

## Short Note

### Residual offset-to-angle .....

*Claudio Guerra*

#### INTRODUCTION

Migration velocity analysis strongly relies on the analysis of the curvature of the reflectors in angle-domain common-image gathers (ADCIG). Unfortunately, because of uneven sampling of the wavefields, after transformation from the subsurface-offset domain image gathers (OD-CIG) (Prucha et al., 2000; Sava and Fomel, 2000), ADCIGs can show curved events which can mislead migration velocity interpretation.

Motivated by the work of (?), here I propose a method to attenuate undesirable kinematic artifacts in angle-domain common-image gathers (ADCIG) which have their origin in badly sampled receiver or source wavefields. The most direct application of the method is to pre-process ADCIGs prior to migration velocity analysis, in such a way that the remaining curved events are only related to incorrect migration velocities. This method along with illumination compensation *\*\*citeguerra\*\** are cheap ways to produce reasonable ADCIGs if compared to least-squares inversion (Prucha et al., 2000; Valenciano, 2006).

Numerical results show the bla,bla,bla....

#### BADLY SAMPLED RECEIVER WAVEFIELD

In a locally-constant velocity media, the source-wavefield is represented by the semi-circle

$$(x - x_s)^2 + z^2 = z_m^2 + (x_m - x_s)^2, \quad (1)$$

where  $x_s$  is the horizontal shot coordinate and  $(x_m, z_m)$  are the coordinates of the image point. Similarly, the receiver-wavefield is the semi-circle given by

$$(x - x_r)^2 + z^2 = z_m^2 + (x_r - x_m)^2, \quad (2)$$

where  $x_r$  is the horizontal receiver coordinate. To derive the analytical formula of the image in a ODCIG,  $I(z, x, h_x)$ , we must apply the multi-offset imaging condition

$$I(z, x, h_x) = \sum_{\omega} D^*(z, x - h_x, \omega) U(z, x + h_x, \omega), \quad (3)$$

where  $D$  is the downward is the source-wavefield,  $U$  is the receiver-wavefield,  $\omega$  is frequency,  $h_x$  is the subsurface-offset. This means to evaluate equations 1 and 2 at different subsurface-offsets. So, equations 1 and 2 reads:

$$(x - h_x - x_s)^2 + z^2 = z_m^2 + (x_m - x_s)^2 \quad (4)$$

and

$$(x + h_x - x_r)^2 + z^2 = z_m^2 + (x_r - x_m)^2. \quad (5)$$

By summing these equations and taking into account that the image is formed when  $x = x_m$ , we get the following relation between depth and subsurface-offset at the image coordinate  $x_m$ :

$$z = \sqrt{z_m^2 - h_x^2 + h_x(x_r - x_s)}. \quad (6)$$

The computation of the ADCIG,  $Q$ , from the ODCIG,  $P$ , can be viewed as a process in which we compute (a) the derivative of  $z$  with respect to  $h_x$  evaluated at  $h_x^*$ , where the slanted-path operator is tangent to  $z$ , obtaining the tangent of the reflection angle,  $\gamma$ , and (b) the depth,  $z_0$ , at which the slanted-path intersects the depth axis; and place at  $Q(\gamma, z_0)$  the amplitude collected at  $P(h_x, z)$ . The derivative  $\frac{dz}{dh_x}$  of the equation 5 is

$$\frac{dz}{dh_x} = \tan(\gamma) = \frac{x_r - x_s - 2h_x}{2z}. \quad (7)$$

The depth,  $z_0$ , in the angle gather is given by

$$z_0 = z - h \tan(\gamma). \quad (8)$$

Substituting the value for  $h_x$  from the equation 7 in equation 6 we get, after some manipulation:

$$z = \sqrt{z_m^2 + \frac{(x_r - x_s)^2}{4} \cos(\gamma)}. \quad (9)$$

The slope at  $h_x = 0$  is the tangent of the reflection angle,  $\gamma_0$ , at the image point,  $I(z_m, x_m)$ , correspondent to the considered source-receiver pair. From this we get:

$$\tan(\gamma_0) = \frac{x_r - x_s}{2z_m}. \quad (10)$$

From equation 10 and 9,  $z$  assumes the form

$$z = z_m \sqrt{1 + \tan^2(\gamma_0) \cos(\gamma)} = z_m (\sec(\gamma_0) \cos(\gamma)). \quad (11)$$

