

# Anisotropic Full Waveform Inversion

Source Estimation and Rock Physics Preconditioning

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SEP168

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- Seismic modeling often assumes simple physics, e.g. acoustic, constant density, no surface waves, or absorbing boundaries...
- This leads to amplitude mismatch between modeled and observed data.
- Source estimation by directly minimizing FWI objective function can help reduce amplitude mismatch.

$$f(\mathbf{m}, s) = \frac{1}{2} \|d(\mathbf{m}, s) - d_0\|_2^2.$$

- $\mathbf{m}$ : velocity model
- $s$ : wavelet
- $d$ : modeled data
- $d_0$ : observed data

$$d = \mathbf{RPQ}s.$$

- **Q**: injection of the source function at shot locations
- **P**: forward propagation
- **R**: recording of wavefields at receivers

$$\frac{\partial f}{\partial s} = \mathbf{Q}^T \mathbf{P}^T \mathbf{R}^T (d - d_0).$$

- $\mathbf{R}^T$ : injection of receiver locations
- $\mathbf{P}^T$ : backward propagation operator
- $\mathbf{Q}^T$ : recording at source locations
- Note: **no cross-correlation**

# Source estimation: Example

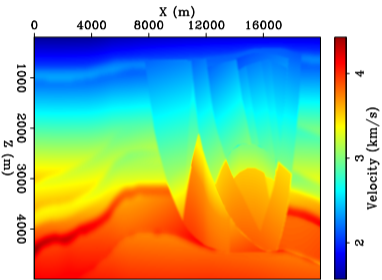


Figure 1: True velocity

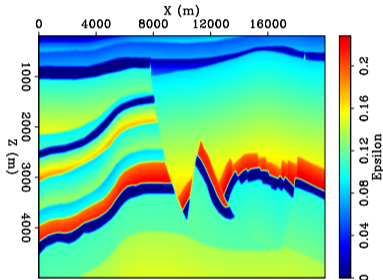


