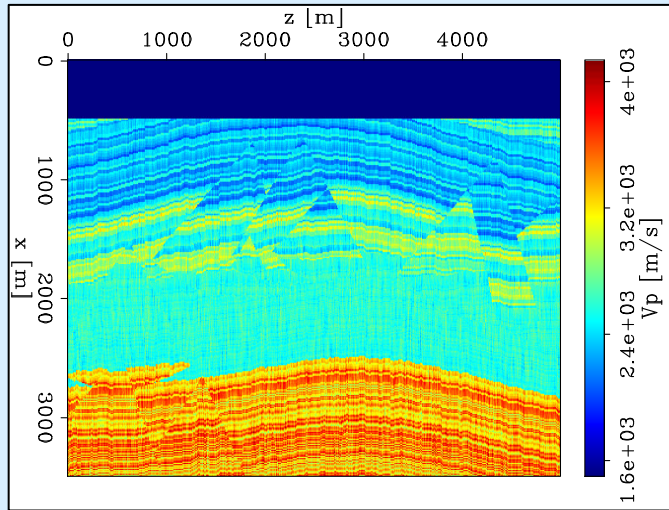
V_s



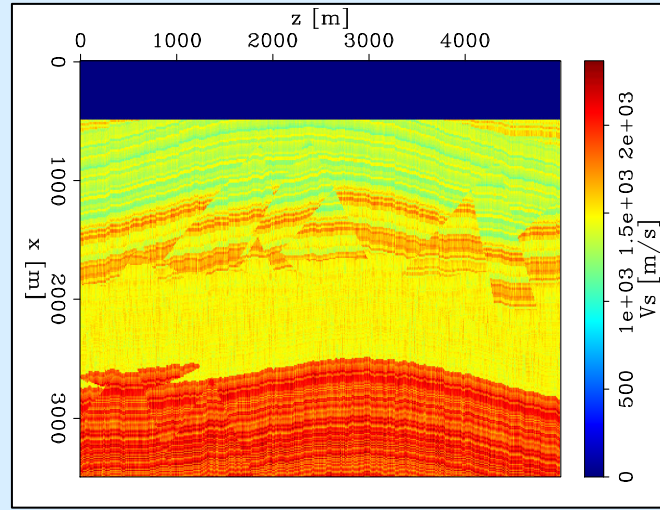
Density



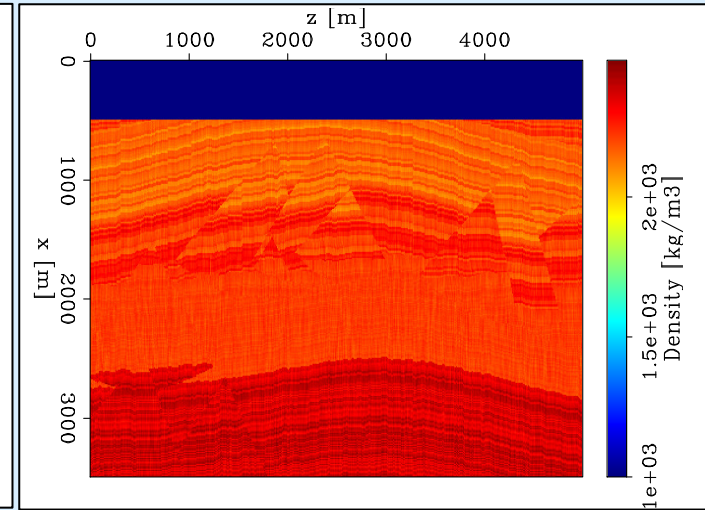
True subsurface model



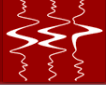
V_p



V_s



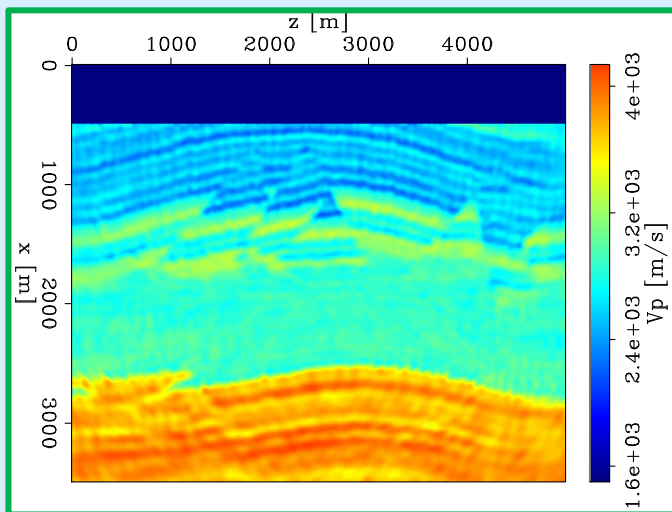
Density



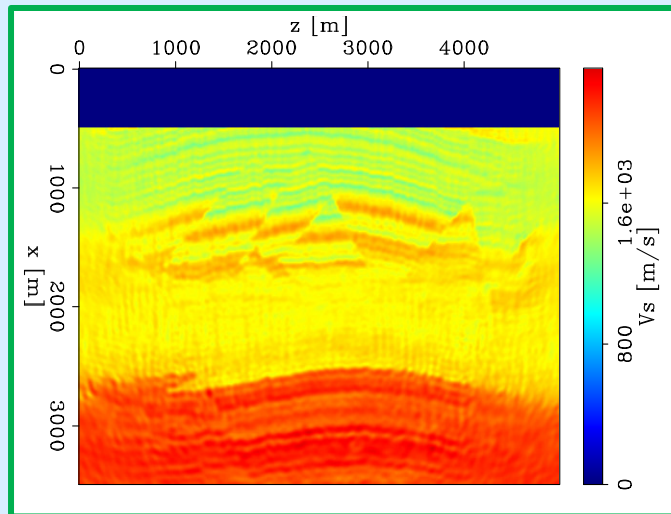