According to equations 7, 10 and 11,  $h_x$  can be recast as

$$h_x = z_m (\tan(\gamma_0) - \sec(\gamma_0) \sin(\gamma)). \quad (12)$$

Finally, substituting equations 11 and 12 in the equation 8 we get

$$z_0 = z_m (\sec(\gamma_0) \sec(\gamma) - \tan(\gamma_0) \tan(\gamma)). \quad (13)$$

Equation 13 if applied to the ADCIG resulting from the transformation to angle of the ODCIG given by equation 6 will focus the smeared energy at the point  $(\gamma_0, z_m)$  correspondent to the correct position of the ADCIG from a well-sampled receiver wavefield.

Figure 1, Figure 2, Figure 3. .

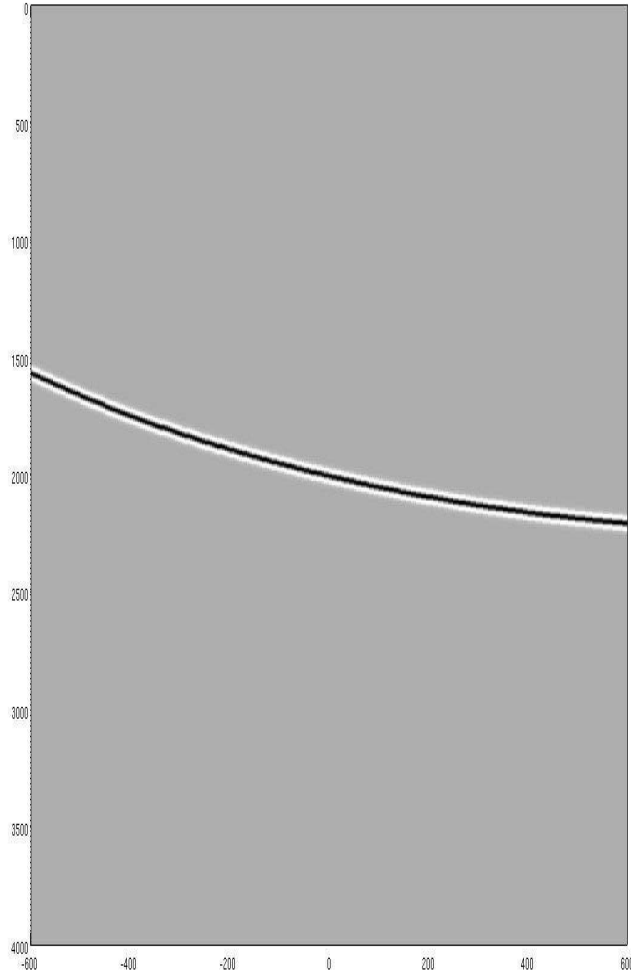


Figure 1: ODCIG badly sampled. `odcig_bad` [ER]