Figure 2: True  $\epsilon$

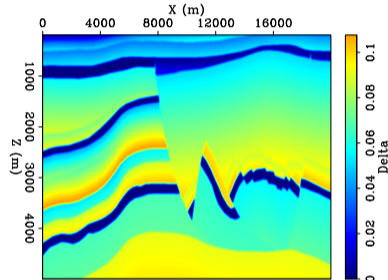


Figure 3: True  $\delta$

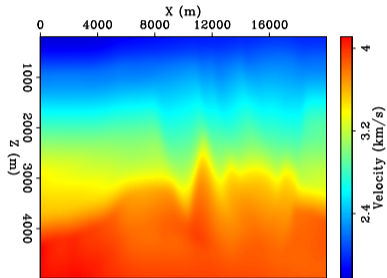


Figure 4: Background velocity

# Source estimation: Example

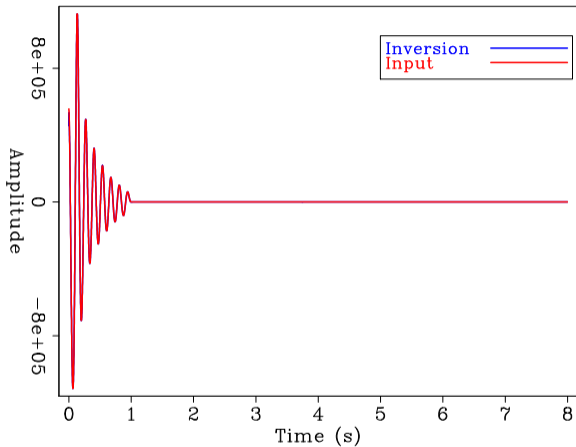


Figure 5: **Input** and **inverted** wavelets

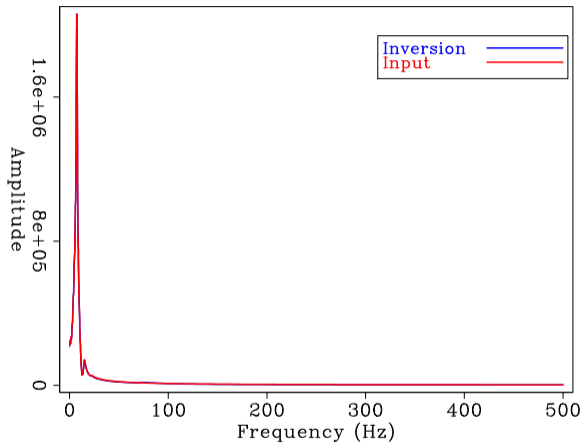


Figure 6: **Input** and **inverted** spectra



# Source estimation: Example

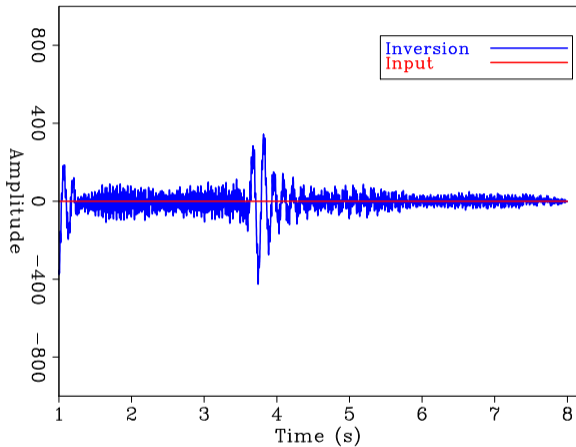


Figure 7: **Input** and **inverted** wavelets

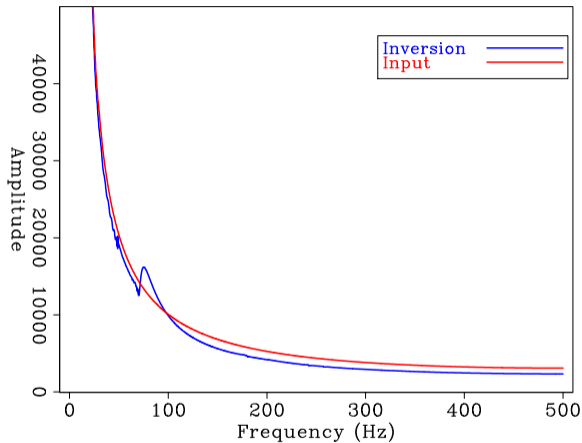


Figure 8: **Input** and **inverted** spectra

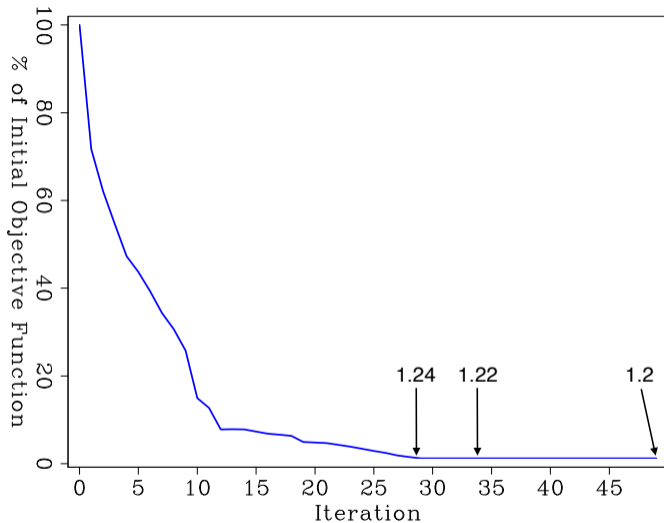


Figure 9: Objective function

- Parameters have different physical interpretations, dimensions, magnitudes, and sensitivities.
- Tradeoff and crosstalk can lead to unrealistic results.
- The Hessian can help reduce crosstalk and speedup convergence but **expensive**.
- Rock physics is another way to obtain model covariances.

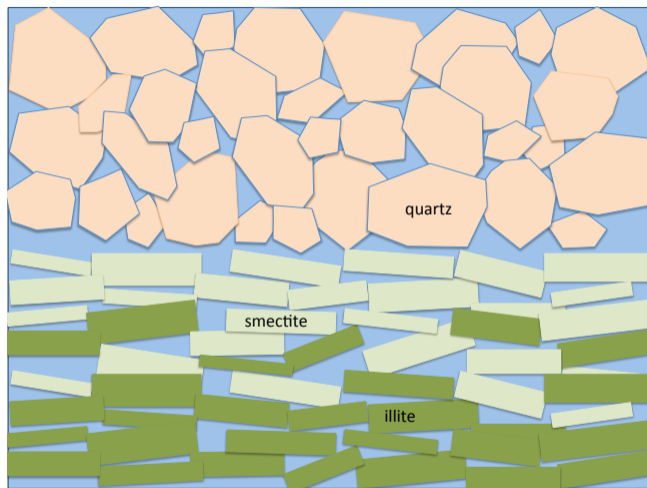


Figure 10: Sand-shale layers typical for Gulf of Mexico

- Shale volume:  $V_{\text{shale}}$
- Temperature increases with burial/depth, smectite transforms into illite.
- Temperature determines illite percentage:  $P_{\text{illite}}(T)$ .