Elastic FWI: synthetic test

40 iterations for 4 bands (5/10/15/20)

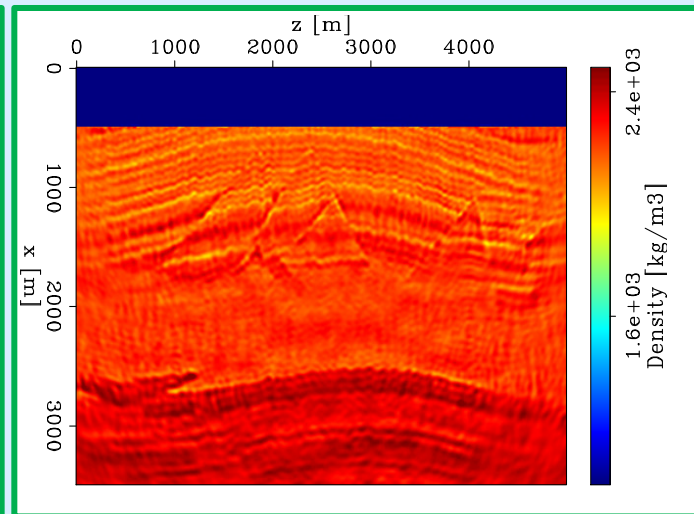
Inverted model with preconditioning



V_p



V_s



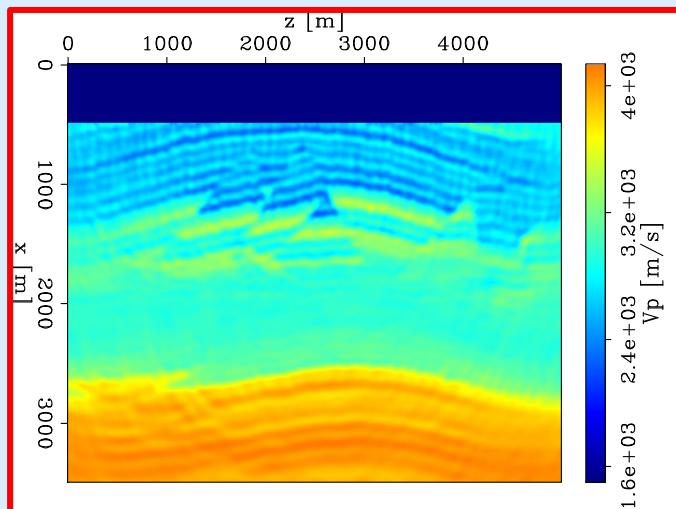
Density



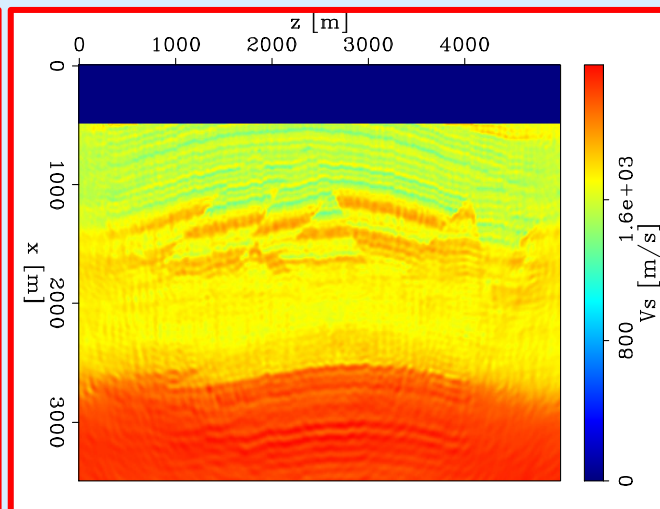
Elastic FWI: synthetic test

40 iterations for 4 bands (5/10/15/20)