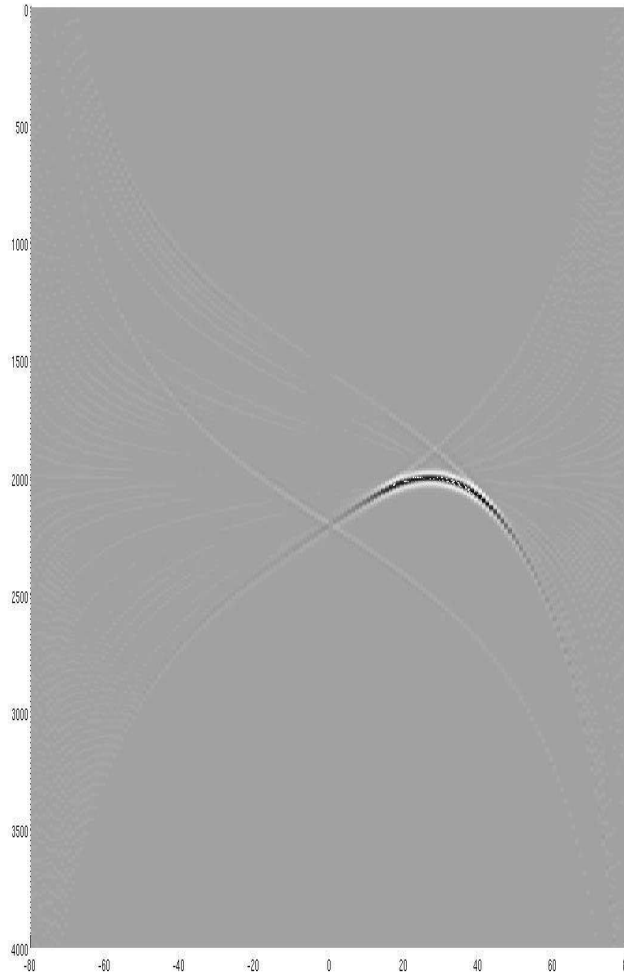


Figure 2: ADCIG resulting from the OFF2ANG of the ODCIG from Figure 1. adcig\_bad  
[ER]

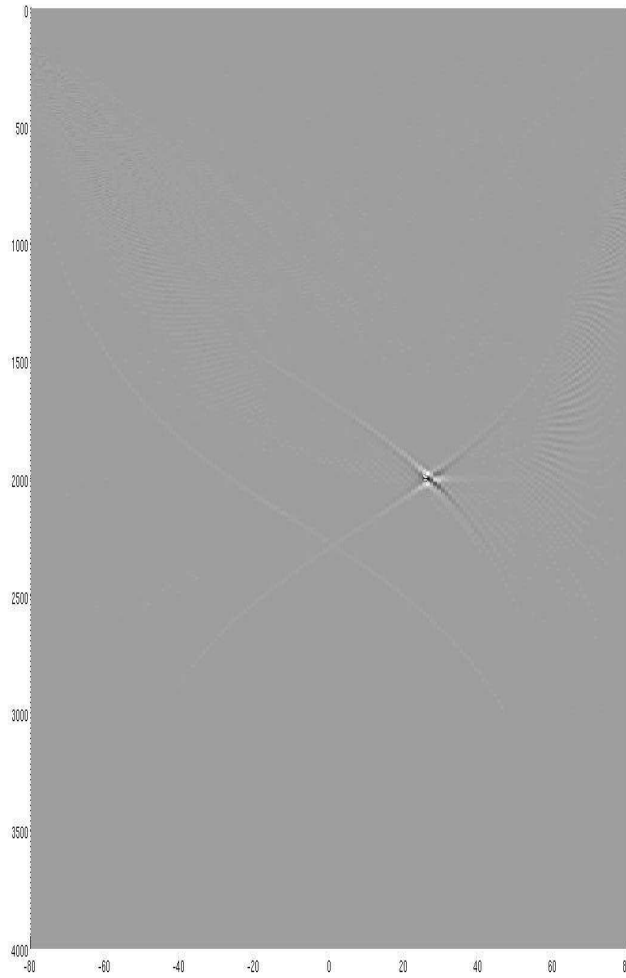


Figure 3: ADCIG resulting from the residual correction of the ADCIG from Figure 2 `adcig2_bad` [ER]

**REFERENCES**

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- Sava, P. and S. Fomel, 2000, Angle-gathers by Fourier Transform: *SEP-103*, 119–130.
- Valenciano, A. A., 2006, Target-oriented wave-equation inversion with regularization in the subsurface offset domain: *SEP-124*.