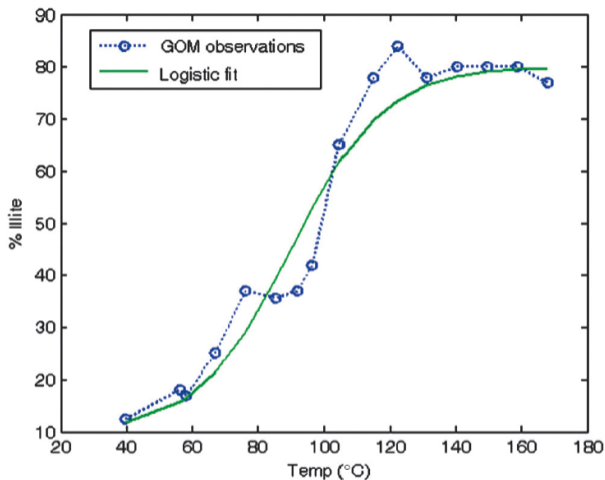


Figure 11: Smectite-illite transition (Bachrach, 2011)

# Compaction

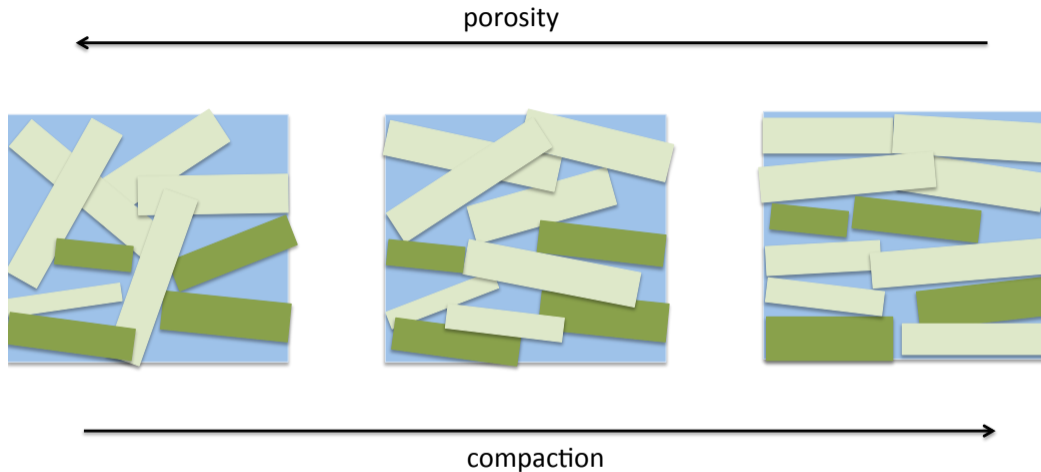


Figure 12: Compaction model for shale: porosity decreased while anisotropy increases as increasing compaction

- Porosity:  $\phi = ae^{bz} + ce^{dz}$  (Dutta et al, 2009)
- Average stiffnesses of clay:  $c_{ij}(c_{ij}^{\text{particle}}, W)$  (Brandyopadhyay, 2009)
- Orientation distribution:  $W(\phi)$

# Rock physics model: Differential Effective Medium

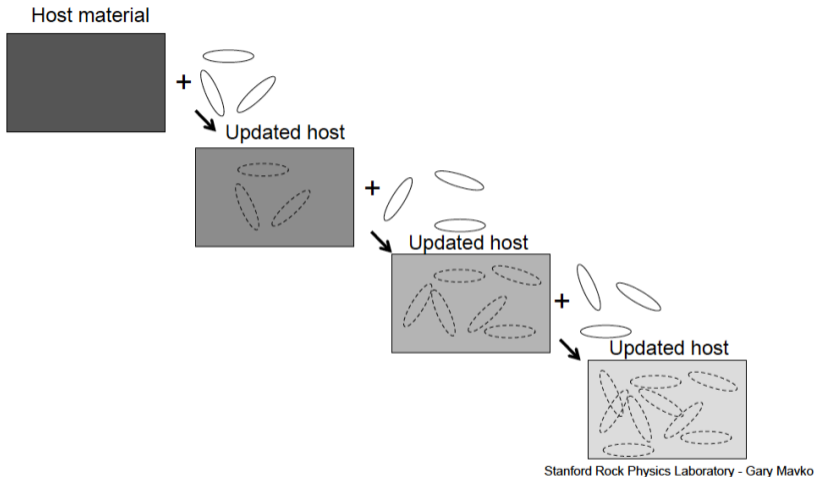


Figure 13: Differential Effective Medium (DEM) model adds inclusions in small increments and updates.