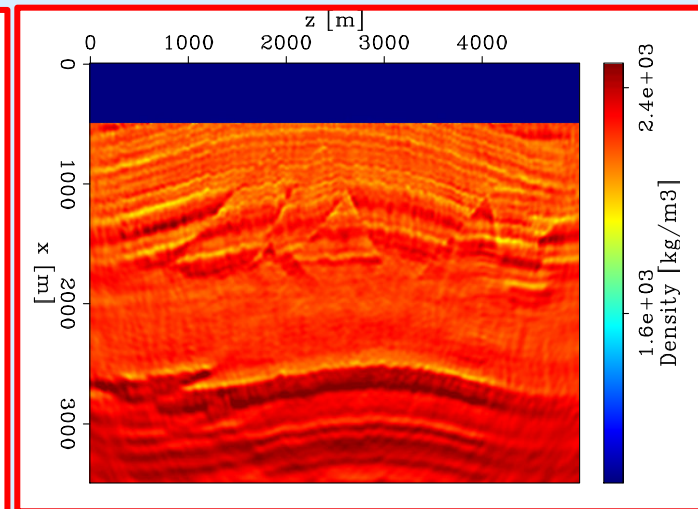
Inverted model **without preconditioning**



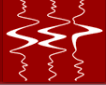
V_p



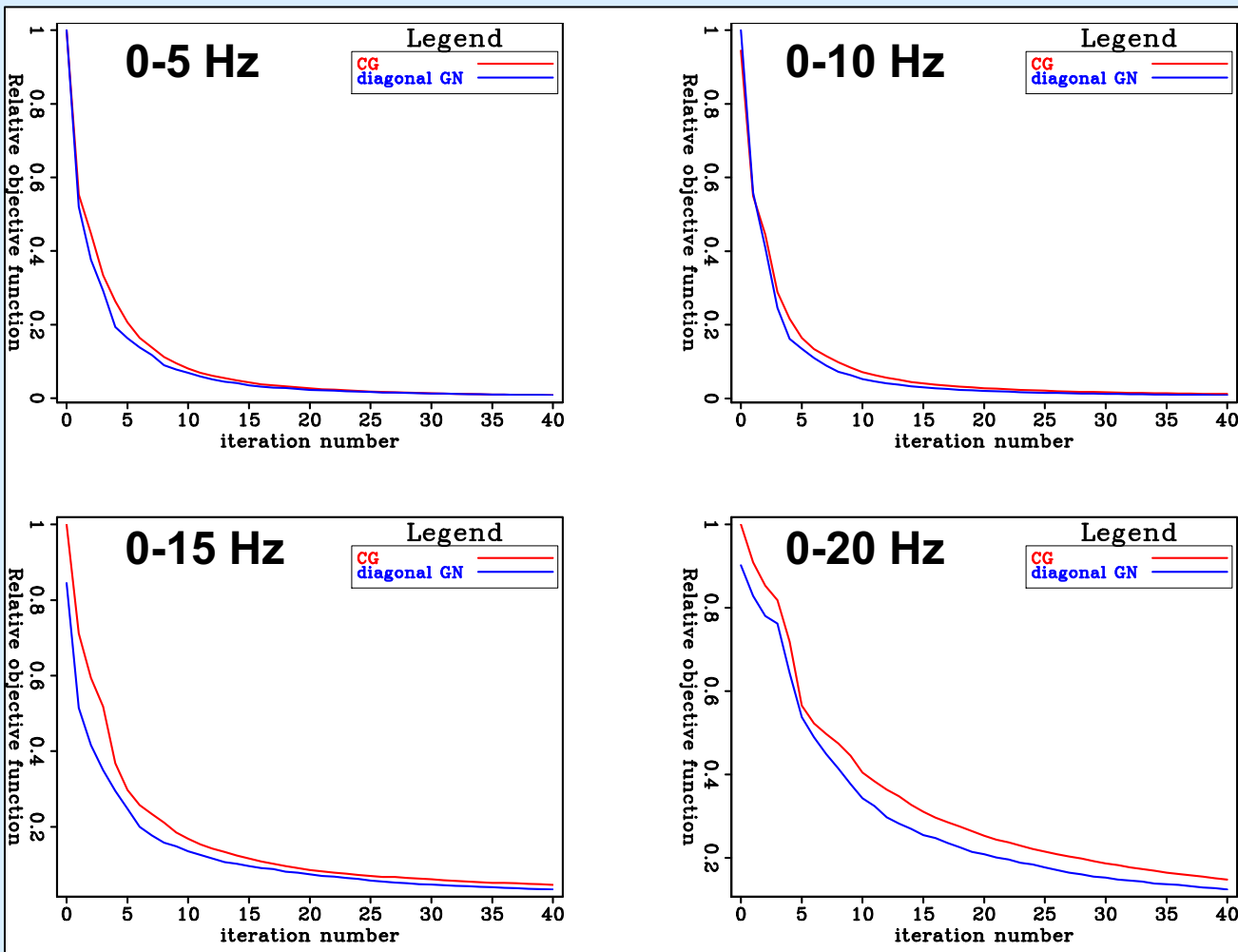
V_s



Density



Elastic FWI: synthetic test



- 1. Conventional AVO modeling/inversion fails for complex interface**
- 2. Elastic full waveform inversion solves for all the frequencies in the data but is affected by parameter cross-talk**
- 3. A simple diagonal approximation already reduces cross-talk in the FWI results for a complex subsurface model**

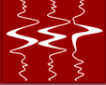
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**Thank you for your attention
Questions?**

18th April 2017



Residuals comparison after inversion