# Rock physics model: Differential Effective Medium

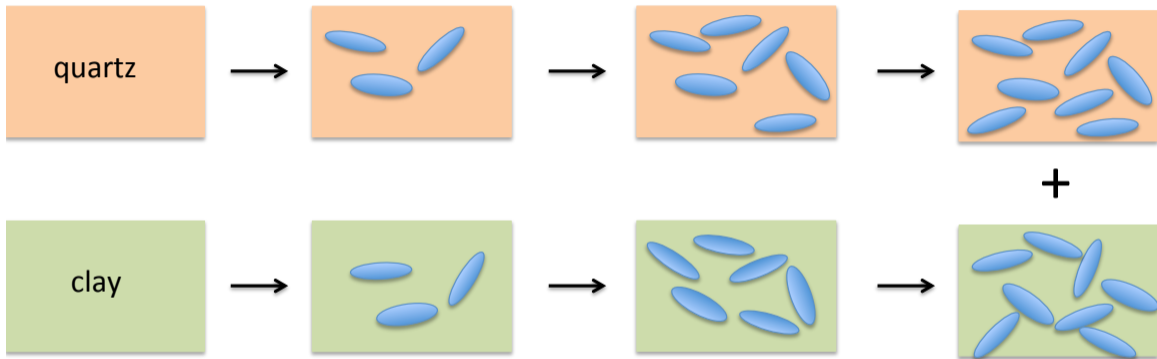


Figure 14: Model sand and shale layers separately, calibrate, and add.

- ① From uniform distributions, randomly select values for parameters like reaction temperatures, clay orientation parameters, critical porosity, and aspect ratio.
- ② Calibrate porosity-depth trends for sand and shale and the total porosity.
- ③ Model sand and shale using DEM.
- ④ Compute the average stiffnesses of sand-shale layers.
- ⑤ Repeat to calibrate with well data and generate many earth models.
- ⑥ Compute the mean models and covariances.

# Field application: sand-shale selection

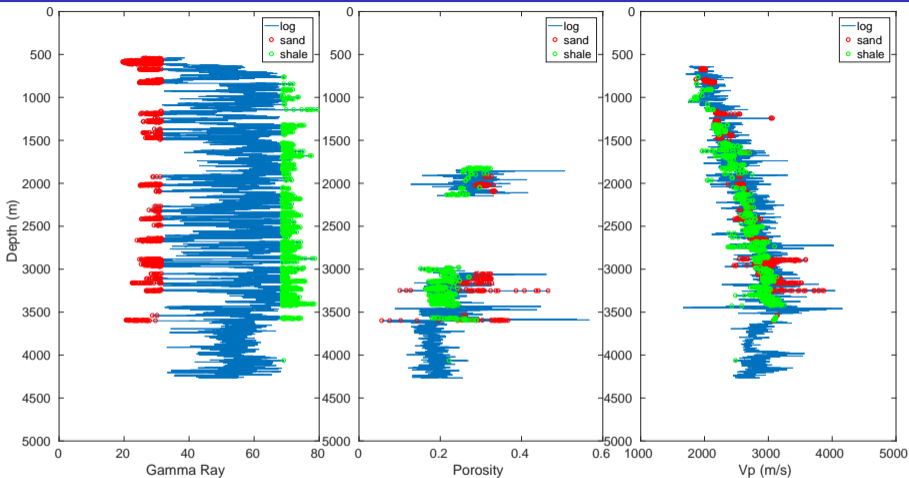


Figure 15: Gamma ray as indication of sand-shale<sup>1</sup>

<sup>1</sup>Includes data supplied by IHS Energy Log Services, Copyright 2017, IHS Energy Log Services Inc.

# Field application: porosity calibration

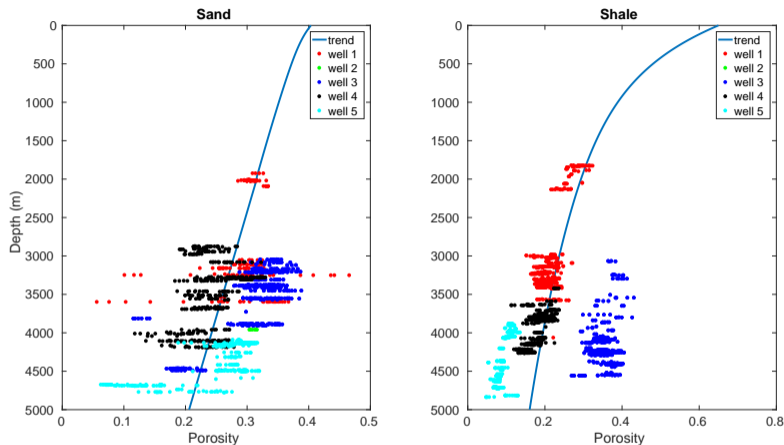


Figure 16: Calibration of porosity<sup>2</sup>:  $\phi = ae^{bz} + ce^{dz}$

<sup>2</sup>Includes data supplied by IHS Energy Log Services, Copyright 2017, IHS Energy Log Services Inc.

# Field application: velocity calibration

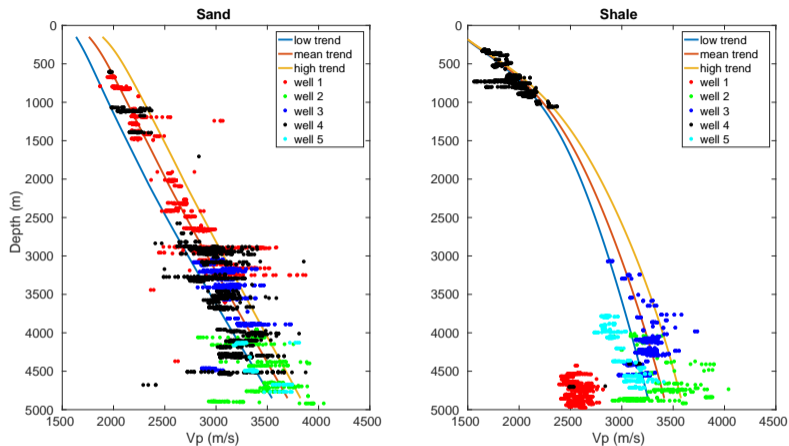


Figure 17: Calibration of velocity<sup>3</sup>

<sup>3</sup>Includes data supplied by IHS Energy Log Services, Copyright 2017, IHS Energy Log Services Inc.

# Field application: distributions

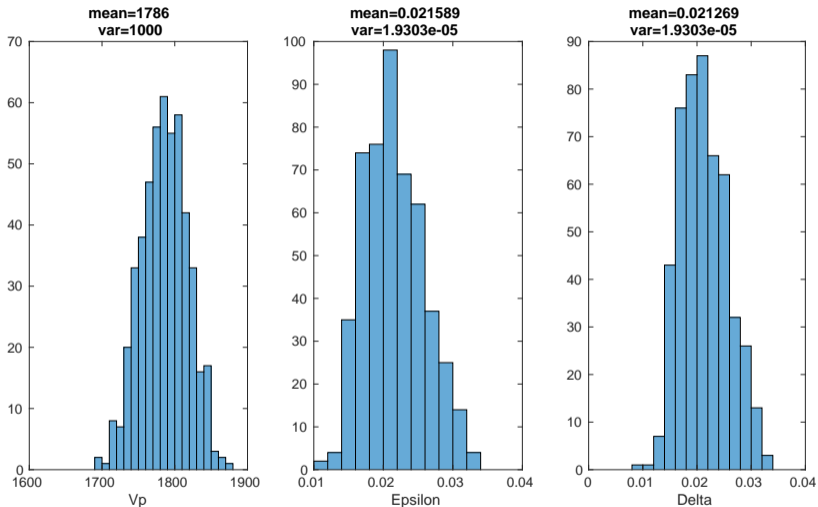


Figure 18: Shallow sandy shale (more shale than sand)

# Field application: distributions

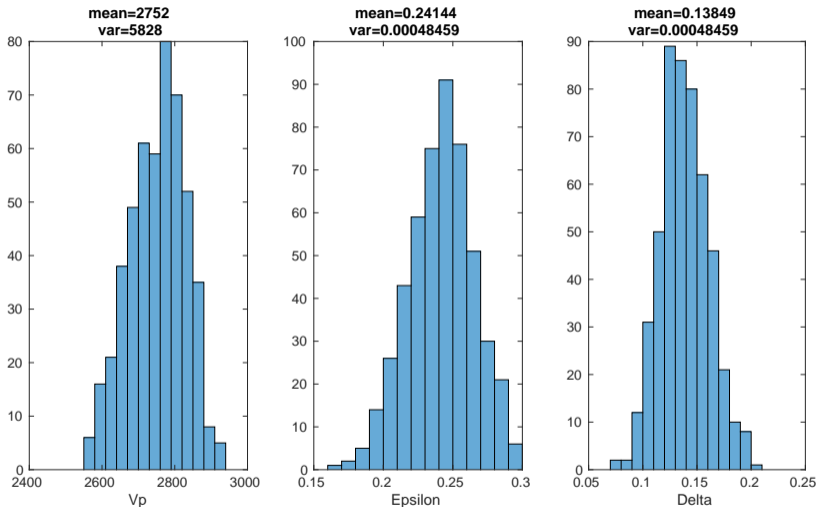


Figure 19: Deep sandy shale

# Field application: distribution

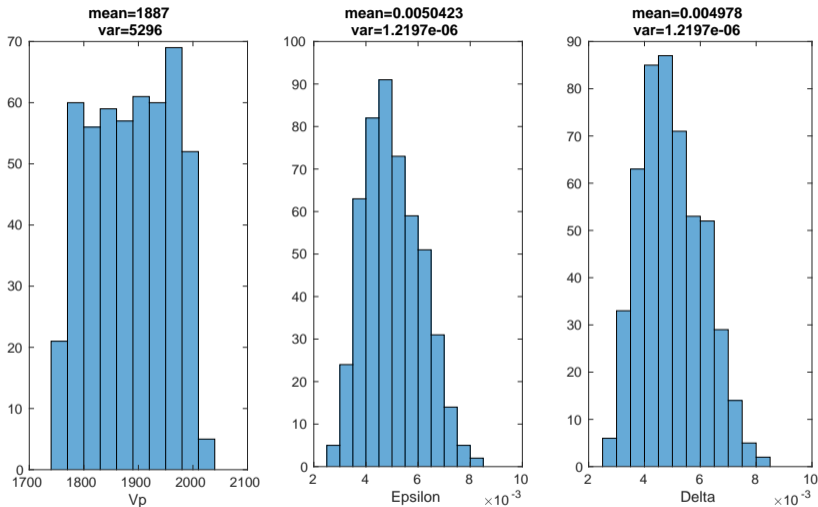


Figure 20: Shallow shaly sand (more sand than shale)



# Field application: distributions

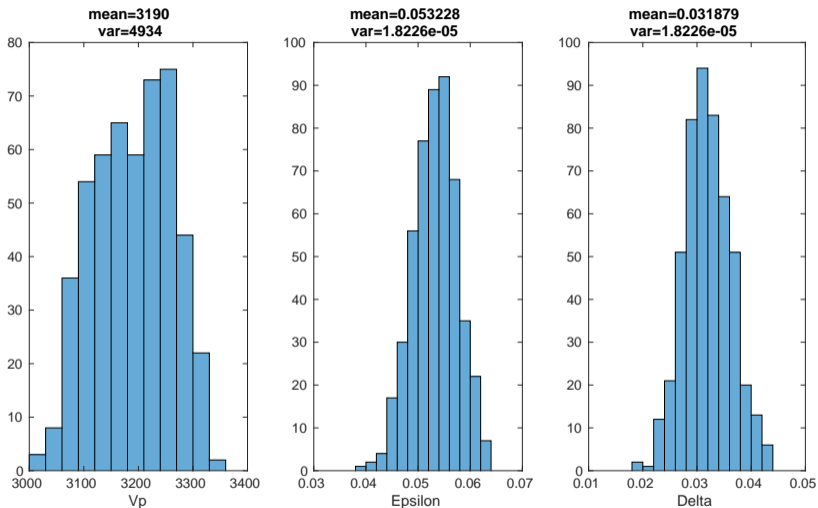


Figure 21: Deep shaly sand

# Field application: correlations

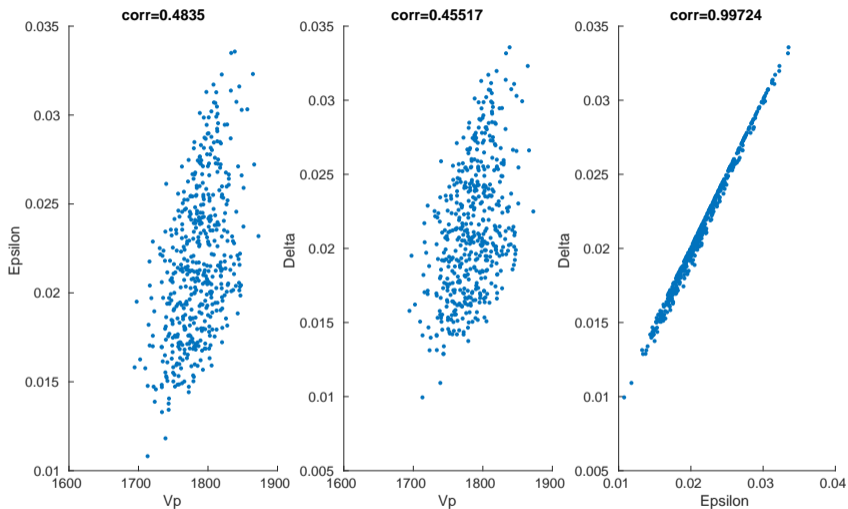


Figure 22: Shallow sandy shale

# Field application: correlations

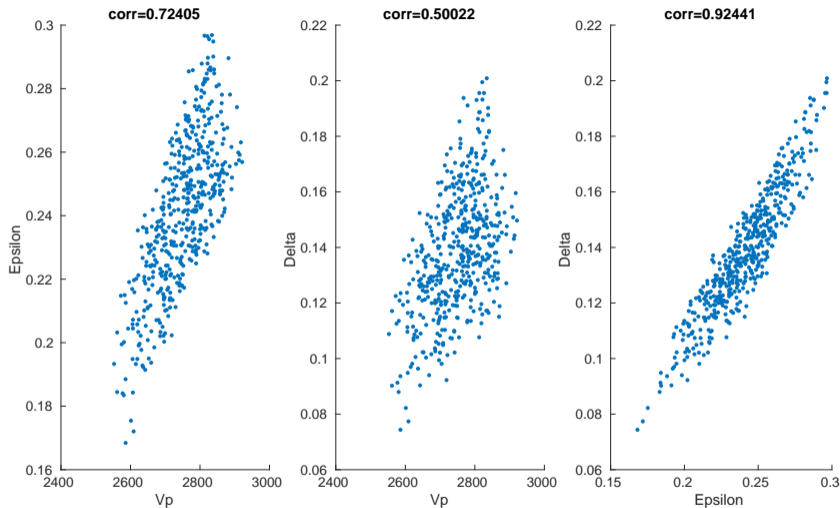


Figure 23: Deep sandy shale

# Field application: correlations

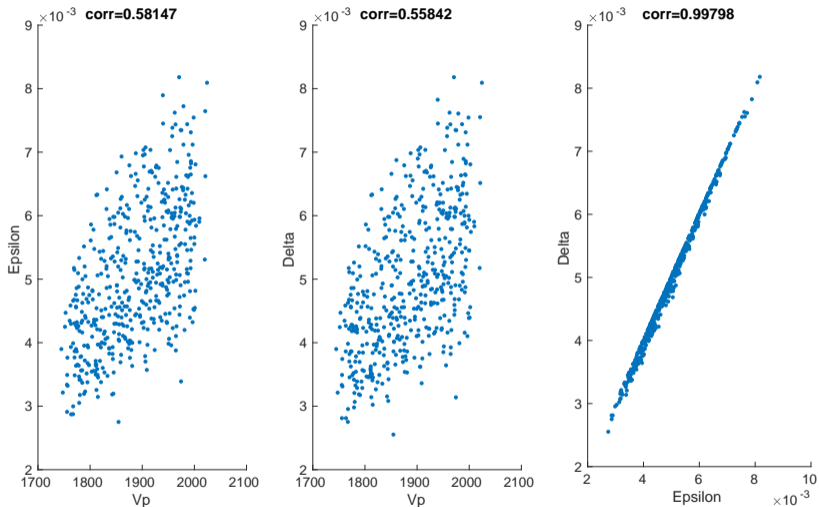


Figure 24: Shallow shaly sand

# Field application: correlations

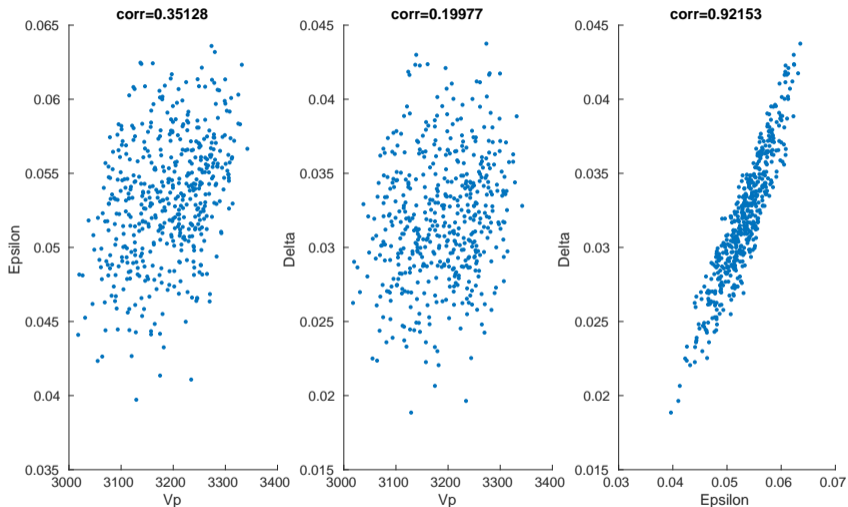


Figure 25: Deep shaly sand

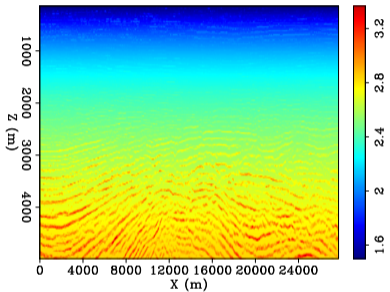


Figure 26: Velocity

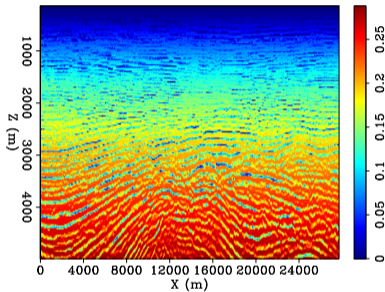


Figure 27:  $\epsilon$

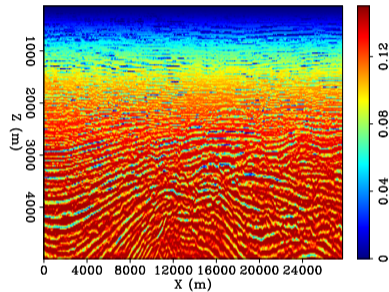


Figure 28:  $\delta$

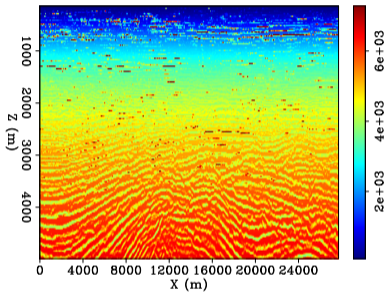


Figure 29: Velocity

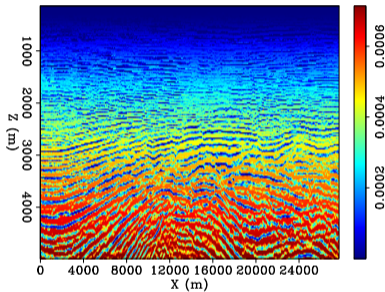


Figure 30:  $\epsilon$

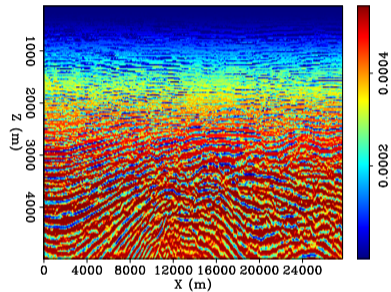


Figure 31:  $\delta$

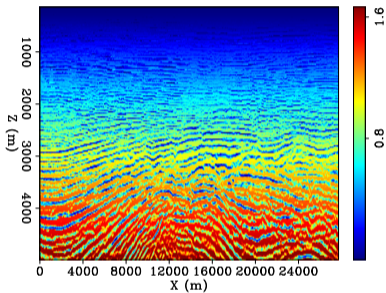


Figure 32: Velocity and  $\epsilon$

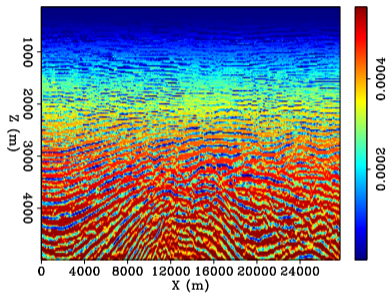


Figure 33:  $\epsilon$  and  $\delta$

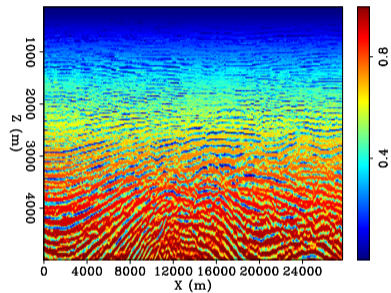


Figure 34: Velocity and  $\delta$



- Source estimation can help reduce amplitude mismatch between modeled and observed data.
- Simple synthetic example validates our derivation.
- Rock physics is one approach to obtain model covariance and precondition FWI.
- Parameters tuning and calibration are important.
- Future work: apply source estimation and rock physics preconditioning on field data.

- We thank WesternGeco for donating the shale volume.
- We thank IHS Energy Log Services Inc. for the well logs.